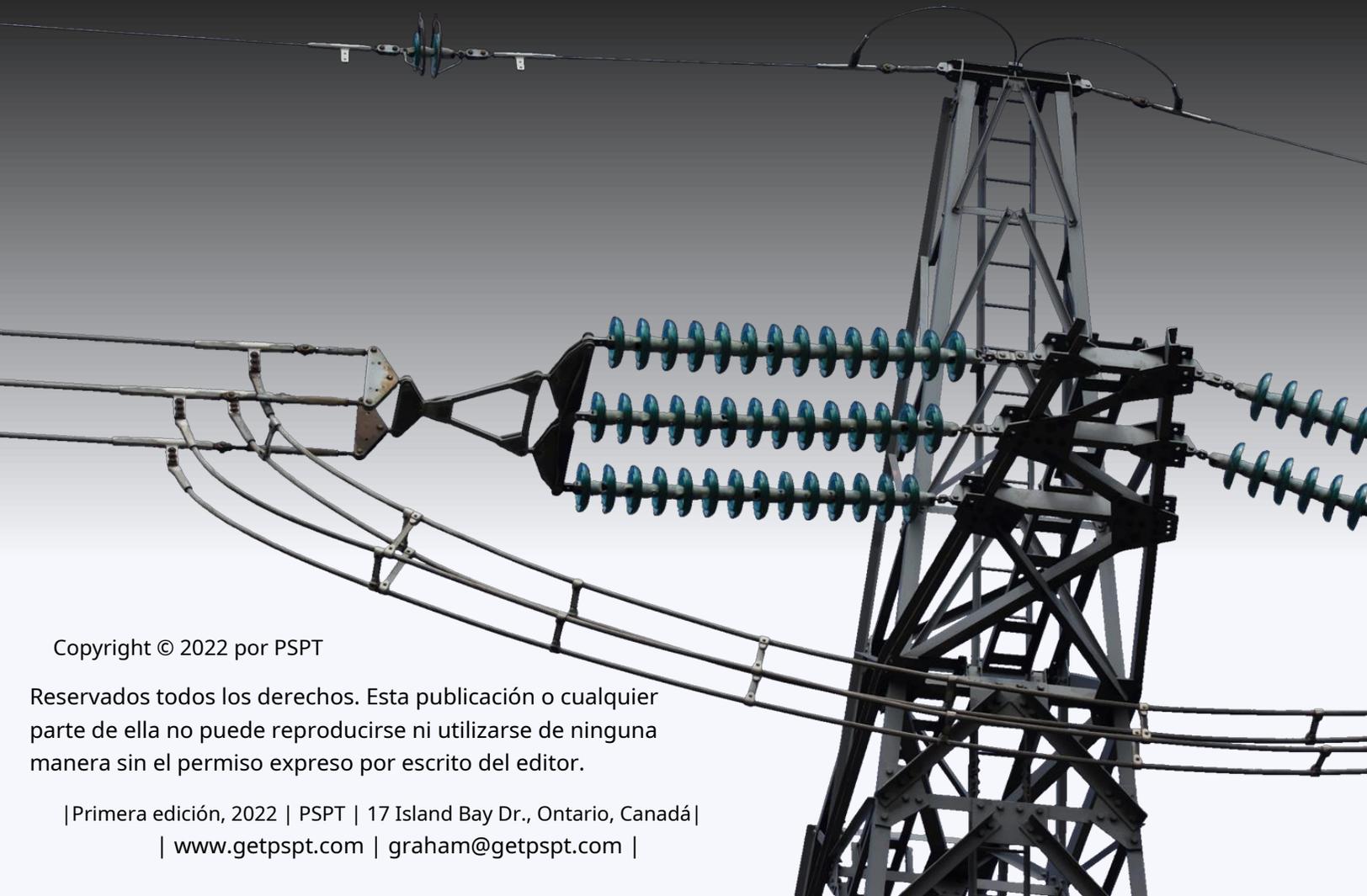


# Energía eléctrica

## Notas y fórmulas



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Las 14 secciones están numeradas individualmente.

# 1) Análisis del circuito CC

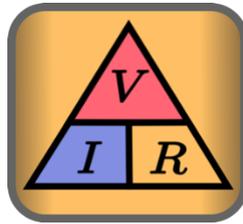
## Ley de Ohm

Corriente, voltaje y resistencia

$$V = I R$$

$$I = \frac{V}{R}$$

$$R = \frac{V}{I}$$



Conductancia

$$G = \frac{1}{R} \text{ siemens}$$

$$G = \frac{I}{V}$$

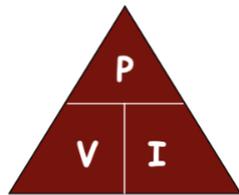
## Energía eléctrica

1 culombio =  $6,241 \times 10^{18}$  electrones Trabajo realizado = Voltios x Q(carga) Julios Trabajo realizado = Voltios x I (amperios) Potencia en julios = Trabajo/tiempo (seg) Watts

$$P = \frac{W}{t} = VI \text{ but } V = IR$$

$$P = I^2 R$$

$$P = \frac{V^2}{R}$$



$$V = \frac{P}{I} \text{ Volts}$$

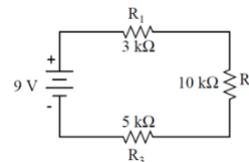
$$I = \frac{P}{V} \text{ Amps}$$

Múltiplos SI para vatios (W)

Submúltiplos			Múltiplos		
Valor	Símbolo	Nombre	Valor	Símbolo	Nombre
10 <sup>-1</sup> W.	dW	decivatio	10 <sup>1</sup> W.	grajilla	decavatio
10 <sup>-2</sup> W.	cW	centivatio	10 <sup>2</sup> W.	hW	hectovatio
10 <sup>-3</sup> W.	mW	milivatio	10 <sup>3</sup> W.	kilovatio	kilovatio
10 <sup>-6</sup> W.	μW	microvatio	10 <sup>6</sup> W.	megavatio	megavatio
10 <sup>-9</sup> W.	noroeste	nanovatio	10 <sup>9</sup> W.	G.W.	gigavatio
10 <sup>-12</sup> W.	pW	picovatio	10 <sup>12</sup> W.	tw	teravatio
10 <sup>-15</sup> W.	fW	femtovatio	10 <sup>15</sup> W.	VP	petavatio
10 <sup>-18</sup> W.	aW	attovatio	10 <sup>18</sup> W.	EW	exavatio
10 <sup>-21</sup> W.	zW	zeptovatio	10 <sup>21</sup> W.	ZW	zettavatio
10 <sup>-24</sup> W.	yW	yoctovatio	10 <sup>24</sup> W.	YW	yottawatt

Los múltiplos comunes están en **rojo** en este documento

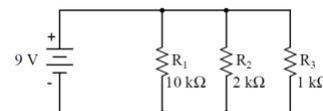
## Circuitos en serie y paralelo



$$R_T = R_1 + R_2 + R_3$$

Ley de voltaje de Kirchhoff:

La suma de las caídas de potencial (caídas de voltaje) alrededor de cualquier circuito cerrado es cero



$$\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

Ley actual de Kirchhoff:

Todas las corrientes que entran en una noda suman cero

Corrientes que entran en "+"

Corrientes que salen de "-"

## Teoremas del circuito

Propiedad de homogeneidad (escalado)

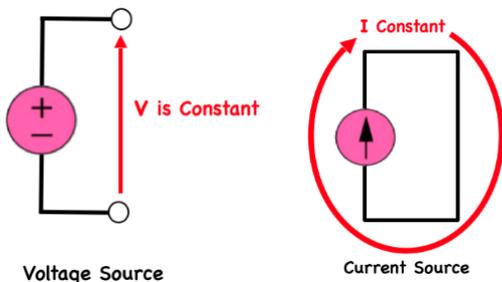
$$v = iR \rightarrow kv = kiR$$

Propiedad aditiva

$$\text{If } v_1 = i_1 R \text{ and } v_2 = i_2 R$$

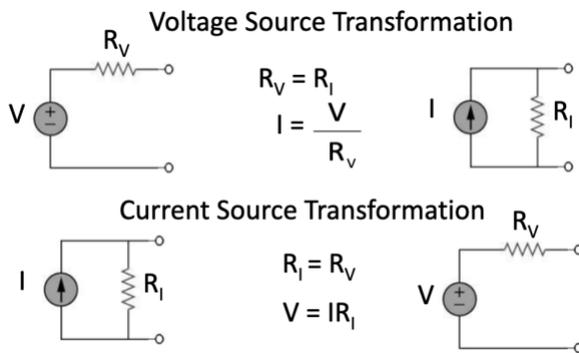
$$v_1 + v_2 = i_1 R + i_2 R = (i_1 + i_2) R$$

### Fuentes de tensión y corriente.



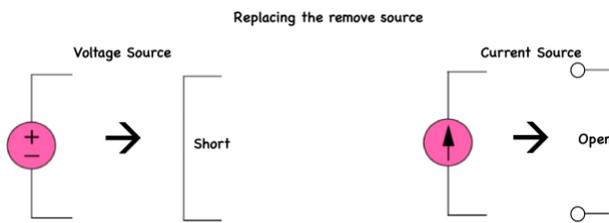
#### Transformación de fuente

La transformación de una fuente de energía de una fuente de voltaje a una fuente de corriente, o de una fuente de corriente a una fuente de voltaje.



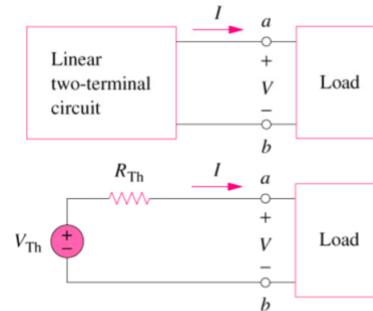
#### Teorema de superposición

En un circuito lineal con varias fuentes, la caída de corriente y tensión, para cualquier elemento del circuito, es la suma de las corrientes y tensiones producidas por cada fuente actuando de forma independiente.



#### Teorema de Thévenin

Un circuito lineal de dos terminales se puede reemplazar por un circuito equivalente que consta de una fuente de voltaje  $V_{Th}$  en serie con una resistencia  $R_{Th}$



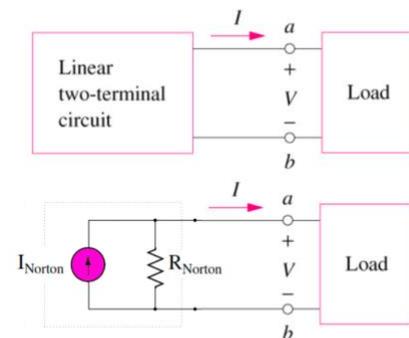
$V_{Th}$  is the open-circuit voltage at the terminals

$R_{Th}$  is the input or equivalent resistance at the terminals

#### Teorema de Norton

Un circuito lineal de dos terminales se puede reemplazar por un circuito equivalente que consta de una fuente de corriente.

$I_{Norton}$  en paralelo con una resistencia  $R_{Norton}$



$R_{Norton}$  is the input or equivalent resistance at the terminals

$I_{Norton}$  is the current flowing in the shorted terminals

#### Análisis de corriente de malla (o bucle)

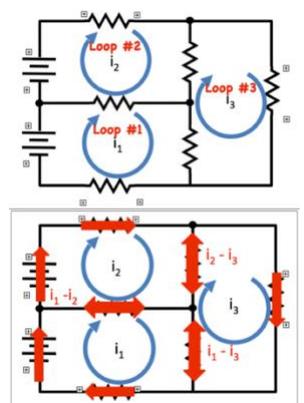
Now write the Kirchoff's Voltage Law equations for each loop:

Voltage drops are +ve and across each resistor are given by Ohms Law  $V = I \times R$

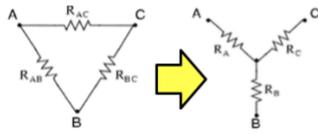
Voltage rises are -ve and equal to the voltage source ratings

Voltage drops across common resistors (resistors with two currents flowing in them) are given by Ohms Law  $V = I \times R$  and are +ve (the polarity is according to the the loop current being followed).

The  $I$  in the Ohms Law equation ( $V = I \times R$ ) is the arithmetic sum of the two currents flowing through it. The loop current being followed is +ve the other current is +ve or -ve depending on its direction flow with respect to the loop current being followed.



To convert from a Delta ( $\Delta$ ) to a Wye (Y)

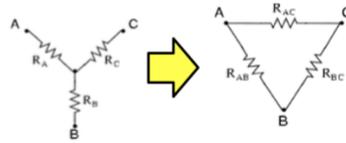


$$R_A = \frac{R_{AB} R_{AC}}{R_{AB} + R_{AC} + R_{BC}}$$

$$R_B = \frac{R_{AB} R_{BC}}{R_{AB} + R_{AC} + R_{BC}}$$

$$R_C = \frac{R_{AC} R_{BC}}{R_{AB} + R_{AC} + R_{BC}}$$

To convert from a Wye (Y) to a Delta ( $\Delta$ )

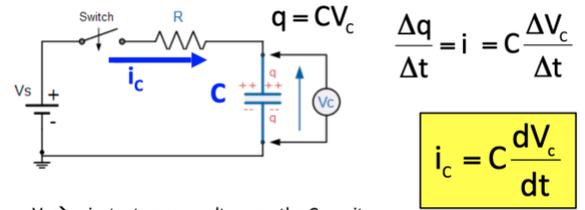


$$R_{AB} = \frac{R_A R_B + R_A R_C + R_B R_C}{R_C}$$

$$R_{BC} = \frac{R_A R_B + R_A R_C + R_B R_C}{R_A}$$

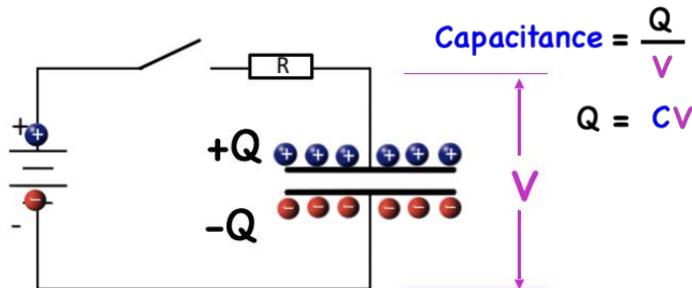
$$R_{AC} = \frac{R_A R_B + R_A R_C + R_B R_C}{R_B}$$

### La ley de Ohm y un condensador



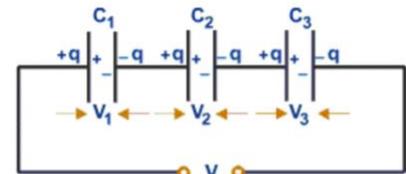
- $V_c \rightarrow$  instantaneous voltage on the Capacitor
- $q \rightarrow$  charge on the capacitor
- $C \rightarrow$  the capacitance of the capacitor
- $\Delta q \rightarrow$  The change in  $q \rightarrow$  charge on the capacitor
- $\Delta t \rightarrow$  The change in time
- $i_c \rightarrow$  current to the capacitor

### Campos eléctricos y C



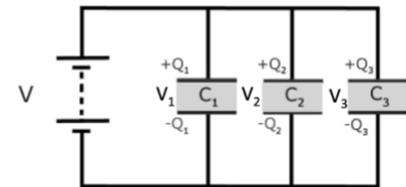
Capacitance  $\rightarrow$  farad (F)

### Capacitors in Series

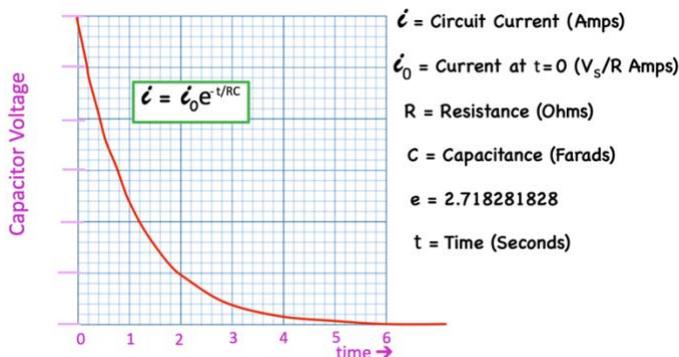
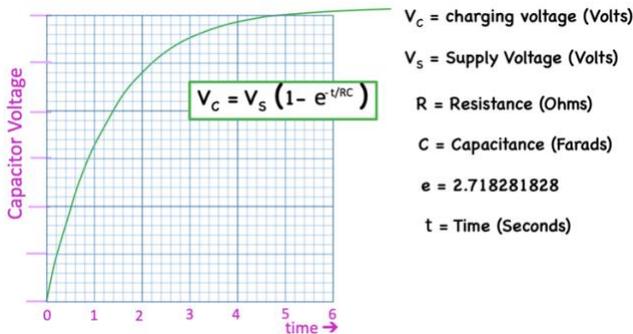


$$\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}$$

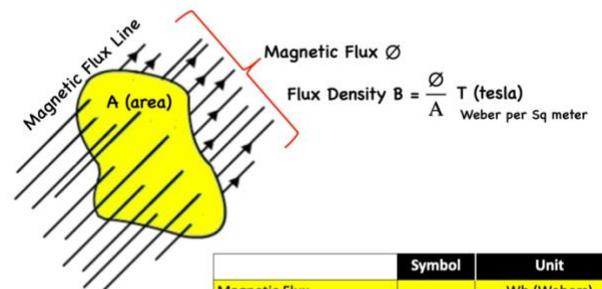
### Capacitors in parallel



$$C_T = C_1 + C_2 + C_3$$

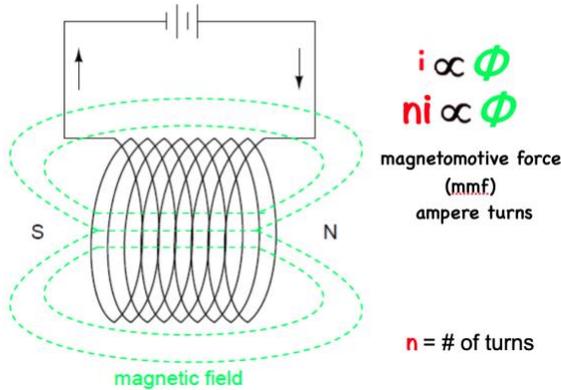


### Magnetic Flux & Flux Density

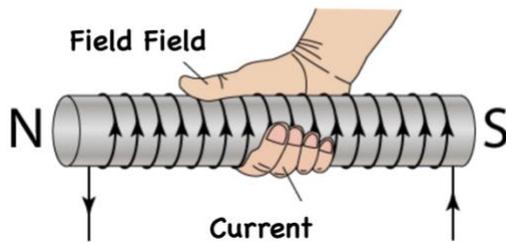


	Symbol	Unit
Magnetic Flux		Wb (Webers)
Magnetic Flux Density	<b>B</b>	T (tesla) Weber per Sq meter

## Electromagnetism

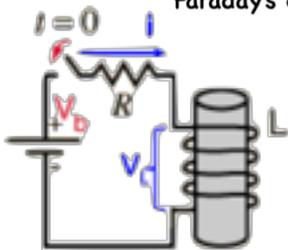


## Determining the Pole of the Magnetic Field



## Inducción electromagnética

Faraday's equation for induced voltage



$$V_R = IR$$

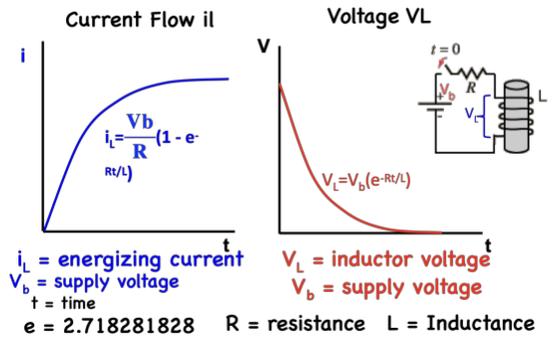
$$V_L = -N \frac{\Delta\phi}{\Delta t}$$

$$i \propto \Phi \text{ or } \Phi = Ki$$

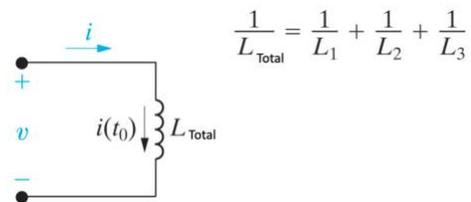
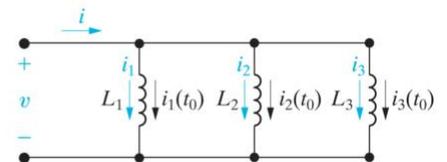
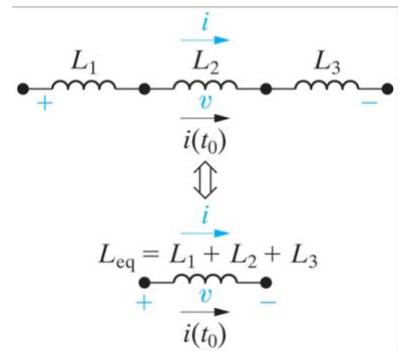
- $V_L \rightarrow$  instantaneous induced voltage  $\frac{\Delta\phi}{\Delta t} = K \frac{\Delta i}{\Delta t}$  or  $\frac{d\phi}{dt} = K \frac{di}{dt}$
- $N \rightarrow$  Number of turns in a wire coil
- $\Delta\phi \rightarrow$  The change in magnetic flux (webers)
- $\Delta t \rightarrow$  The change in time
- $\Delta\phi / \Delta t$  The rate of change of flux linkage

$$V_L = -L \frac{di}{dt} \quad (L = NK)$$

## Energizar un inductor

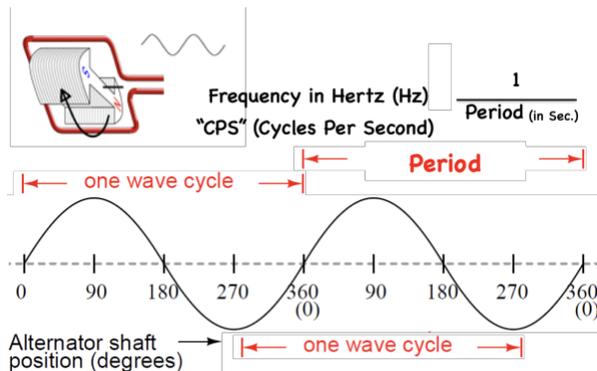


## Series & Parallel Inductors



# 2) Análisis del circuito de CA

## Ondas sinusoidales y valores RMS



The r.m.s. value of an a.c. supply is equal to the direct current which would dissipate energy at the same rate in a given resistor

We can use the same logic to define the r.m.s. value of the voltage of an alternating voltage supply.

$$V_{rms} = \frac{V_{max}}{\sqrt{2}} \quad I_{rms} = \frac{I_{max}}{\sqrt{2}}$$

where  $V_{max}$  is the maximum (or peak) value of the voltage

where  $I_{max}$  is the maximum (or peak) value of the current

For **sinusoidal** current & voltage

$$P_{avg} = (I_{RMS})^2 R$$

$$V_{RMS} = I_{RMS} R \quad \text{Ohm's Law}$$

$$R = \frac{V_{RMS}}{I_{RMS}}$$

$$P_{avg} = I_{RMS} V_{RMS}$$

For circuits with resistive loads only

### Scalar

magnitude

Scalar quantities  
Length, Area, Volume,  
Speed,  
Mass, Density  
Temperature, Pressure  
Energy, Entropy  
Work, Power



### Vector

magnitude  
direction

Vector quantities  
Displacement, Direction,  
Velocity, Acceleration,  
Momentum, Force,  
Electric field, Magnetic field

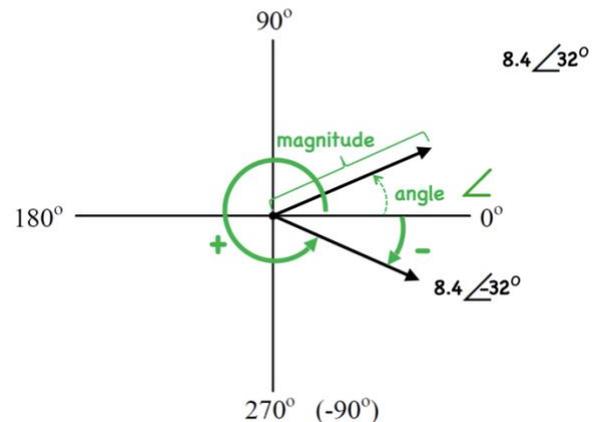


### Phasor

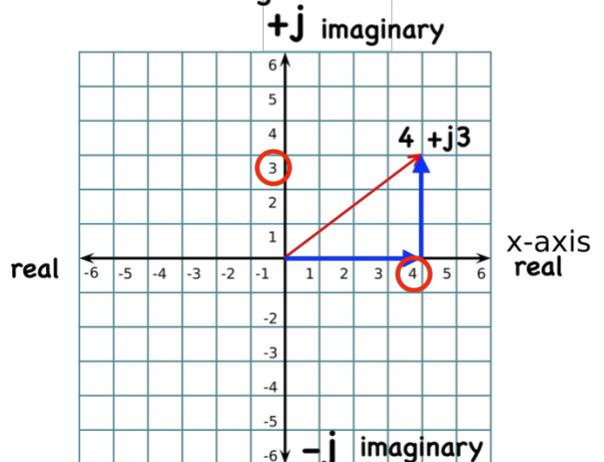
direction  
magnitude  
phase angle



## Polar Notation



## Rectangular Notation

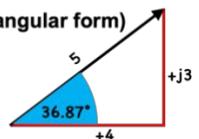


$4 + j3$  (rectangular form)

$5 \angle 36.87^\circ$  (polar form)  $\rightarrow$  (rectangular form)

$(5)(\cos 36.87^\circ) = 4$  (real component)

$(5)(\sin 36.87^\circ) = 3$  (imaginary component)



$4 + j3$  (rectangular form)  $\rightarrow$  (polar form)

$5 \angle 36.87^\circ$  (polar form)

$$\sqrt{4^2 + 3^2} = 5$$

$$\text{Arctan} \left( \frac{3}{4} \right) = 36.87^\circ \text{ angle}$$

### Phasor Math

rectangular  $\rightarrow$  polar

**Multiplication**  $(A \angle B^\circ)(X \angle Y^\circ) = AX \angle (B^\circ + Y^\circ)$

**Division**  $(A \angle B^\circ) \div (X \angle Y^\circ) = \frac{A}{X} \angle (B^\circ - Y^\circ)$

polar  $\rightarrow$  rectangular

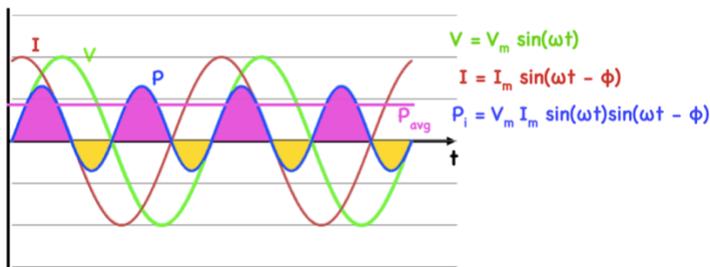
**Addition**  $(A, B) + (X, Y) = [(A + X), (B + Y)]$

**Subtraction**  $(A, B) - (X, Y) = [(A - X), (B - Y)]$

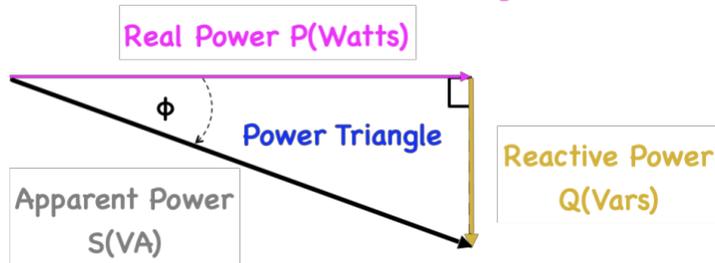
### Reactancia e impedancia

### Electric Power

$$P = V_i \times I_i$$



The average power is...  $P_{avg} = \frac{V_m I_m}{2} \cos(\phi)$



$\phi$  is known as the "Power Factor Angle"

$\cos(\phi)$  is known as the "Power Factor"

$$P_{avg} = \frac{V_m I_m}{2} \cos(\phi)$$

$$P_{avg} = \frac{V_m}{\sqrt{2}} \times \frac{I_m}{\sqrt{2}} \cos(\phi)$$

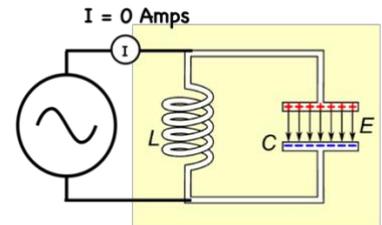
$$V_{rms} = \frac{V_m}{\sqrt{2}} \quad \text{And} \quad I_{rms} = \frac{I_m}{\sqrt{2}}$$

$$P_{avg} = V_{rms} \times I_{rms} \cos(\phi)$$

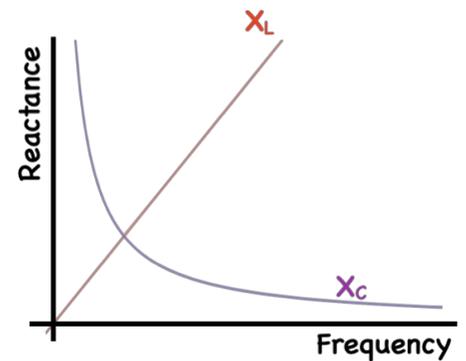
$$Q_{avg} = V_{rms} \times I_{rms} \sin(\phi)$$

$$\text{Apparent Power (VA)} = V_{rms} \times I_{rms}$$

### Frecuencia armónica



Generator frequency = LC frequency



$$2\pi fL = \frac{1}{2\pi fC}$$

$$2\pi f^2 L = \frac{1}{2\pi C}$$

$$f^2 = \frac{1}{2\pi \times 2\pi LC}$$

$$f = \frac{1}{2\pi \sqrt{LC}}$$

# 3) Análisis de potencia en circuitos de CA

## Energía eléctrica

Work done or electric energy (E) is the movement of charge (Q) caused by EMF

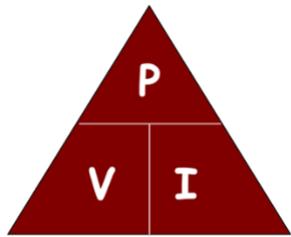
$E = V \times Q$   
 P is the rate at which electric energy (E) is transferred by an electric circuit  
 $P = \frac{E}{t} = \frac{VQ}{t} = V \times Q/t = V \times I$   
 one electron =  $1/Q = 1.6 \times 10^{-19}$  coulombs  
 1 coulomb = 6,250,000,000,000,000,000 electrons  
 1 amp = 1 coulomb passing by in 1 second of time

## Energía eléctrica

Energy = Power x Time **Joule (J)**  
**Watt hour**  
**Watt Sec**  
**kilowatt hour**

SI multiples for watt hour (W-h)					
Submultiples			Multiples		
Value	Symbol	Name	Value	Symbol	Name
$10^{-3}$	mW-h	milliwatt hour	$10^3$	kW-h	kilowatt hour
$10^{-6}$	$\mu$ W-h	microwatt hour	$10^6$	MW-h	megawatt hour
			$10^9$	GW-h	gigawatt hour
			$10^{12}$	TW-h	terawatt hour
			$10^{15}$	PW-h	petawatt hour

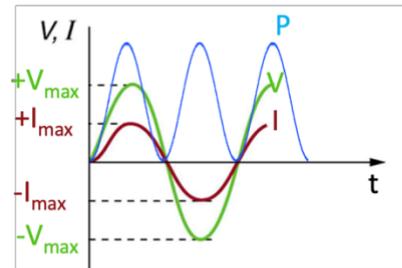
Electrical power is measured in **Watts** (symbol: **W**)



$P = V I$  watts  
 $V = \frac{P}{I}$  volts  
 $I = \frac{P}{V}$  amps

## Alternating Current and Voltage

$P_i = V_i \times I_i$



**P is sinusoidal**  
**P's frequency is 2 X that of V & I**  
**P is greater than zero**

Múltiplos SI para vatios (W)

Submúltiplos			Múltiplos		
Valor	Símbolo	Nombre	Valor	Símbolo	Nombre
$10^{-1}W$	dw	decivatio	$10_1W$	grajilla	decavatio
$10^{-2}W$	cW	centivatio	$10_2W$	hW	hectovatio
$10^{-3}W$	<b>mW</b>	<b>milivatio</b>	$10_3W$	kilovatio	<b>kilovatio</b>
$10^{-6}W$	<b><math>\mu</math>W</b>	<b>microvatio</b>	$10_6W$	megavatio	<b>megavatio</b>
$10^{-9}W$	noroste	<b>nanovatio</b>	$10_9W$	<b>G.W.</b>	<b>gigavatio</b>
$10^{-12}W$	<b>pW</b>	<b>picovatio</b>	$10_{12}W$	<b>tw</b>	<b>teravatio</b>
$10^{-15}W$	fW	femtovatio	$10_{15}W$	VP	petavatio
$10^{-18}W$	aw	attovatio	$10_{18}W$	EW	exavatio
$10^{-21}W$	zW	zeptovatio	$10_{21}W$	ZW	zettavatio
$10^{-24}W$	yW	yoctovatio	$10_{24}W$	YW	yottavatio

Los múltiplos comunes están en **negrita**

### Resistor

$|X_R| = R$   
 $\bar{X}_R = |X_R| \angle 0^\circ = X_R$

$Z_T = X_R$

### Resistor-Inductor

$|X_L| = 2\pi fL$   
 $\bar{X}_L = |X_L| \angle 90^\circ = jX_L$

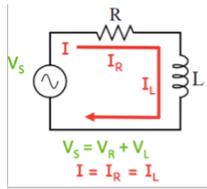
$Z_T = X_R + X_L$

### Resistor-Capacitor

$|X_C| = \frac{1}{2\pi fC}$   
 $\bar{X}_C = |X_C| \angle -90^\circ = -jX_C$

$Z_T = X_R + X_C$

Alimentación de CA



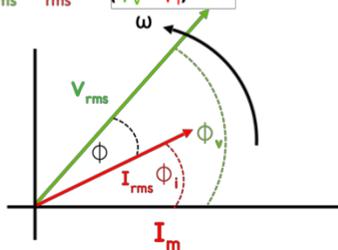
$$P_{avg} = \frac{V_m I_m}{2} \cos \phi$$

$$P_{avg} = \frac{V_m}{\sqrt{2}} \times \frac{I_m}{\sqrt{2}} \cos \phi$$

$$V_{rms} = \frac{V_m}{\sqrt{2}} \quad \text{And} \quad I_{rms} = \frac{I_m}{\sqrt{2}}$$

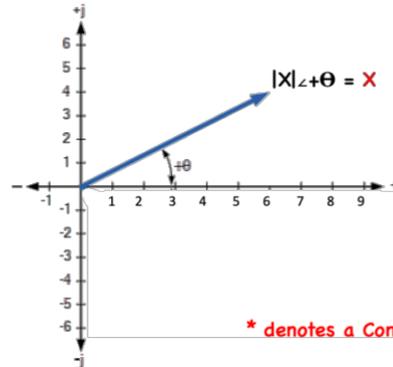
$$P_{avg} = V_{rms} \times I_{rms} \cos(\phi_v - \phi_i) \quad \text{Real Power}$$

$$Q_{avg} = V_{rms} \times I_{rms} \sin(\phi_v - \phi_i) \quad \text{Reactive Power}$$



Poder complejo

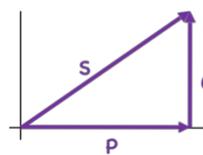
Red => Phasors (Vectors)  
Black => Non-Vector Quantities



$$\begin{aligned} \mathbf{X} \bullet \mathbf{X}^* &= |\mathbf{X}|_{L+\theta} \bullet |\mathbf{X}|_{L-\theta} \\ &= |\mathbf{X}| \bullet |\mathbf{X}|_{L-L} \\ &= |\mathbf{X}|^2 \bullet 0 \\ &= |\mathbf{X}|^2 \end{aligned}$$

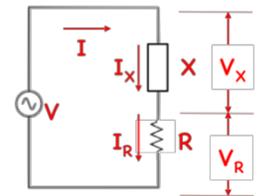
\* denotes a Conjugate phasor (vector)

$$\text{Complex power } S = \mathbf{V} \bullet \mathbf{I}^*$$



$$S = |\mathbf{I}|^2 \bullet Z$$

$$S = \frac{|\mathbf{V}|^2}{Z^*}$$



$$P = V_R \bullet I_R^*$$

$$P = |\mathbf{I}_R|^2 \bullet R$$

$$P = \frac{|\mathbf{V}_R|^2}{R^*}$$

$$V = V_X$$

$$I = I_X$$

$$Z = jX$$

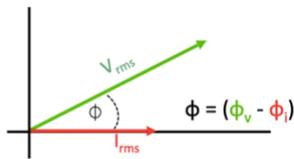
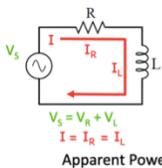
$$S = Q$$

Red is a Phasor  
\* is a Conjugate

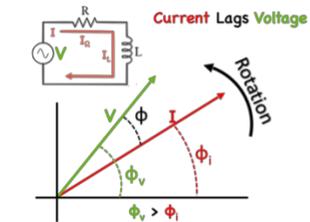
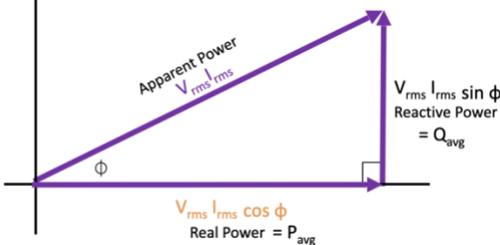
$$Q = V_X \bullet I_X^*$$

$$Q = |\mathbf{I}_X|^2 \bullet jX$$

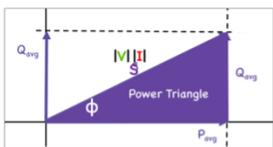
$$Q = \frac{|\mathbf{V}_X|^2}{jX^*}$$



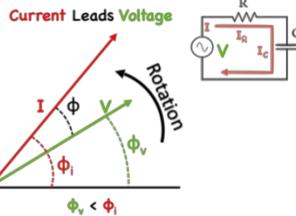
Apparent Power



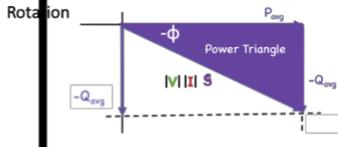
$\phi = (\phi_v - \phi_i)$  Power Factor Angle (Positive)



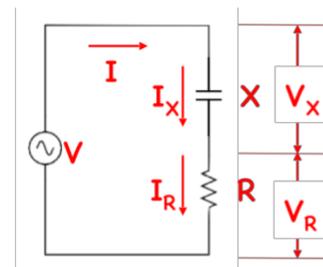
$Q_{avg}$  is Positive  
 $P_{avg}$  is Positive



$\phi = (\phi_v - \phi_i)$  Power Factor Angle (Negative)



$Q_{avg}$  is Negative  
 $P_{avg}$  is Positive



$$X_L = 2\pi fL$$

$$(X_L)^* = -2\pi fL$$

f = frequency in cps

$\pi = 3.14159$

L = inductance in henry's

$$X_C = -\frac{1}{2\pi fC}$$

$$(X_C)^* = \frac{1}{2\pi fC}$$

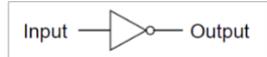
C = capacitance in farads

Red is a Phasor  
\* is a Conjugate

# 4) Circuitos eléctricos digitales

## Puertas

### Inverter, or NOT gate

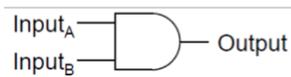


NOT gate truth table

Input	Output
0	1
1	0

### The AND gate

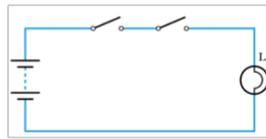
2-input AND gate



The truth table

A	B	Output
0	0	0
0	1	0
1	0	0
1	1	1

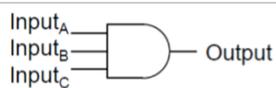
S1 S2



The truth table

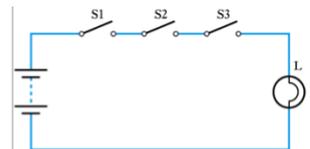
S1	S2	L
0	0	0
0	1	0
1	0	0
1	1	1

3-input AND gate



The truth table

A	B	C	Output
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

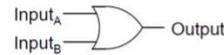


The truth table

S1	S2	S3	L
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

### The OR gate

2-input OR gate



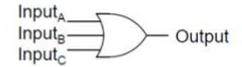
The truth table

A	B	Output
0	0	0
0	1	1
1	0	1
1	1	1

Output will be "low" (0) if and only if all inputs are "low" (0)

Output will be "high" (1) if any of the inputs are "high" (1)

3-input OR gate

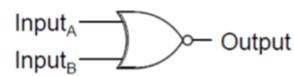


The truth table

A	B	C	Output
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	1

### The NOR gate

2-input NOR gate



The truth table

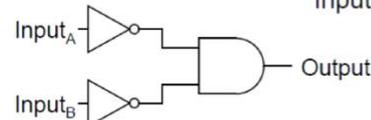
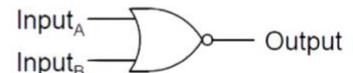
A	B	Output
0	0	1
0	1	0
1	0	0
1	1	0

Output is "high" (1) only when all inputs are "low" (0)

Output goes "low" (0) if any of the inputs are made "high" (1)

### The Negative-AND gate

2-input Negative-AND gate



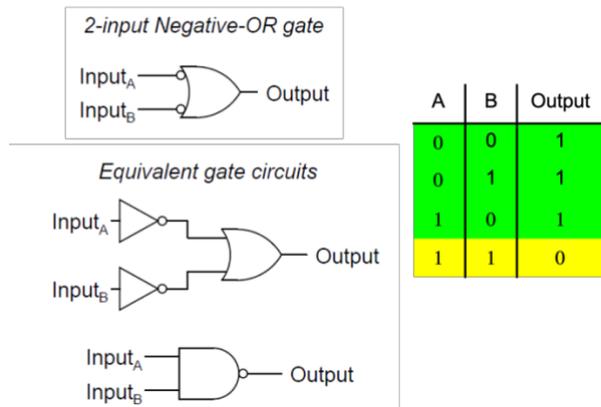
The truth table

A	B	Output
0	0	1
0	1	0
1	0	0
1	1	0

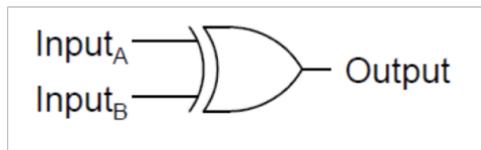
Output is "high" (1) only when all inputs are "low" (0)

Output goes "low" (0) if any of the inputs are made "high" (1)

### The Negative-OR gate



### The Exclusive-OR gate (sometimes called XOR)



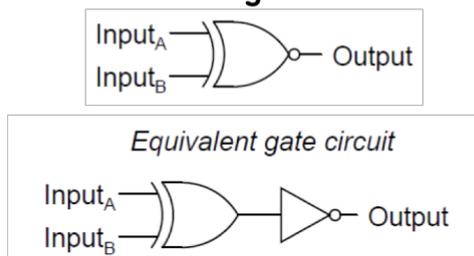
A	B	Output
0	0	0
0	1	1
1	0	1
1	1	0

Output a "low" (0) logic level if the inputs are at the *same*

Output a "high" (1) logic level if the inputs are at *different*

Output a "low" (0) logic level if the inputs are at the *same*

### The Exclusive-NOR gate XNOR gate



A	B	Output
0	0	1
0	1	0
1	0	0
1	1	1

Output a "high" (1) logic level if the inputs are at the *same*

Output a "low" (0) logic level if the inputs are at *different*

Output a "high" (1) logic level if the inputs are at the *same*

### AND gate:

output is high only if both inputs high (A AND B are high).

### OR gate:

output is high if input A OR input B are high.

### NAND gate:

output is NOT high if both A input AND B input are high.

### NOR gate:

output is NOT high if either A input OR B input are high.

### A Negative-AND gate:

behaves like a NOR gate.

### A Negative-OR gate:

behaves like a NAND gate.

### Exclusive-OR gate:

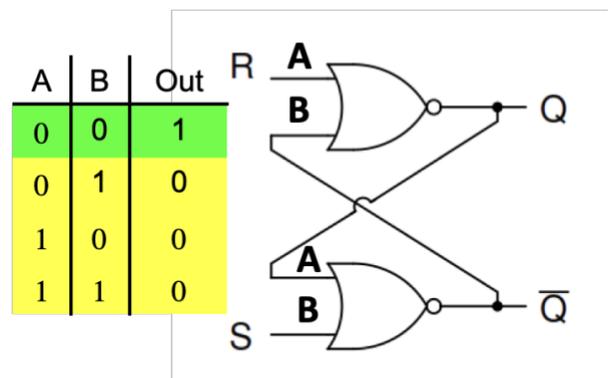
output is high if the input logic levels are *different*.

### Exclusive-NOR gate:

output is high if the input logic levels are the *same*.

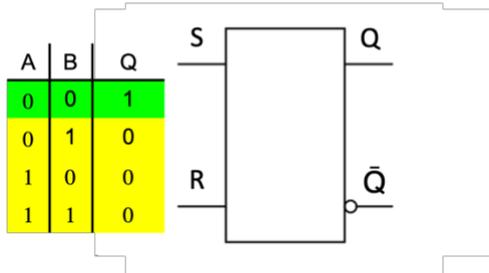
## Chancas y multivibradores

### The S-R Latch



S	R	Q	$\bar{Q}$
0	0	latch	Latch
0	1	0	1
1	0	1	0
1	1	0	0

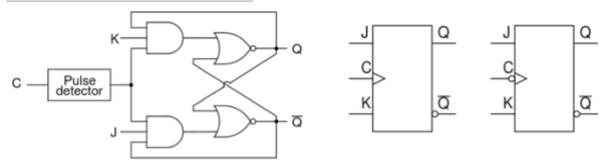
### The S-R Latch



S	R	Q	$\bar{Q}$
0	0	latch	Latch
0	1	0	1
1	0	1	0
1	1	0	0

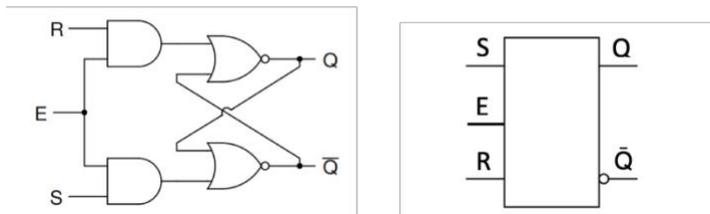
*Reset*  
*Set*

### The J-K Flip-Flop



C	J	K	Q	$\bar{Q}$
1	0	0	Latch	Latch
1	0	1	0	1
1	1	0	1	0
1	1	1	Toggle	Toggle
X	0	0	Latch	Latch
X	0	1	Latch	Latch
X	1	0	Latch	Latch
X	1	1	Latch	Latch

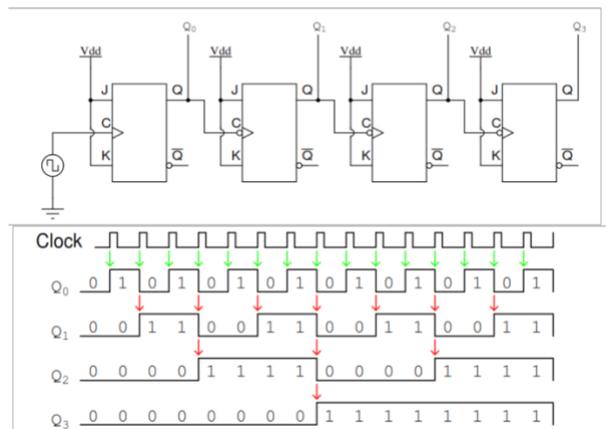
### The Gated S-R Latch



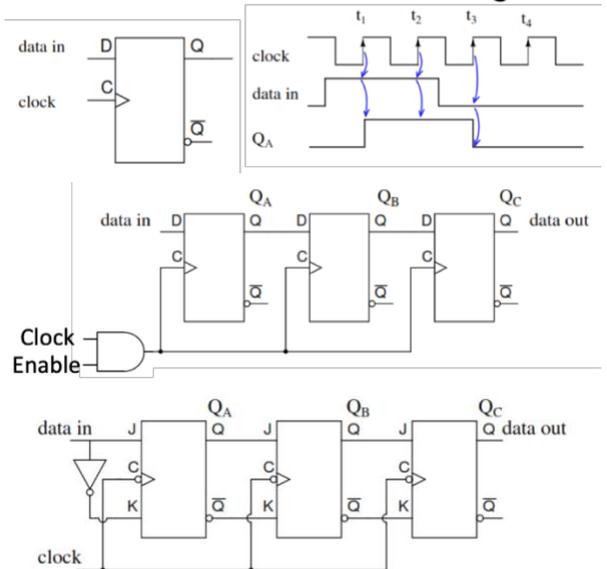
E	S	R	Q	$\bar{Q}$
0	0	0	Latch	Latch
0	0	1	Latch	Latch
0	1	0	Latch	Latch
0	1	1	Latch	Latch
1	0	0	Latch	Latch
1	0	1	0	1
1	1	0	1	0
1	1	1	0	0

### Contadores y registros de turnos

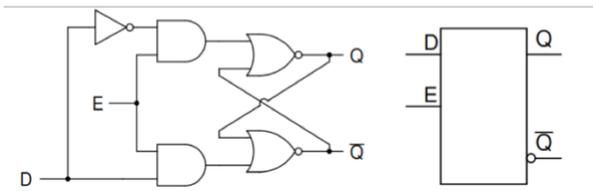
#### A Four-Bit "Up" Counter



#### Serial-In/Serial-Out Shift Register

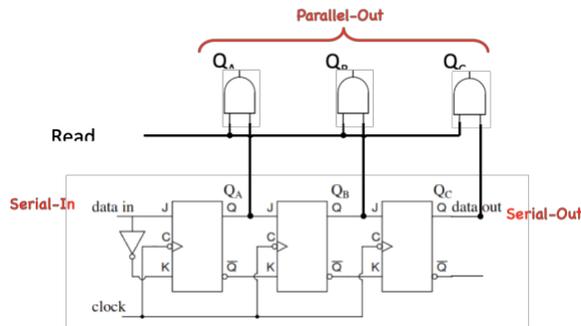


### The D Latch



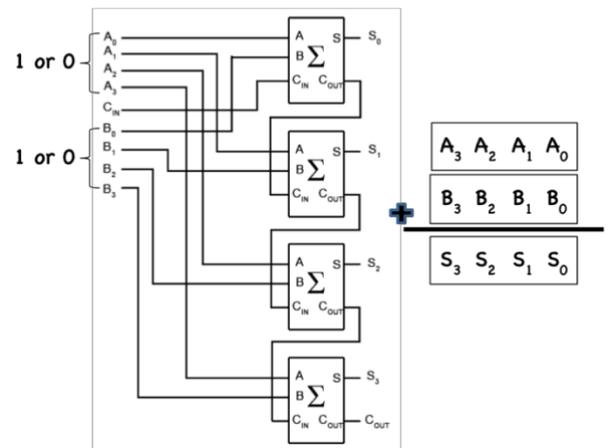
E	D	Q	$\bar{Q}$
0	0	Latch	Latch
0	1	Latch	Latch
1	0	0	1
1	1	1	0

## Serial-In/Parallel-Out Shift Register

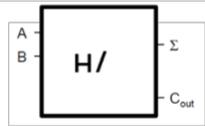
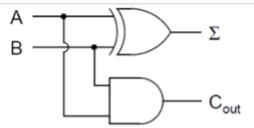


sumadores

## Parallel Adders



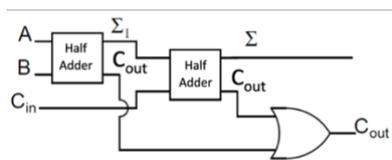
## The Half Adder



	A	B	Σ	C <sub>out</sub>
0 plus 0 = 0	0	0	0	0
0 plus 1 = 1	0	1	1	0
1 plus 0 = 1	1	0	1	0
1 plus 1 = 0	1	1	0	1

Carry 1

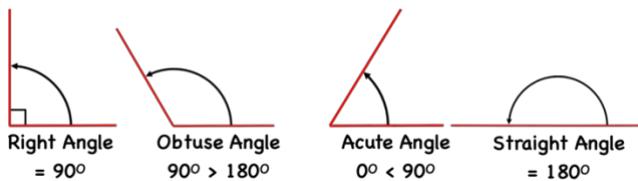
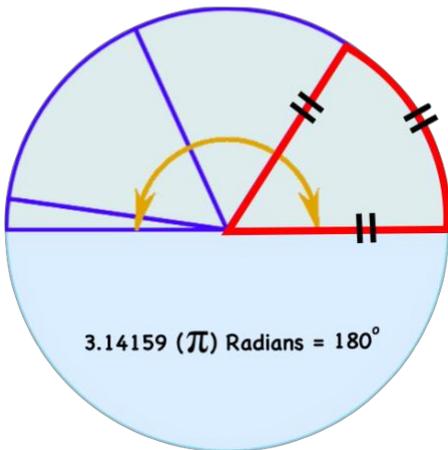
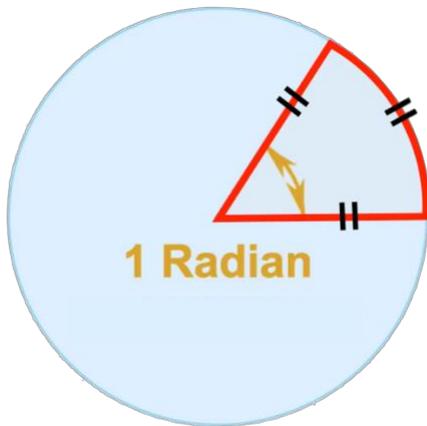
## The Full Adder



A	B	Carry-In	Sum	Carry-Out
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

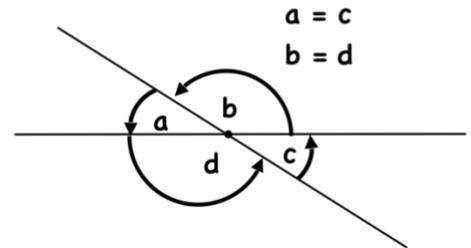
# 5) Trigonometría eléctrica

## Medición de ángulo



**Congruent Angles** - equal  $\cong$   
**Supplemental angles** - add to  $180^\circ$   
**Complementary angles** - add to  $90^\circ$

## Opposite Angles of Intersecting Lines Are Equal



$$a = c$$

$$b = d$$

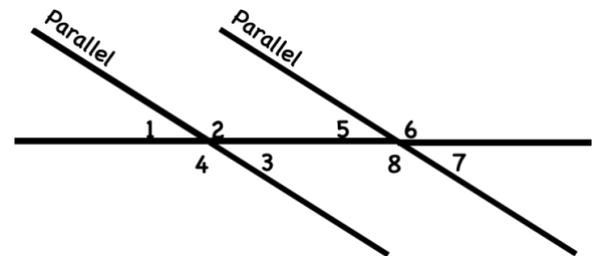
$$a + b = 180^\circ$$

$$c + b = 180^\circ$$
~~$$a + b = c + b$$~~

$$a = c$$

$$a + d = 180^\circ$$
~~$$a + b = 180^\circ$$~~
~~$$a + d = a + b$$~~

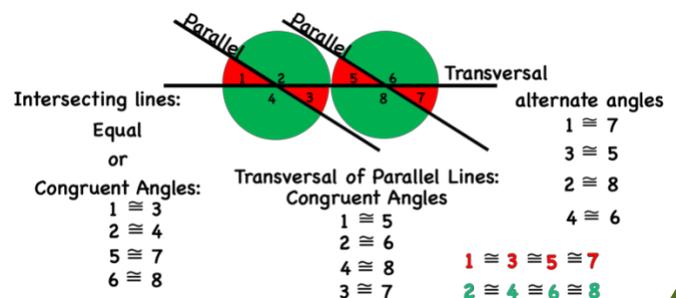
$$b = d$$



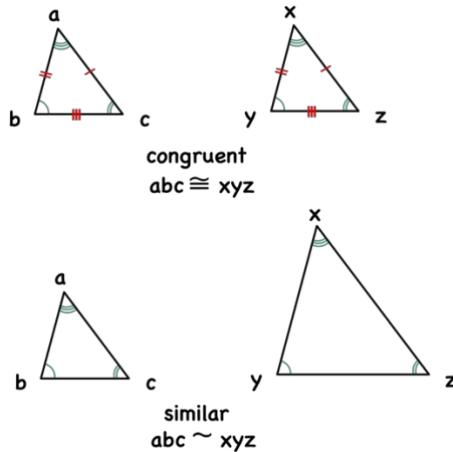
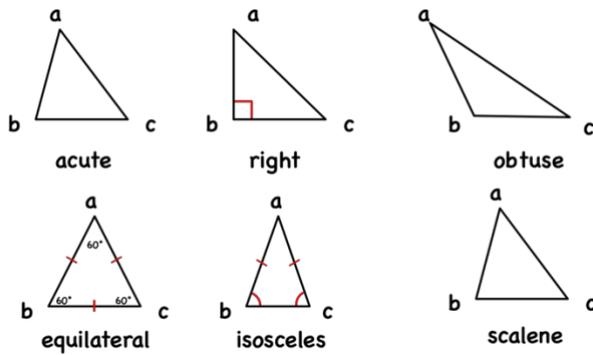
Transversal-same side exterior angles 1; 6; 4; 7  
 -same side interior angles 2; 3; 8; 5

### Corresponding Angles

same side of Transversal 1 & 5  
 and  
 same position w.r.t. parallel lines 2 & 6  
 4 & 8  
 3 & 7



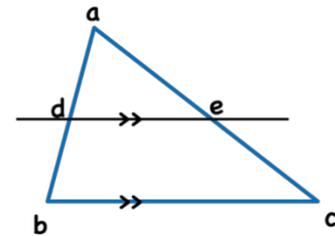
## triángulos



## Basic Proportionality Theorem

A line parallel to one side of a triangle divides the other two sides in equal proportions

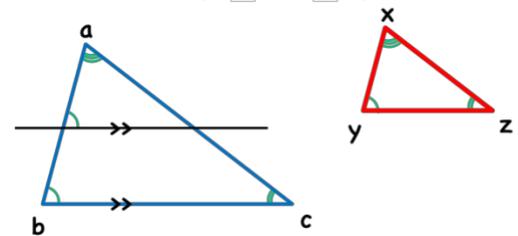
$$\frac{ad}{db} = \frac{ae}{ec}$$



## Triangle Proportionality Theorem

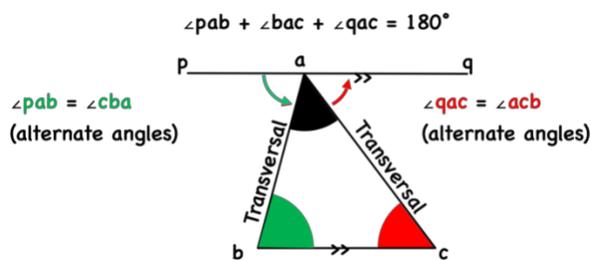
If two triangles are similar their sides are proportional

$$\frac{ab}{xy} = \frac{ac}{xz} = \frac{bc}{yz}$$



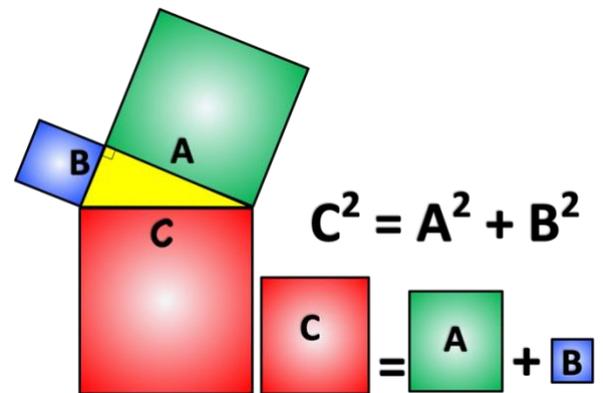
## Propiedad de la suma de ángulos de un triángulo

**Theorem 1:** The sum of interior angles of a triangle is  $180^\circ$



The sum of the interior angles of a triangle is  $180^\circ$

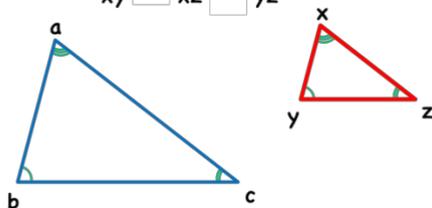
## El teorema de Pitágoras



## Triangle Proportionality Theorem

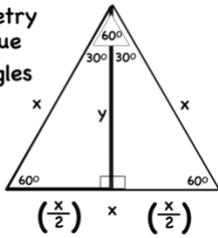
If two triangles are similar their sides are proportional

$$\frac{ab}{xy} = \frac{ac}{xz} = \frac{bc}{yz}$$



### Triángulos y proporciones únicos

Geometry Unique Triangles



$$x^2 = \left(\frac{x}{2}\right)^2 + y^2$$

$$y^2 = -\left(\frac{x}{2}\right)^2 + x^2$$

$$= -\frac{x^2}{4} + x^2$$

$$= -\frac{x^2}{4} + \frac{4x^2}{4}$$

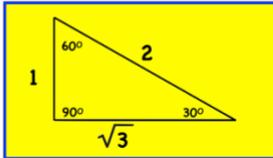
$$= \frac{-x^2 + 4x^2}{4} = \frac{3x^2}{4}$$

$$y = \sqrt{\frac{3x^2}{4}} = \sqrt{3} \cdot \frac{x}{2}$$

Let  $x = 2$

$$= \sqrt{3} \cdot \frac{2}{2}$$

$$y = 3$$



$$\frac{\text{opposite}}{\text{hypotenuse}} = \text{sine (sin}\theta\text{)} \quad \text{SOH}$$

$$\frac{\text{adjacent}}{\text{hypotenuse}} = \text{cosine (cos}\theta\text{)} \quad \text{CAH}$$

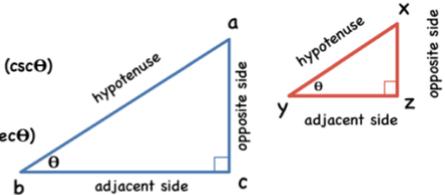
SOH - CAH - TOA

$$\frac{\text{opposite}}{\text{adjacent}} = \text{tangent (tan}\theta\text{)} \quad \text{TOA}$$

$$\frac{\text{opposite}}{\text{hypotenuse}} = \text{cosecant (csc}\theta\text{)}$$

$$\frac{\text{adjacent}}{\text{hypotenuse}} = \text{secant (sec}\theta\text{)}$$

$$\frac{\text{opposite}}{\text{adjacent}} = \text{cotangent (cot}\theta\text{)}$$

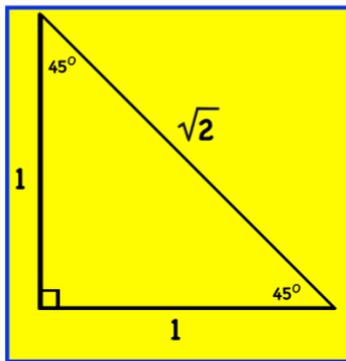
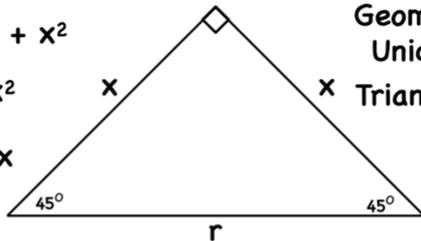


$$r^2 = x^2 + x^2$$

$$r^2 = 2x^2$$

$$r = \sqrt{2} x$$

Geometry Unique Triangles

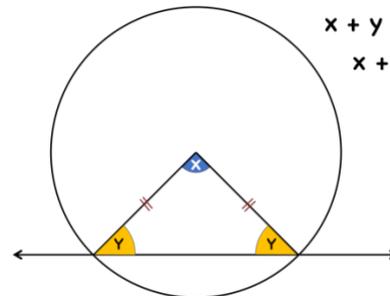


$$x + y + y = 180^\circ$$

$$x + 2y = 180^\circ$$

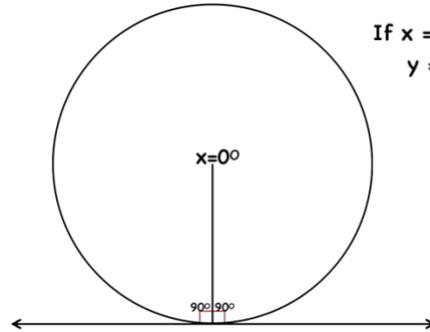
$$y = 180^\circ/2 - x/2$$

$$y = 90^\circ - x/2$$



$$\text{If } x = 0^\circ$$

$$y = 90^\circ$$



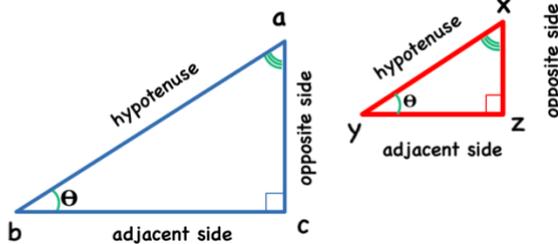
The radius line of a circle meets the tangent line at  $90^\circ$

### Funciones trigonométricas y tangente

$$\frac{ab}{xy} = \frac{ac}{xz}$$

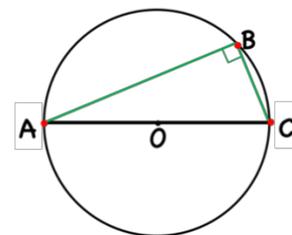
$$\frac{ab}{xy} = \frac{bc}{yz}$$

$$\frac{ac}{xz} = \frac{bc}{yz}$$

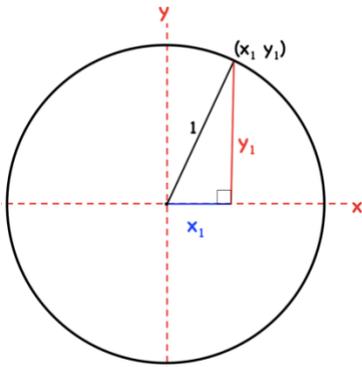


### Thales' Theorem

If A, B, and C are (distinct) points on a circle such that the line segment AC is a diameter of the circle, then the angle  $\angle ABC$  is a right angle. In other words, the triangle  $\triangle ABC$  is a right triangle.

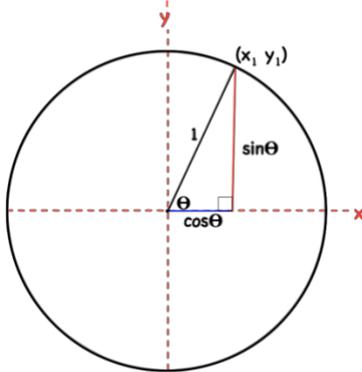


### El círculo unitario



$$\sin \theta = \frac{\text{opposite side}}{\text{hypotenuse}} = \frac{y_1}{1}$$

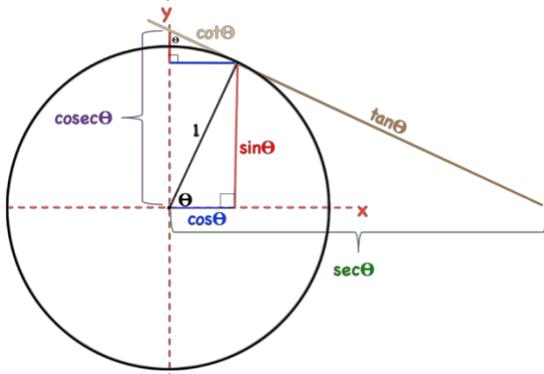
$$\sin \theta = y_1$$



$$\cos \theta = \frac{\text{adjacent side}}{\text{hypotenuse}} = \frac{x_1}{1}$$

$$\cos \theta = x_1$$

$$\tan \theta = \frac{\text{opposite side}}{\text{adjacent side}}$$



### Triángulos únicos

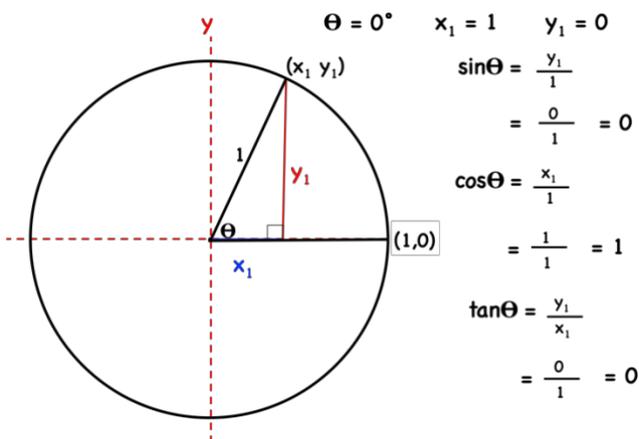
$$\begin{aligned} \text{sine (sin)} \ 30^\circ &= \frac{1}{2} \frac{\text{opposite}}{\text{hypotenuse}} \\ \text{cosine (cos)} \ 30^\circ &= \frac{\sqrt{3}}{2} \frac{\text{adjacent}}{\text{hypotenuse}} \\ \text{tangent (tan)} \ 30^\circ &= \frac{1}{\sqrt{3}} \frac{\text{opposite}}{\text{adjacent}} \\ \text{cosecant (csc)} \ 30^\circ &= \frac{2}{1} \text{reciprocal of sin } \theta \\ \text{secant (sec)} \ 30^\circ &= \frac{2}{\sqrt{3}} \text{reciprocal of cos } \theta \\ \text{cotangent (cot)} \ 30^\circ &= \frac{\sqrt{3}}{1} \text{reciprocal of tan } \theta \end{aligned}$$

$$\begin{aligned} \text{sine (sin)} \ 60^\circ &= \frac{\sqrt{3}}{2} \frac{\text{opposite}}{\text{hypotenuse}} \\ \text{cosine (cos)} \ 60^\circ &= \frac{1}{2} \frac{\text{adjacent}}{\text{hypotenuse}} \\ \text{tangent (tan)} \ 60^\circ &= \frac{\sqrt{3}}{1} \frac{\text{opposite}}{\text{adjacent}} \\ \text{cosecant (csc)} \ 60^\circ &= \frac{2}{\sqrt{3}} \text{reciprocal of sin } \theta \\ \text{secant (sec)} \ 60^\circ &= \frac{2}{1} \text{reciprocal of cos } \theta \\ \text{cotangent (cot)} \ 60^\circ &= \frac{1}{\sqrt{3}} \text{reciprocal of Tan } \theta \end{aligned}$$

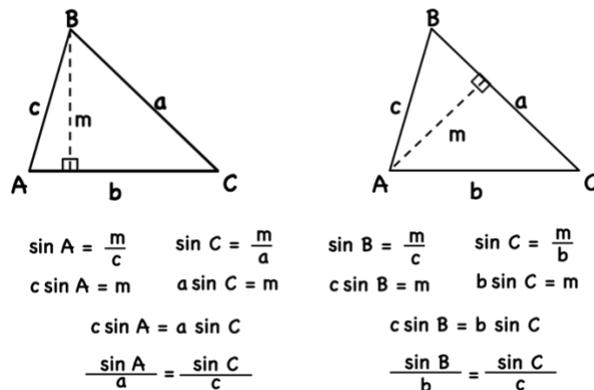
$$\begin{aligned} \text{sine (sin)} \ 45^\circ &= \frac{1}{\sqrt{2}} \frac{\text{opposite}}{\text{hypotenuse}} \\ \text{cosine (cos)} \ 45^\circ &= \frac{1}{\sqrt{2}} \frac{\text{adjacent}}{\text{hypotenuse}} \\ \text{tangent (tan)} \ 45^\circ &= \frac{1}{1} \frac{\text{opposite}}{\text{adjacent}} \\ \text{cosecant (csc)} \ 45^\circ &= \frac{\sqrt{2}}{1} \text{reciprocal of sin } \theta \\ \text{secant (sec)} \ 45^\circ &= \frac{\sqrt{2}}{1} \text{reciprocal of cos } \theta \\ \text{cotangent (cot)} \ 45^\circ &= \frac{1}{1} \text{reciprocal of Tan } \theta \end{aligned}$$

2 <sup>nd</sup> Quadrant	1 <sup>st</sup> Quadrant
$\sin \theta = \text{Positive}$	$\sin \theta = \text{Positive}$
$\cos \theta = \text{Negative}$	$\cos \theta = \text{Positive}$
$\tan \theta = \text{Negative}$	$\tan \theta = \text{Positive}$
3 <sup>rd</sup> Quadrant	4 <sup>th</sup> Quadrant
$\sin \theta = \text{Negative}$	$\sin \theta = \text{Negative}$
$\cos \theta = \text{Negative}$	$\cos \theta = \text{Positive}$
$\tan \theta = \text{Positive}$	$\tan \theta = \text{Negative}$

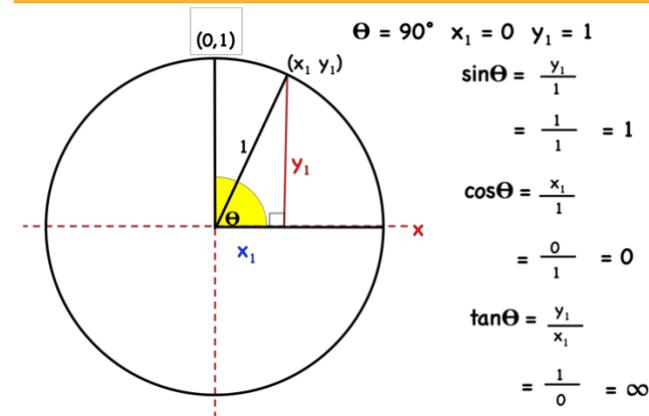
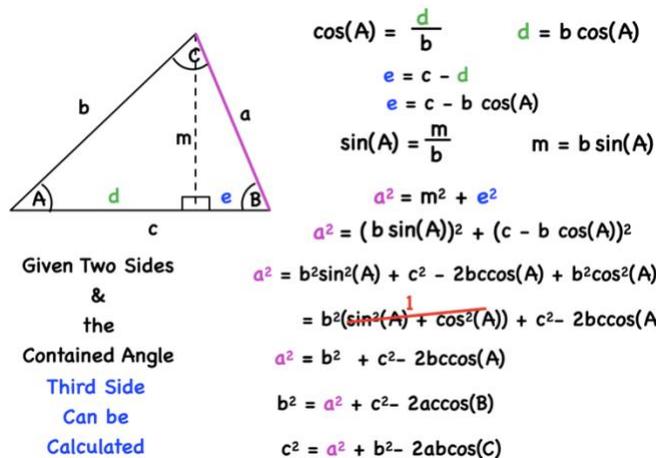
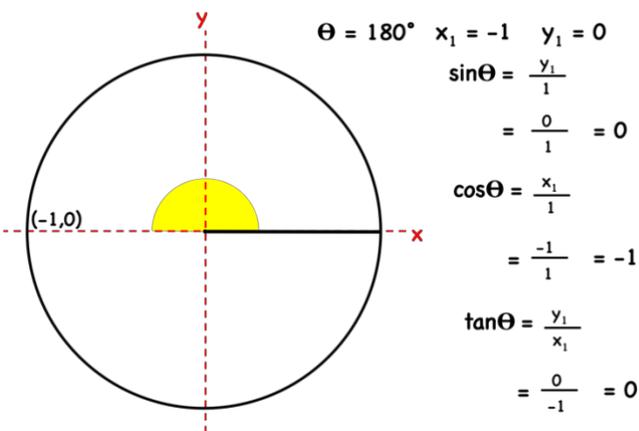
### Ángulos únicos



### La ley de los senos



### La ley de los cosenos



#### Identidades trigonométricas

##### Reciprocal Identities

$$\csc \theta = 1/(\sin \theta)$$

$$\sec \theta = 1/(\cos \theta)$$

$$\cot \theta = 1/(\tan \theta)$$

$$\sin \theta = 1/(\csc \theta)$$

$$\cos \theta = 1/(\sec \theta)$$

$$\tan \theta = 1/(\cot \theta)$$

##### Negative Angle Identities

$$\sin(-\theta) = -\sin \theta$$

$$\cos(-\theta) = \cos \theta$$

$$\tan(-\theta) = -\tan \theta$$

$$\csc(-\theta) = -\csc \theta$$

$$\sec(-\theta) = \sec \theta$$

$$\cot(-\theta) = -\cot \theta$$

##### Quotient Identities

$$\tan \theta = (\sin \theta)/(\cos \theta)$$

$$\cot \theta = (\cos \theta)/(\sin \theta)$$

##### Sum & Difference Formulas

$$\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$$

$$\sin(\alpha - \beta) = \sin \alpha \cos \beta - \cos \alpha \sin \beta$$

$$\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$$

$$\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$$

##### Pythagorean Identities

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$1 - \cos^2 x = \sin^2 x$$

$$1 - \sin^2 x = \cos^2 x$$

Trig Identity for:  $\sin(x - y) = \sin x \cdot \cos y - \cos x \cdot \sin y$

$$\sin(x + y) = \sin x \cdot \cos y + \cos x \cdot \sin y$$

$$\sin(x + (-y)) = \sin x \cdot \cos(-y) + \cos x \cdot \sin(-y)$$

$$\sin(x - y) = \sin x \cdot \cos y - \cos x \cdot \sin y$$

Trig Identity for:  $\cos(x - y) = \cos x \cdot \cos y + \sin x \cdot \sin y$

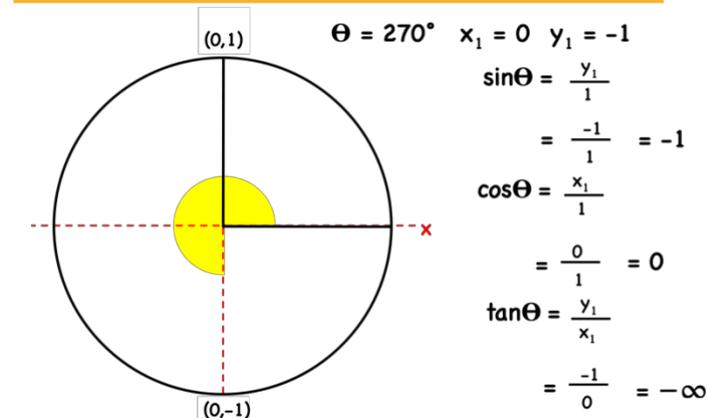
$$\cos(x + y) = \cos x \cdot \cos y - \sin x \cdot \sin y$$

$$\cos(x + (-y)) = \cos x \cdot \cos(-y) - \sin x \cdot \sin(-y)$$

$$\cos(x - y) = \cos x \cdot \cos y + \sin x \cdot \sin y$$

$$\cos(y) = \cos(-y)$$

$$\sin(-y) = -\sin(y)$$



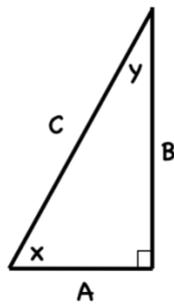
### Fórmulas de producto a suma

$$\begin{aligned} \sin x \cdot \sin y &= (1/2)[\cos(x - y) - \cos(x + y)] \\ \cos x \cdot \cos y &= (1/2)[\cos(x + y) + \cos(x - y)] \\ \sin x \cdot \cos y &= (1/2)[\sin(x + y) + \sin(x - y)] \\ \cos x \cdot \sin y &= (1/2)[\sin(x + y) - \sin(x - y)] \end{aligned}$$

### Fórmulas de suma a producto

$$\begin{aligned} \sin x + \sin y &= 2 \sin \left( \frac{x+y}{2} \right) \cos \left( \frac{x-y}{2} \right) \\ \sin x - \sin y &= 2 \cos \left( \frac{x+y}{2} \right) \sin \left( \frac{x-y}{2} \right) \\ \cos x + \cos y &= 2 \cos \left( \frac{x+y}{2} \right) \cos \left( \frac{x-y}{2} \right) \\ \cos x - \cos y &= -2 \sin \left( \frac{x+y}{2} \right) \sin \left( \frac{x-y}{2} \right) \end{aligned}$$

### Identidades de cofunción



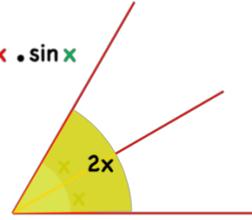
$$y = 90^\circ - x$$

$\cos y = \frac{b}{c} = \sin x$	$\sec y = \frac{c}{b} = \csc x$
$\cos(90^\circ - x) = \sin x$	$\sec(90^\circ - x) = \csc x$
$\sin y = \frac{a}{c} = \cos x$	$\csc y = \frac{c}{a} = \sec x$
$\sin(90^\circ - x) = \cos x$	$\csc(90^\circ - x) = \sec x$
$\tan y = \frac{a}{b} = \cot x$	$\cot y = \frac{b}{a} = \tan x$
$\tan(90^\circ - x) = \cot x$	$\cot(90^\circ - x) = \tan x$

### Fórmulas de doble ángulo

$$\begin{aligned} \sin 2x &= \sin(x + x) = \sin x \cdot \cos x + \cos x \cdot \sin x \\ &= \sin x \cdot \cos x + \cos x \cdot \sin x \\ &= 2 \sin x \cdot \cos x \end{aligned}$$

$$\begin{aligned} \cos 2x &= \cos(x + x) = \cos x \cdot \cos x - \sin x \cdot \sin x \\ &= \cos^2 x - \sin^2 x \\ &= 2 \cos^2 x - 1 \\ &= 1 - 2 \sin^2 x \end{aligned}$$



$$\begin{aligned} \tan 2x &= \frac{\sin 2x}{\cos 2x} = \frac{\sin x \cdot \cos x + \cos x \cdot \sin x}{\cos^2 x - \sin^2 x} \cdot \frac{\cos^2 x}{\cos^2 x} \\ &= \frac{\sin x \cdot \cos x + \cos x \cdot \sin x}{\cos^2 x - \sin^2 x} = \frac{2 \tan x}{1 - \tan^2 x} \end{aligned}$$



# 06) Derivados

## Propiedades límite

$$\lim_{z \rightarrow c} f(x) = L \quad \lim_{z \rightarrow c} g(x) = M$$

$$\lim_{z \rightarrow c} (f(x) + g(x)) = \lim_{z \rightarrow c} \frac{L}{f(x)} + \lim_{z \rightarrow c} \frac{M}{g(x)} = L + M \quad \text{The "Sum" Property}$$

$$\lim_{z \rightarrow c} (f(x) - g(x)) = L - M \quad \text{The "Difference" Property}$$

$$\lim_{z \rightarrow c} (f(x) g(x)) = \lim_{z \rightarrow c} \frac{L}{f(x)} \lim_{z \rightarrow c} \frac{M}{g(x)} = LM \quad \text{The "Multiple" Property}$$

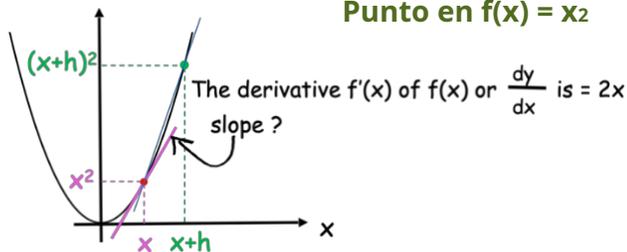
$$\lim_{z \rightarrow c} kf(x) = k \lim_{z \rightarrow c} f(x) = kL \quad \text{The "Constant Multiple" Property}$$

$$\lim_{z \rightarrow c} \frac{f(x)}{g(x)} = \frac{\lim_{z \rightarrow c} \frac{L}{f(x)}}{\lim_{z \rightarrow c} \frac{M}{g(x)}} = \frac{L}{M} \quad \text{The "Quotient" Property}$$

$$\lim_{z \rightarrow c} (f(x))^{R/S} = \left( \lim_{z \rightarrow c} \frac{L}{f(x)} \right)^{R/S} = L^{R/S} \quad \text{The "Exponent" Property}$$

## La pendiente de la tangente

Punto en  $f(x) = x^2$



## Derivados comunes (continuación)

### Trig Functions

$$\frac{d}{dx}(\sin x) = \cos x \quad \frac{d}{dx}(\cos x) = -\sin x$$

$$\frac{d}{dx}(\tan x) = \sec^2 x \quad \frac{d}{dx}(\cot x) = -\csc^2 x$$

$$\frac{d}{dx}(\sec x) = \sec x \tan x \quad \frac{d}{dx}(\csc x) = -\csc x \cot x$$

### Exponential/Logarithm Functions

$$\frac{d}{dx}(a^x) = a^x \ln(a) \quad \frac{d}{dx}(e^x) = e^x$$

$$\frac{d}{dx}(\ln x) = \frac{1}{x} \quad x > 0 \quad \frac{d}{dx}(\ln |x|) = \frac{1}{x} \quad x \neq 0$$

$$\frac{d}{dx}(\log_a x) = \frac{1}{x \ln(a)} \quad x > 0$$

## El teorema de la compresión

$$\lim_{x \rightarrow 0} \frac{1 - \cos x}{x} = 0$$

$$\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

## Derivados comunes

Polynomials (c = constant x = variable)

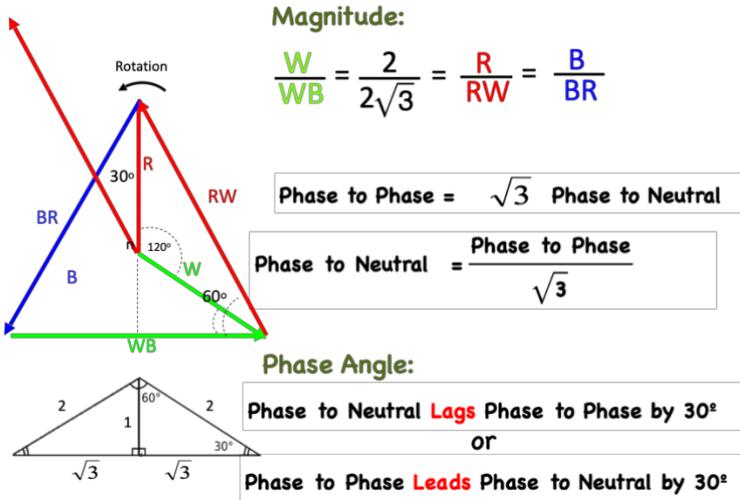
$$\frac{d}{dx}(c) = 0$$

$$\frac{d}{dx}(x) = 1$$

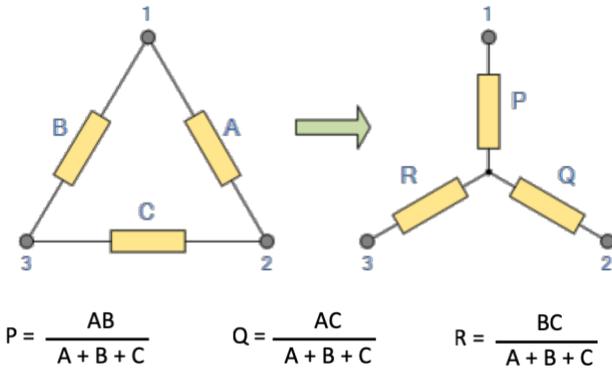
$$\frac{d}{dx}(cx) = c \quad \frac{d}{dx}(x^n) = nx^{n-1} \quad \frac{d}{dx}(cx^n) = ncx^{n-1}$$

# 7) Análisis por unidad

## Relaciones de fase



## Conversiones $\Delta - Y$



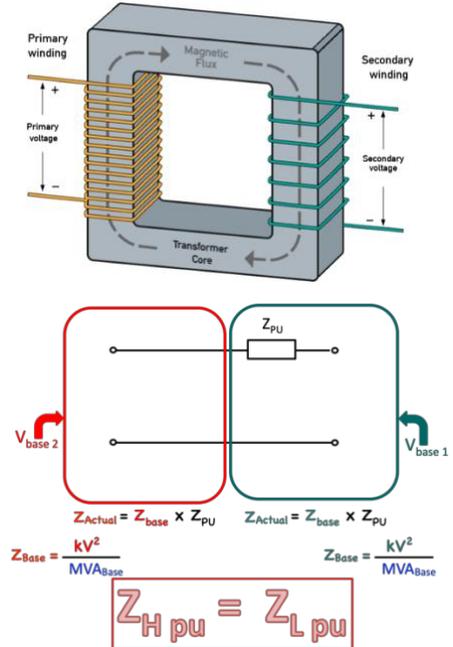
## Normalización

- 1) Specify the **VA or S Base**
- 2) Determine the **Voltage Base**
- 3) Determine **Impedance Bases and Current Bases** from VA Base & each Voltage Bases
- 4) **Per unit** quantities are calculated by dividing the actual value by its equivalent base value
- 5) For each component, it's actual value may be found by multiplying its **per unit** quantity by the base value for that quantity at its connected location

$$\text{Quantity in PU} = \frac{\text{Actual value of Quantity}}{\text{Base value of Quantity}}$$

$$\text{Actual value of Quantity} = \text{Quantity in PU} \times \text{Base value of Quantity}$$

## Transformadores y análisis por unidad



- 1) Specify the **VA Base** **Base Values are Magnitude Only** [Quantity] **VA**

$$S_{\text{base}}^{3\phi} = 3S_{\text{base}}^{1\phi} = P_{\text{base}}^{3\phi} = Q_{\text{base}}^{3\phi} = 3P_{\text{base}}^{1\phi} = 3Q_{\text{base}}^{1\phi}$$

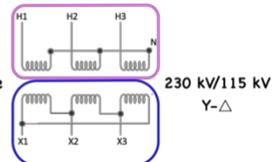
Base values of real power, reactive power, and complex power have the same base value number

- 2) Determine or pick a **Voltage Base** [Quantity] **Volts**

$$V_{\text{base}}^{\text{LN}} = \frac{V_{\text{base}}^{\text{LL}}}{\sqrt{3}}$$

**There is a voltage base for each and every voltage level in the system**

Transformer voltage ratios are given as **line-to-line voltage**



- 3) Determine **Impedance Bases and Current Bases** from VA Base & each Voltage Bases

Current Bases:

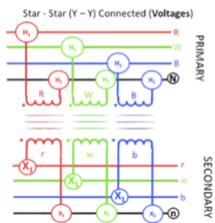
$$I_{\text{base}} = \frac{S_{\text{base}}^{1\phi}}{V_{\text{base}}^{\text{LN}}} = \frac{\frac{S_{\text{base}}^{3\phi}}{3}}{\frac{V_{\text{base}}^{\text{LL}}}{\sqrt{3}}} = \frac{\sqrt{3} S_{\text{base}}^{3\phi}}{3 V_{\text{base}}^{\text{LL}}} = \frac{\sqrt{3} S_{\text{base}}^{3\phi}}{\sqrt{3} \sqrt{3} V_{\text{base}}^{\text{LL}}} = \frac{S_{\text{base}}^{3\phi}}{\sqrt{3} V_{\text{base}}^{\text{LL}}}$$

Impedance Bases:

$$Z_{\text{base}} = \frac{V_{\text{base}}^{\text{LN}}}{I_{\text{base}}} = \frac{(V_{\text{base}}^{\text{LN}})^2}{S_{\text{base}}^{1\phi}} = \frac{\left(\frac{V_{\text{base}}^{\text{LL}}}{\sqrt{3}}\right)^2}{\frac{S_{\text{base}}^{3\phi}}{3}} = \frac{1/3 (V_{\text{base}}^{\text{LL}})^2}{1/3 S_{\text{base}}^{3\phi}} = \frac{(V_{\text{base}}^{\text{LL}})^2}{S_{\text{base}}^{3\phi}}$$

### Conexiones del transformador

Estrella - Estrella (Y - Y)



The Primary Voltage Relationship:

$$RW = \sqrt{3} RN \angle 30^\circ$$

$$V_{LL} = \sqrt{3} V_{LN} \angle 30^\circ$$

The Secondary Voltage Relationship:

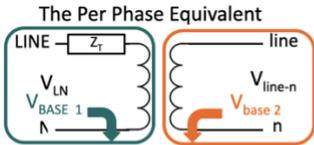
$$rw = \sqrt{3} rn \angle 30^\circ$$

$$V_{line-line} = \sqrt{3} V_{line-n} \angle 30^\circ$$

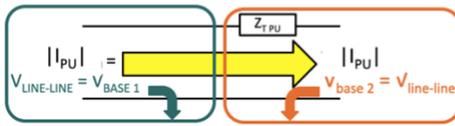
The Turns Ratio of the Transformer:

$$\frac{V_{LN}}{V_{line-n}} = a = \frac{R}{r} = \frac{W}{w} = \frac{B}{b}$$

$$\frac{V_{LL}}{V_{line-line}} = a = \frac{I_{line}}{\text{Prim } I_{LINE}}$$

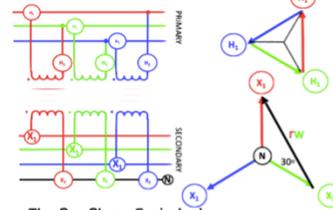


The Per Unit Equivalent



$$Z_H \text{ pu} = Z_L \text{ pu}$$

Delta - Star ( $\Delta$  - Y)



The Secondary Voltage Relationship:

$$rw = \sqrt{3} rn \angle 30^\circ$$

$$V_{line-line} = \sqrt{3} V_{line-n} \angle 30^\circ$$

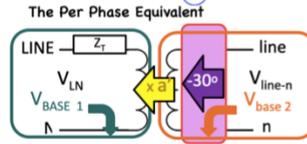
The Per Phase Turns Ratio

$$\frac{V_{LL}}{V_{line-n}} = a$$

$$V_{line-n} = \frac{V_{LL}}{a}$$

$$V_{LL} = \sqrt{3} V_{LN} \angle 30^\circ$$

$$V_{LN} = \frac{V_{LL}}{\sqrt{3}} \angle -30^\circ$$



The Per Unit Equivalent



$$\frac{V_{LN}}{V_{line-n}} = \frac{a}{\sqrt{3}} \angle -30^\circ$$

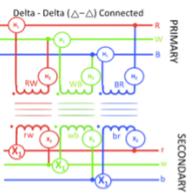
$$a' = \frac{a}{\sqrt{3}}$$

$$V_{LN} = a' V_{line-n} \angle -30^\circ$$

$$V_{LL} = a' V_{line-line} \angle -30^\circ$$

$$I_{Line-prim} = \frac{1}{a'} I_{line-sec} \angle -30^\circ$$

Delta - Delta ( $\Delta$  -  $\Delta$ )



The Turns Ratio of the Transformer:

$$\frac{V_{LL}}{V_{line-line}} = a = \frac{RW}{rw} = \frac{WB}{wb} = \frac{BR}{br}$$

The Per Phase Equivalent



The Per Unit Equivalent



$$V_{LN} = \frac{V_{LL}}{\sqrt{3}} \angle -30^\circ$$

$$V_{line-n} = \frac{V_{line-line}}{\sqrt{3}} \angle -30^\circ$$

$$\frac{V_{LL}}{V_{line-line}} = \frac{V_{LL}}{V_{line-line}} = a$$

$$\frac{I_{line}}{\text{Prim } I_{LINE}} = a$$

$$Z_H \text{ pu} = Z_L \text{ pu}$$

Phase Shift Through a ( $\Delta$ -Y) Voltages Line Currents

Star - Delta (Y- $\Delta$ ) Connected

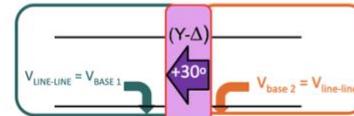
The Secondary Lags Primary by 30°

(Y- $\Delta$ ) Connected Transformer Voltages Line Currents

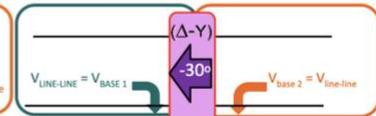
Delta - Star ( $\Delta$  - Y) Connected

The Secondary Leads Primary by 30°

The Per Unit Equivalent



The Per Unit Equivalent



$$|I_{PU}| = |I_{PU}|$$

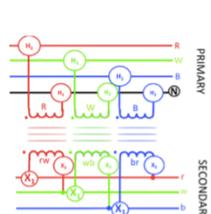
$$|V_{PU}| = |V_{PU}|$$

Cambio de Bases

$$M \xrightarrow{\text{Red Arrow}} N$$

$$Z_{Npu} = Z_{Mpu} \times \frac{S_{NBase}}{S_{MBase}} \times \frac{(V_{MBase})^2}{(V_{NBase})^2}$$

Star - Delta (Y -  $\Delta$ )



The Primary Voltage Relationship:

$$RW = \sqrt{3} RN \angle 30^\circ$$

$$V_{LL} = \sqrt{3} V_{LN} \angle 30^\circ$$

The Per Phase Turns Ratio

$$V_{LN} = a V_{line-line}$$

$$V_{line-line} = \sqrt{3} V_{line-n} \angle 30^\circ$$

$$V_{line-n} = \frac{V_{line-line}}{\sqrt{3}} \angle -30^\circ$$

$$\frac{V_{LN}}{V_{line-n}} = \frac{a V_{line-line} \angle 30^\circ}{\frac{V_{line-line}}{\sqrt{3}} \angle -30^\circ} = a' \sqrt{3}$$

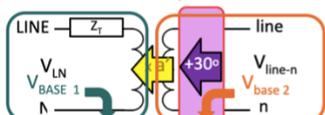
$$\frac{V_{LN}}{V_{line-line}} = \frac{V_{LN}}{V_{line-line}} = a' \angle 30^\circ$$

$$V_{LN} = a' V_{line-n} \angle 30^\circ$$

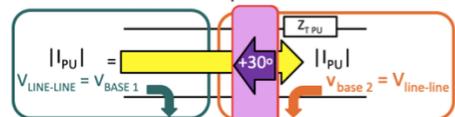
$$V_{LL} = a' V_{line-line} \angle 30^\circ$$

$$I_{Line-prim} = \frac{I_{Line-sec}}{a} \angle +30^\circ$$

The Per Phase Equivalent



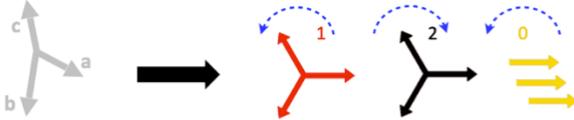
The Per Unit Equivalent



# 8) Componentes simétricos

Fasores asimétricos

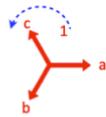
Componentes simétricos



$$\begin{aligned} Z_a &= Z_{0a} + Z_{1a} + Z_{2a} \\ Z_b &= Z_{0b} + Z_{1b} + Z_{2b} \\ Z_c &= Z_{0c} + Z_{1c} + Z_{2c} \end{aligned}$$

$$\begin{aligned} V_a &= V_{0a} + V_{1a} + V_{2a} \\ V_b &= V_{0b} + V_{1b} + V_{2b} \\ V_c &= V_{0c} + V_{1c} + V_{2c} \end{aligned}$$

$$\begin{aligned} I_a &= I_{0a} + I_{1a} + I_{2a} \\ I_b &= I_{0b} + I_{1b} + I_{2b} \\ I_c &= I_{0c} + I_{1c} + I_{2c} \end{aligned}$$

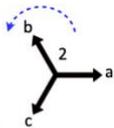


## Positive Sequence

Each phasor has the same magnitude

Each positive sequence phasor quantity is displaced 120° from each another

All phasors rotate counter - clockwise giving a phase sequence of a - b - c

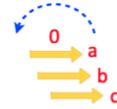


## Negative Sequence

Each phasor has the same magnitude

Each negative sequence quantity is displaced 120° from one another

The negative sequence quantities have a counter clock-wise, phase rotation giving a phase sequence of a-c-b if phasors c & b are swapped



## Zero Sequence

Each zero sequence phasor quantity has the same magnitude

All three phasors have no angular displacement between them, all in phase

The zero sequence phasor quantities have, counter clock-wise, phase rotation

## El operador "a"

Some Properties of "a"-operator

$$a = 1\angle 120^\circ$$

$$a^2 = 1\angle -120^\circ \text{ or } 1\angle +240^\circ \text{ or } a(a)$$

$$a^3 = 1\angle 360^\circ \text{ or } 1 \text{ or } 1\angle 0^\circ$$

$$a^3 - 1 = 0 \text{ or } 0\angle 0^\circ$$

$$a^{-1} = \frac{1}{a} = \frac{1}{1\angle 120^\circ} = 1\angle -120^\circ = a^2$$

$$a^{-2} = \frac{1}{a^2} = a$$

**B-Phase Positive Sequence**  
We replace the Vb sequence term by the Va sequence term shifted by the "a" operator

$$V_{b1} = a^2 V_{a1}$$

**B-Phase Negative Sequence**  
We replace the Vb sequence term by the Va sequence term shifted by the "a" operator

$$V_{b2} = a V_{a2}$$

**B-Phase Zero Sequence**  
We replace the Vb sequence term by the Va sequence without any shift as they are in phase.

$$V_{b0} = V_{a0}$$

**C-Phase Positive Sequence**

We replace the Vc sequence term by the Va sequence term shifted by the "a" operator

$$V_{c1} = aV_{a1}$$

**C-Phase Negative Sequence**

We replace the Vc sequence term by the Va sequence term shifted by the "a<sup>2</sup>" operator

$$V_{c2} = a^2V_{a2}$$

**C-Phase Zero Sequence**

We replace the Vc sequence term by Va sequence without any shift as they are in phase.

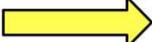
$$V_{c0} = V_{a0}$$

Asymmetrical Phasor Quantities  Symmetrical Components

$$V_{a0} = \frac{1}{3} (V_a + V_b + V_c)$$

$$V_{a1} = \frac{1}{3} (V_a + aV_b + a^2V_c)$$

$$V_{a2} = \frac{1}{3} (V_a + a^2V_b + aV_c)$$

Symmetrical Components  Asymmetrical Phasor Quantities

$$V_a = V_{a0} + V_{a1} + V_{a2}$$

$$V_a = V_{a0} + V_{a1} + V_{a2}$$

$$V_b = V_{b0} + V_{b1} + V_{b2}$$

$$V_b = V_{a0} + a^2V_{a1} + aV_{a2}$$

$$V_c = V_{c0} + V_{c1} + V_{c2}$$

$$V_c = V_{a0} + aV_{a1} + a^2V_{a2}$$

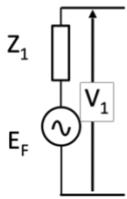
# 9) Análisis de cortocircuito

## Fallas Trifásicas Asimétricas

The system only has positive sequence generators

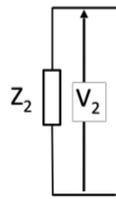
Positive Sequence Network

$$V_1 = E_f - Z_1 \times I_1$$



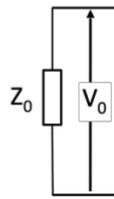
Negative Sequence Network

$$V_2 = -Z_2 \times I_2$$



Zero Sequence Network

$$V_0 = -Z_0 \times I_0$$

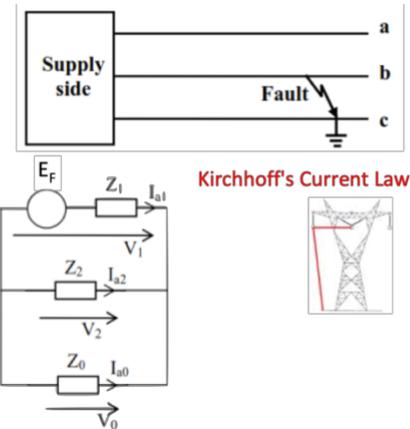


## Fase a Fase a Tierra o Fallas

$$V_b = V_c = 0 \text{ and } I_a = 0$$

$$I_{a0} + I_{a1} + I_{a2} = 0 = I_a$$

$$V_{a0} = V_{a1} = V_{a2}$$



Kirchhoff's Current Law

## Fallas de línea única a tierra

$$I_f = \frac{3E_f}{Z_1 + Z_2 + Z_0}$$

$$V_{a0} + V_{a1} + V_{a2} = 0$$

$$I_{a0} = I_{a1} = I_{a2}$$

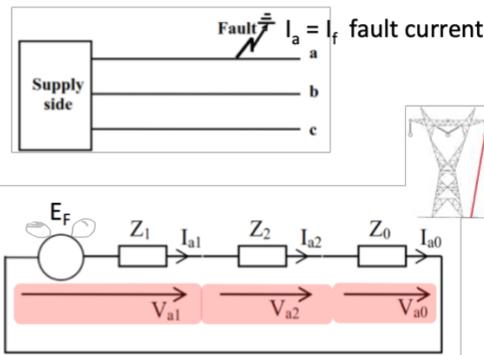
$$I_f = I_a = I_{a0} + I_{a1} + I_{a2}$$

$$I_{a0} = I_{a1} = I_{a2} = \frac{1}{3} I_a$$

$$I_f = I_a = 3I_{a0}$$

$$I_f = I_a = 3I_{a1}$$

$$I_f = I_a = 3I_{a2}$$



## Fase a tierra con impedancia

$$I_a = \frac{3E_f}{Z_1 + Z_2 + Z_0 + 3Z_f} = I_f$$

$$I_{a0} = I_{a1} = I_{a2}$$

$$I_f = I_a = I_{a0} + I_{a1} + I_{a2}$$

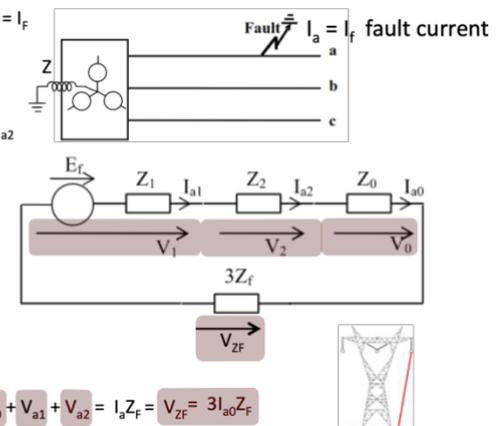
$$I_{a0} = I_{a1} = I_{a2} = \frac{1}{3} I_a$$

$$I_f = I_a = 3I_{a0}$$

$$I_f = I_a = 3I_{a1}$$

$$I_f = I_a = 3I_{a2}$$

$$V_{a0} + V_{a1} + V_{a2} = I_a Z_f = V_{ZF} = 3I_{a0} Z_f$$



## Fallas fase a fase

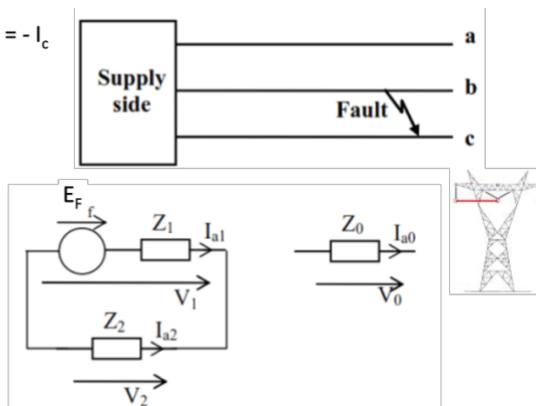
$$V_b = V_c, I_a = 0, I_b = -I_c$$

$$I_{a0} = 0$$

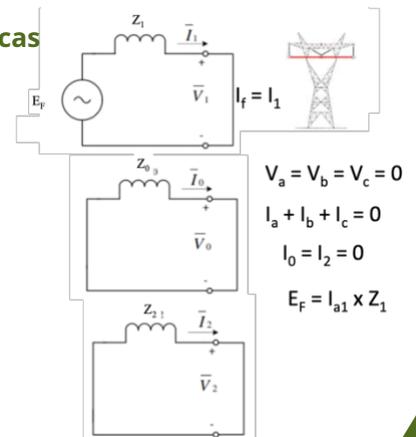
$$I_{a1} = -I_{a2}$$

$$I_{a1} + I_{a2} = 0$$

$$V_{a1} = V_{a2}$$



## Fallas trifásicas



$$V_a = V_b = V_c = 0$$

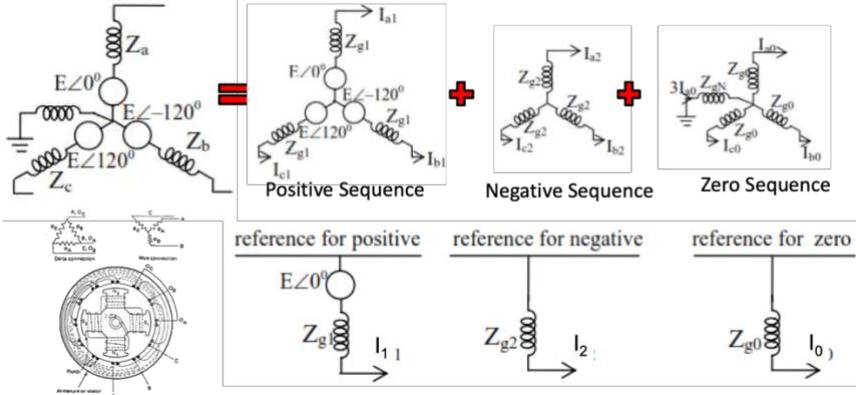
$$I_a + I_b + I_c = 0$$

$$I_0 = I_2 = 0$$

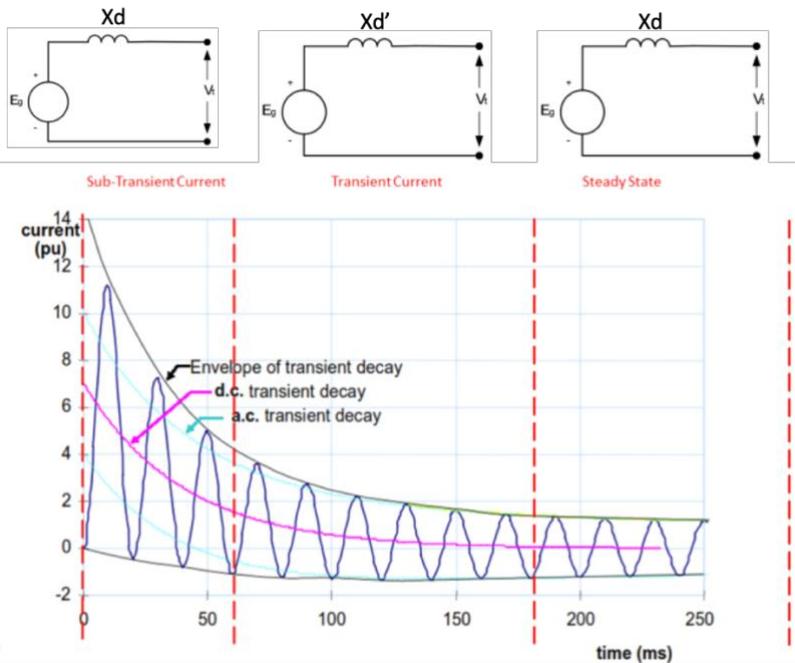
$$E_f = I_{a1} \times Z_1$$

## Diagramas unifilares para red Componentes

### El generador



### Modelado: Generadores Síncronos



### Modelado: Transformadores

#### Single-Line Diagrams for Network Components

$U_p$  = primary side terminal voltage

$U_s$  = secondary side terminal voltage

$R_{w,p}$  = primary winding resistance

$X_{l,p}$  = primary winding leakage reactance

$R_{w,s}$  = secondary winding resistance

$X_{l,s}$  = secondary winding leakage reactance

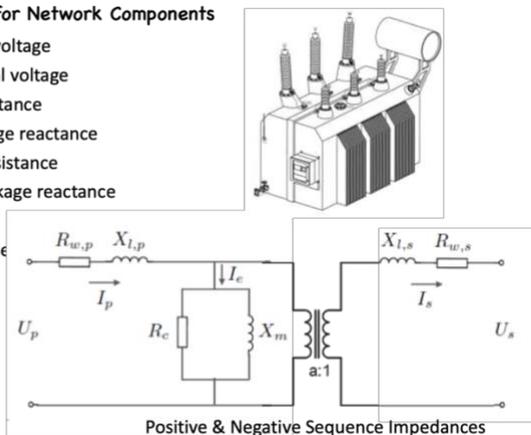
$X_m$  = magnetising reactance

$R_c$  = eddy current / core loss

$I_p$  = primary current

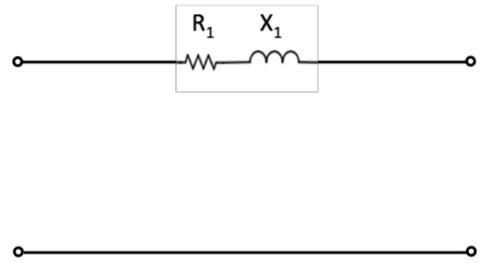
$I_s$  = secondary current

$I_e$  = magnetising current

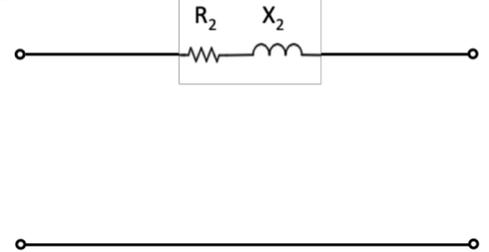


### Modelado: Transformadores (continuación)

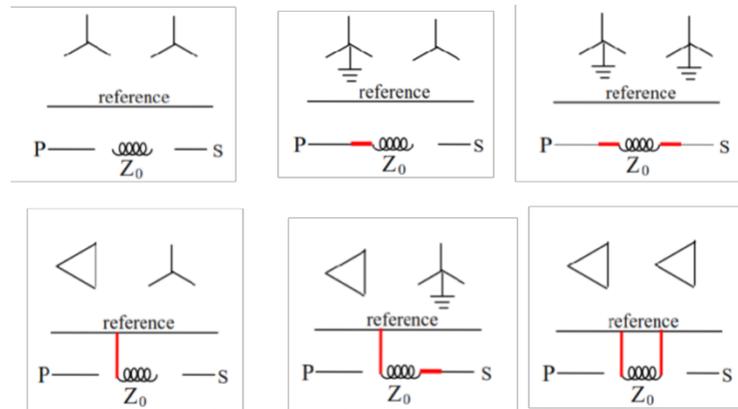
#### Positive Sequence Impedance in Per Unit Values



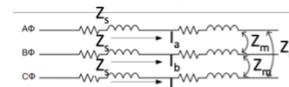
#### Negative Sequence Impedance in Per Unit Values



### Secuencia cero a través de un transformador.



### Modelado: Líneas de Transmisión



$$V_a = Z_1 \times I_a + Z_m \times I_b + Z_m \times I_c$$

$$(I_b + I_c) = -I_a$$

$$V_a = (Z_1 - Z_m) \times I_a$$

$$Z_a = \frac{V_a}{I_a} = (Z_1 - Z_m)$$

$$I_{a0} = I_{b0} = I_{c0}$$

$$V_{a0} = Z_1 \times I_{a0} + Z_m \times I_{b0} + Z_m \times I_{c0}$$

$$= Z_1 \times I_{a0} + Z_m \times I_{a0} + Z_m \times I_{a0}$$

$$= Z_1 \times I_{a0} + (Z_m + Z_m) \times I_{a0}$$

$$= (Z_1 + 2Z_m) \times I_{a0}$$

$$Z_{a0} = \frac{V_{a0}}{I_{a0}} = (Z_1 + 2Z_m)$$

Single-Line Diagram for Network Components

$$Z_{a1} = (Z_1 - Z_m) \text{ Positive Sequence Impedance}$$

$$Z_{a2} = (Z_1 - Z_m) \text{ Negative Sequence Impedance}$$

$$Z_{a0} = (Z_1 + 2Z_m) \text{ Zero Sequence Impedance}$$

# 10) Protección y Control

## Aparatos eléctricos

- 1 – Elemento maestro
- 2 – Retardo de tiempo de arranque o cierre del relé
- 3 – Relé de verificación o enclavamiento
- 4 – Contactor maestro
- 5 – Parar
- 6 – Disyuntor de arranque
- 7 – Relé de velocidad de cambio
- 8 – Dispositivo de desconexión de alimentación de control
- 9 – Dispositivo de inversión
- 10 – Interruptor de secuencia de unidades
- 11 – Dispositivo multifunción
- 12 – Dispositivo de exceso de velocidad
- 13 – Dispositivo de velocidad síncrona
- 14 – Dispositivo de velocidad insuficiente
- 15 – Velocidad – o Frecuencia, Dispositivo coincidente
- 16 – Dispositivo de comunicación de datos
- 17 – Interruptor de derivación o descarga
- 18 – Dispositivo de aceleración o desaceleración
- 19 – Contratista de transición de arranque a funcionamiento
- 20 – Válvula operada eléctricamente
- 21 – Relevo de distancia
- 22 – Disyuntor del ecualizador
- 23 – Dispositivo de control de temperatura
- 24 – Relé de voltios por hercio
- 25 – Dispositivo de sincronización o verificación de sincronización
- 26 – Dispositivo térmico del aparato
- 27 – Relé de subtensión
- 27s - Relé de subtensión CC
- 28 – Detector de llama
- 29 – Contactor o interruptor de aislamiento
- 30 – Relé anunciador
- 31 – Excitación separada
- 32 – Relé de potencia direccional o relé de potencia inversa
- 33 – Interruptor de posición
- 34 – Dispositivo de secuencia maestra
- 35 – Dispositivo de cortocircuito con operación de escobillas o anillo colector
- 36 – Dispositivos de polaridad o voltaje polarizador
- 37 – Relé de baja corriente o baja potencia
- 38 – Dispositivo protector de rodamientos
- 39 – Monitor de condición mecánica
- 40 – Relé de campo (sobreexcitación/subexcitación)
- 41 – Disyuntor de campo
- 42 – Disyuntor en funcionamiento
- 43 – Dispositivo selector o de transferencia manual
- 44 – Relé de arranque de secuencia de unidad
- 45 – Relé de sobretensión CC
- 46 – Relé de corriente de fase inversa o equilibrio de fases
- 47 – Relé de voltaje de secuencia de fases o equilibrio de fases
- 48 – Relé de secuencia incompleta
- 49 – Máquina o Transformador, Relé Térmico-OLR
- 50 – Relé de Sobrecorriente Instantánea
- 50G - Relé instantáneo de sobrecorriente de tierra (método CT neutro)
- 50N - Relé instantáneo de sobrecorriente de tierra (método residual)
- 50BF - Falla del disyuntor
- 51 – Relé de sobrecorriente de tiempo inverso de CA
- 51G - Relé de sobrecorriente de tierra de tiempo inverso de CA (método CT neutro)
- 51N - Relé de sobrecorriente de tierra de tiempo inverso de CA (método residual)
- 52 - Disyuntor de CA
- 52a - Posición del disyuntor de CA (contacto abierto cuando el disyuntor está abierto)
- 52b - Posición del disyuntor de CA (contacto cerrado cuando el disyuntor está abierto)
- 53 - Relé del excitador o del generador de CC
- 54 – Dispositivo de engranaje de giro
- 55 – Relé de factor de potencia
- 56 – Relé de aplicación de campo
- 57 – Dispositivo de cortocircuito o puesta a tierra
- 58 – Relé de falla de rectificación
- 59 – Relé de sobretensión
- 60 – Relé de equilibrio de voltaje o corriente
- 61 – Interruptor o sensor de densidad
- 62 – Relé Temporizado de Parada o Apertura

**Números ANSI** Números de función del dispositivo del sistema de energía eléctrica estándar IEEE según. según IEEE C.37.2-1991

**Dispositivos eléctricos (continuación)**

- 63 - Interruptor de presión 64 - Relé detector de tierra 64R - Falla a tierra restringida 64S - Falla a tierra del estator 65 - Gobernador
- 66 - Dispositivo de muesca o jogging 67 - Relé de sobrecorriente direccional de CA 68 - Relé de bloqueo
- 69 - Dispositivo de control permisivo 70 - Reóstato
- 71 - Interruptor de nivel de líquido 72 - Disyuntor de CC 73 - Contactor de resistencia de carga 74 - Relé de alarma
- 75 - Mecanismo de cambio de posición 76 - Relé de sobrecorriente CC
- 77 - Dispositivo de Telemedición
- 78 - Relé de medición de ángulo de fase o relé "fuera de paso" 79 - Relé de reconexión de CA (reconexión automática)
- 80 - Interruptor de flujo 81 - Relé de frecuencia 82 - Relé de reconexión de CC
- 83 - Control Selectivo Automático o Relé de Transferencia 84 - Mecanismo de Operación
- 85 - Comunicaciones, portadora o relé de cable piloto
- 86 - Relé de bloqueo/disparo maestro 87 - Relé de protección diferencial
- 88 - Motor auxiliar o motor generador 89 - Interruptor de línea
- 90 - Dispositivo de regulación 91 - Relé direccional de voltaje
- 92 - Relé direccional de voltaje y potencia 93 - Contactor de cambio de campo

- 94 - Relé de disparo o disparo libre (relé de supervisión del circuito de disparo) 95 - Para aplicaciones específicas donde otros números no son adecuados 96 - Relé de bloqueo de disparo de barra colectora
- 97 - Para aplicaciones específicas donde otros números no son adecuados 98 - Para aplicaciones específicas donde otros números no son adecuados 99 - Para aplicaciones específicas donde otros números no son adecuados 150 - Indicador de falla a tierra AFD - Detector de arco eléctrico CLK - Fuente de reloj o temporización DDR - Registrador de perturbaciones dinámicas DFR - Registrador de fallas digital

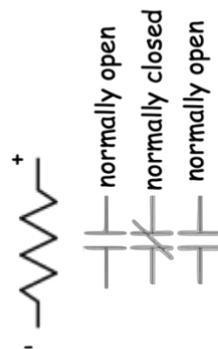
- DME - Equipo de monitoreo de perturbaciones ENV - Datos ambientales HIZ - Detector de fallas de alta impedancia HMI - Interfaz hombre-máquina HST - Historiador LGC - Lógica de esquema MET - Medición de subestaciones PDC - Concentrador de datos fasoriales PMU - Unidad de medición fasorial PQM - Monitor de calidad de energía RIO - Dispositivo remoto de entrada/salida RTU - Unidad Terminal Remota/Concentrador de Datos SER - Registrador de Secuencia de Eventos TCM - Monitor de circuito de disparo LRSS - INTERRUPTOR SELECTOR LOCAL/REMOTO SOTF - Encendido hasta falla

**Números ANSI Números de función del dispositivo del sistema de energía eléctrica estándar IEEE según IEEE C.37.2-1991**

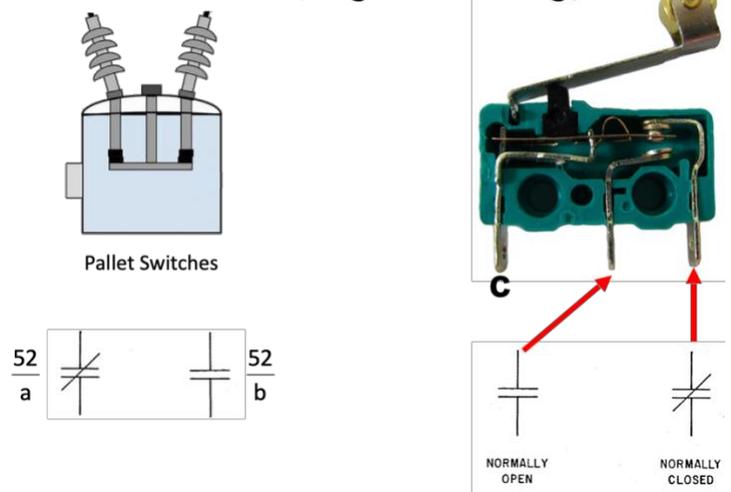
**Relay Identification**

Battery on coil (B)  
 Device Function (Trip)  
 Remote Trip  
 Receive  
 Timer

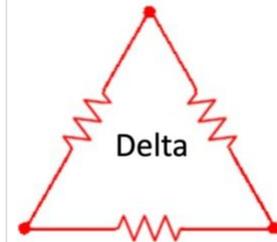
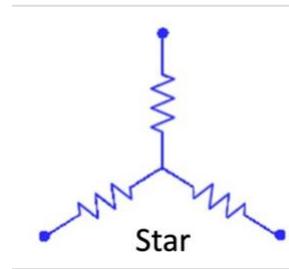
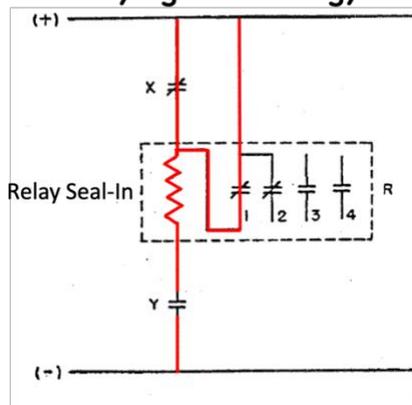
**B94 RT rt**  
**RRKN1 - 307**  
 0.05 - 0.5  
 Sec. p.u.  
 110 - 125V



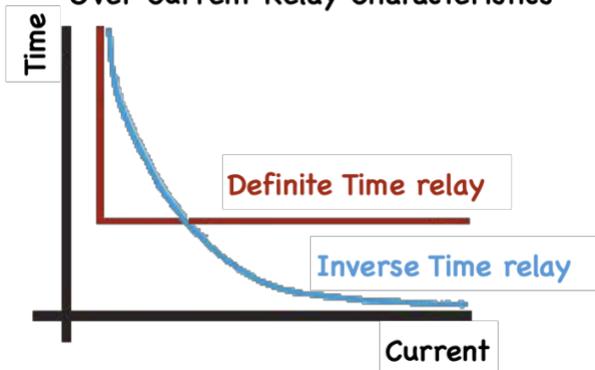
**Relaying Terminology**



### Relaying Terminology



### Over Current Relay Characteristics



### Esquemas de relés de protección

Differential Protection: Generators, Transformers, Lines & Buses

Pilot Wire Protection: Short Lines

Impedance Protection: Long Lines

- (a) Two zone distance protection
- (b) Phase comparison protection
- (c) Directional comparison protection
- (d) Direct under-reaching protection
- (e) Permissive overreaching protection

Co-ordinated Over-Current Protection: Feeders

Breaker failure protection

CT and breaker flash protection

Remote Trip: Short Distances

Transfer Trip: Long Distances

### Liquid Cooled Transformers

**First letter:** Internal cooling medium in contact with the windings

- O** mineral oil or synthetic insulating liquid with fire point < 300°C
- K** insulating liquid with fire point > 300°C
- L** insulating liquid with no measurable fire point

**Second letter:** Circulation mechanism for internal cooling medium:

- N** natural convection flow through cooling equipment and windings
- F** forced circulation through cooling equipment (cooling pumps)
- D** forced circulation through cooling equipment, directed from the cooling equipment into at least the main windings

**Third letter:** External cooling medium

- A** air
- W** water

**Fourth letter:** Circulation mechanism for external cooling medium

- N** natural convection
- F** forced circulation (fans, pumps)

**ONAF** Cooling of Transformer "Oil Natural Air Forced"

**ONAN** Cooling of Transformer "Oil Natural Air Natural"

**OFAF** Cooling of Transformer "Oil Forced Air Forced"

**OFWF** Cooling of Transformer "Oil Forced Water Forced"

### Tipos de E

Phase to Ground (short cct)



Phase to Phase (short cct)



Phase to Phase to Grd (short cct)



Three Phase (short cct)



High Resistance Phase to Grd (open cct)



Open Phase (open cct)



### Esquemas de relés de protección

Differential Protection: Generators, Transformers, Lines & Buses

Pilot Wire Protection: Short Lines

Impedance Protection: Long Lines

- (a) Two zone distance protection
- (b) Phase comparison protection
- (c) Directional comparison protection
- (d) Direct under-reaching protection
- (e) Permissive overreaching protection

Co-ordinated Over-Current Protection: Feeders

Breaker failure protection

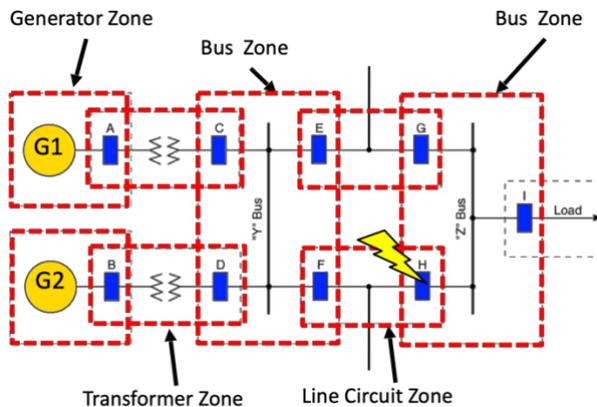
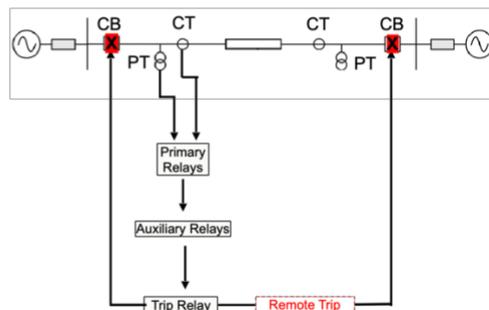
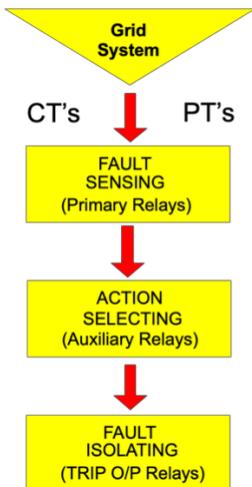
CT and breaker flash protection

Remote Trip: Short Distances

Transfer Trip: Long Distances

### Elementos de una protección

Esquema de retransmisión



### Estructura básica del sistema eléctrico

**Color Key:**  
 Blue: Transmission  
 Green: Distribution  
 Black: Generation

**Transmission**

Transmission Lines  
735, 500, 345, 230, and 138 kV

Transmission Customer  
138kV or 230kV

**Distribution**

Substation Step-Down Transformer

Subtransmission Customer  
28kV and 69kV

Primary Customer  
13kV and 4 kV

Secondary Customer  
120V and 240V

12.5 14.4 27.6 kV

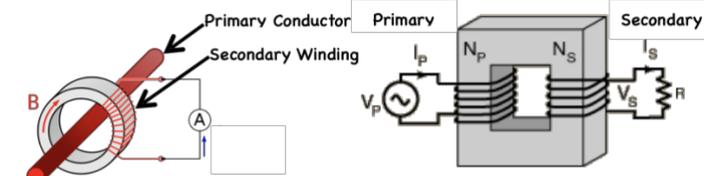
Function	Typical Voltages (Phase to Phase - kV)							
Utilization	120/240	.440	.600	2.4	4.16	14.4		
Distribution	2.4	4.16	8.32	12.5	14.4	27.6		
Sub-Transmission	14.4	27.6	44	115				
Transmission	115	230	500	735				
Transformation	Transformation Between voltage levels							
System Machines (synchronous condensers frequency changers, etc.)	12.5 - 14.4							
Generation	2.4	4.16	13.8 - 24.0					

### Transformadores de instrumentos

Two Types

Current Transformer

Potential Transformer



$$I_p N_p = I_s N_s$$

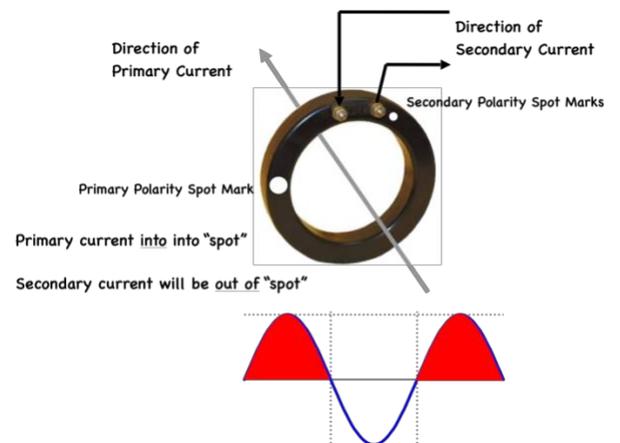
$$I_s = I_p \frac{N_p}{N_s} \quad \text{If } N_p \text{ is } = 1$$

$$I_s = \frac{I_p}{N_s}$$

$$\frac{V_s}{V_p} = \frac{N_s}{N_p}$$

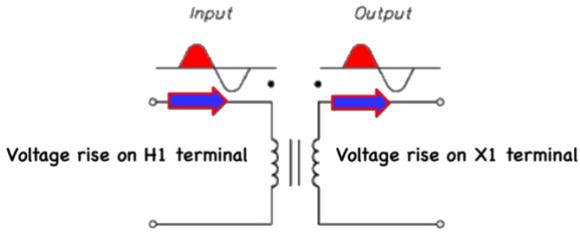
### Polaridad

#### Current Transformers



Polaridad (continuación)

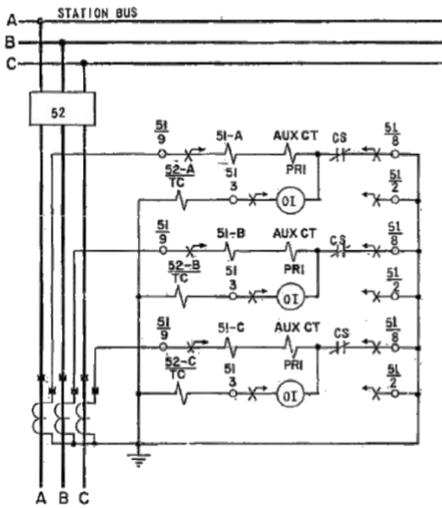
Potential Transformers



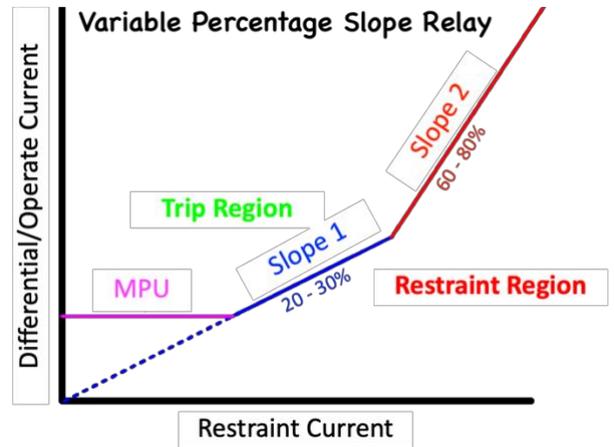
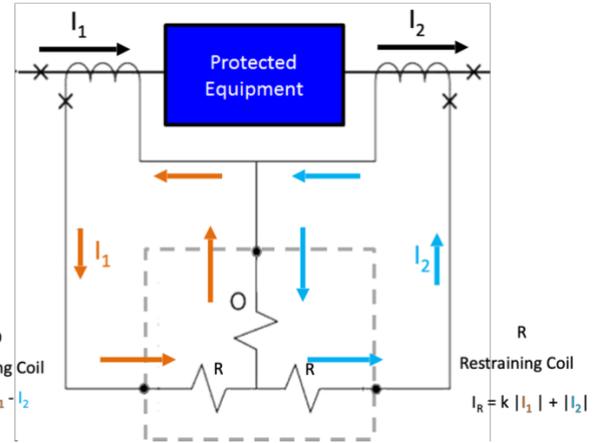
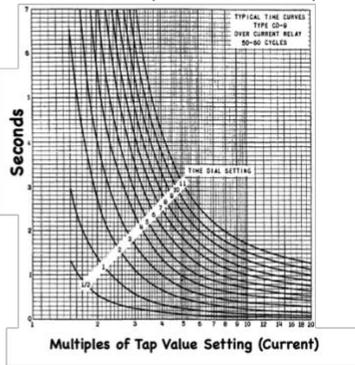
Tipos de disyuntores de alta tensión

- Oil Breakers
- Minimum Oil Breakers
- Vacuum Breakers
- SF6 Breakers
- Air Blast Breakers

Westinghouse (ABB)



- CO-2 Short Time Relay
- CO-5 Long Time Relay
- CO-6 Definite Minimum Time Relay
- CO-7 Moderately Inverse Time Relay
- CO-8 Inverse Time Relay
- CO-9 Very Inverse Time Relay
- CO-11 Extremely Inverse Time Relay

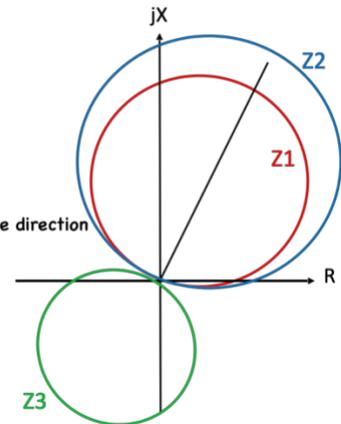


Retransmisión de impedancia

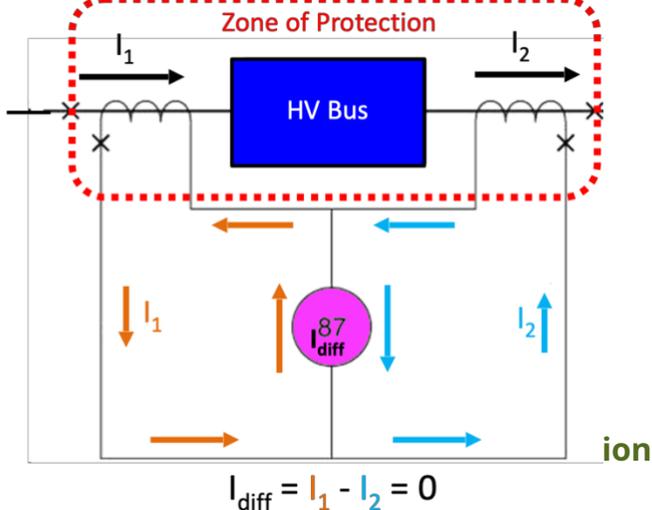
The Mho Type Distance Relay

Several elements can be set differently:

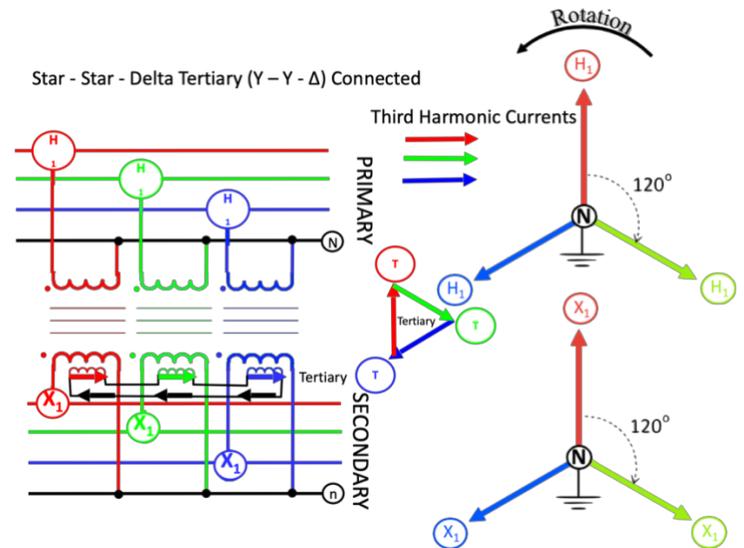
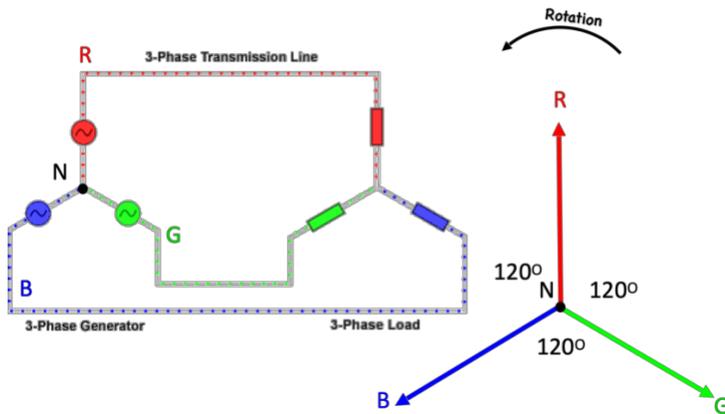
- Z1 75% - 80% of the line impedance
- Z2 120% of the line impedance
- Z3 20%-30% of the line impedance reverse direction use in Directional Comparison Protection



Protección diferencial

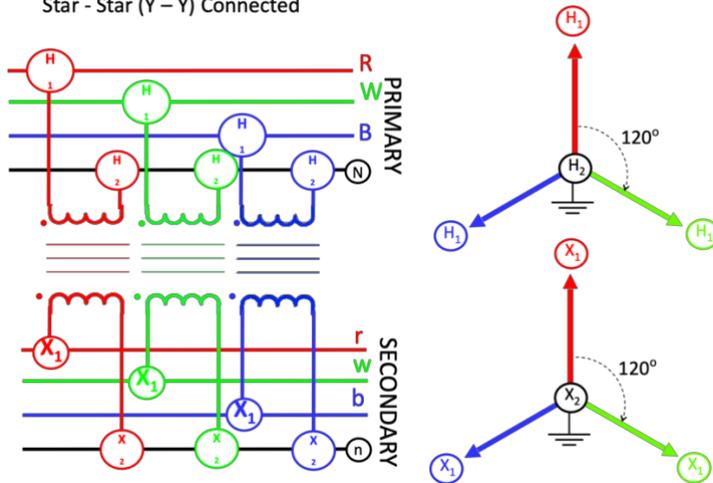


# 11) Transformadores Trifásicos

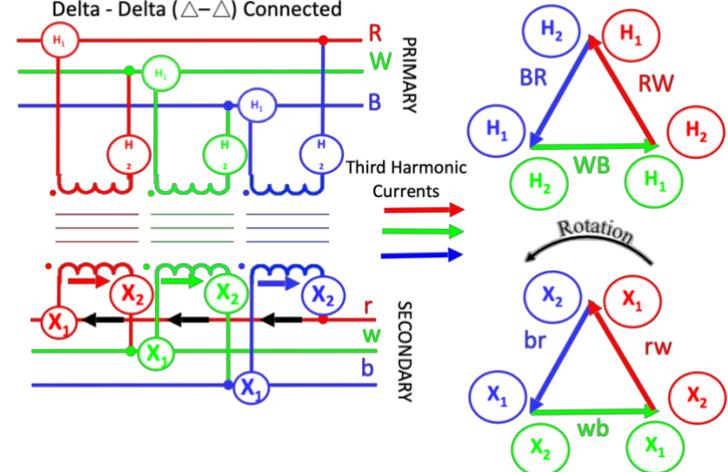


## Conexiones del transformador

Star - Star (Y - Y) Connected



Delta - Delta (Δ-Δ) Connected



## The 3rd Harmonic

Fundamental Frequency is  $\sin(\omega t)$

3rd Harmonic is Frequency is  $\sin 3x(\omega t)$

$$A = A \sin(\omega t + 0^\circ)$$

$$B = B \sin(\omega t + 120^\circ)$$

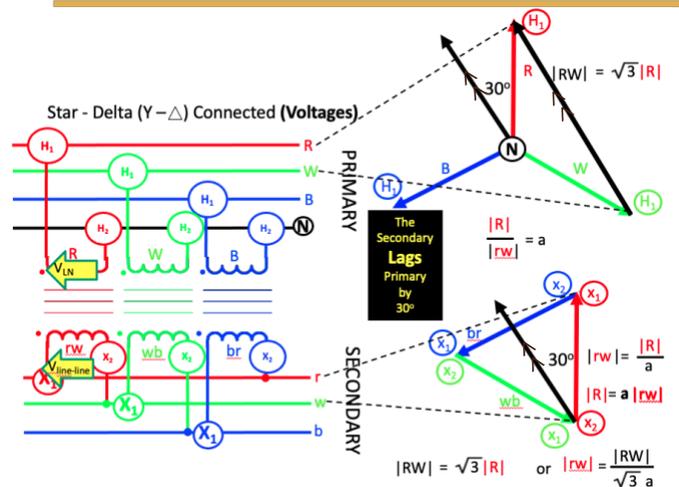
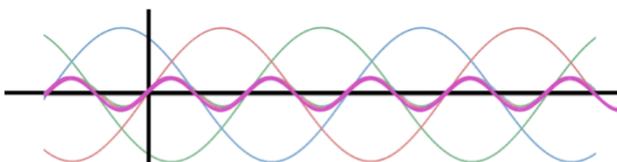
$$W = W \sin(\omega t - 120^\circ)$$

$$A_{(3H)} = A_{(3H)} \sin 3(\omega t + 0^\circ) = A_{(3H)} \sin(3\omega t + 3 \times 0^\circ) = A_{(3H)} \sin(3\omega t)$$

$$B_{(3H)} = B_{(3H)} \sin 3(\omega t + 120^\circ) = B_{(3H)} \sin(3\omega t + 360^\circ) = B_{(3H)} \sin(3\omega t)$$

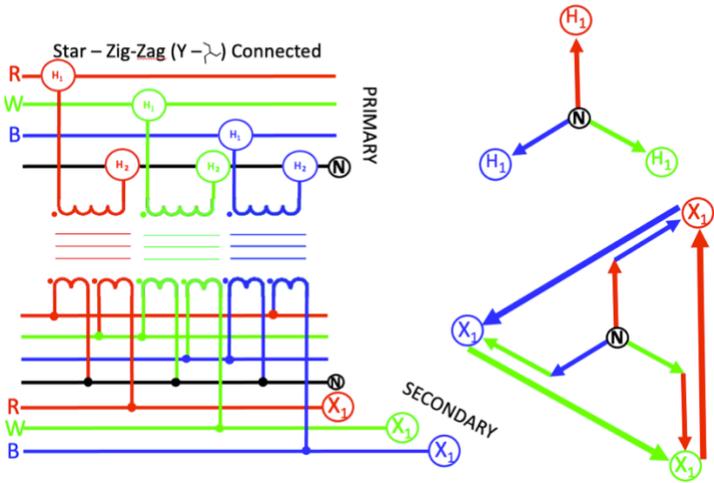
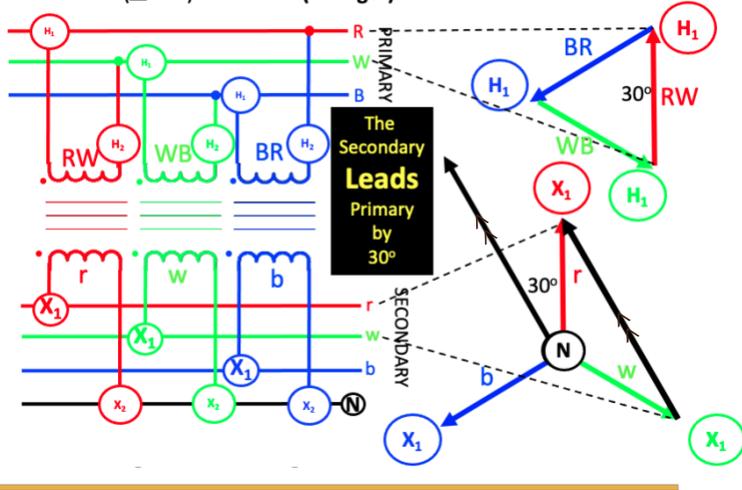
$$W_{(3H)} = W_{(3H)} \sin 3(\omega t - 120^\circ) = W_{(3H)} \sin(3\omega t - 360^\circ) = W_{(3H)} \sin(3\omega t)$$

In Phase



Conexiones del transformador (continuación)

Delta - Y ( $\Delta$  - Y) Connected (Voltages)



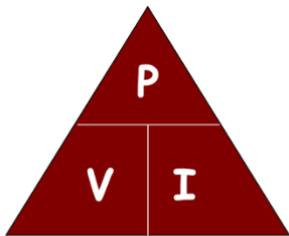
# 12) Medición

## Poder y energía

Work done or electric energy (E) is the movement of charge (Q) caused by EMF

$E = V \times Q$   
 P is the rate at which electric energy (E) is transferred by an electric circuit  
 $P = \frac{E}{t} = \frac{VQ}{t} = V \times Q/t = V \times I$   
 one electron =  $1/Q = 1.6 \times 10^{-19}$  coulombs  
 1 coulomb = 6,250,000,000,000,000 electrons  
 1 amp = 1 coulomb passing by in 1 second of time

Electrical power is measured in **Watts** (symbol: **W**)



$$P = V I \text{ watts}$$

$$V = \frac{P}{I} \text{ volts}$$

$$I = \frac{P}{V} \text{ amps}$$

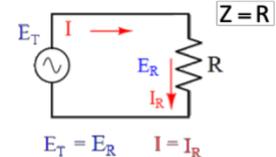
## Energía eléctrica

**Energy = Power x Time**  
**Joule (J)**  
**Watt hour**  
**Watt Sec**  
**kilowatt hour**

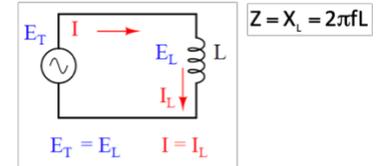
SI multiples for watt hour (W-h)

Submultiples			Multiples		
Value	Symbol	Name	Value	Symbol	Name
$10^{-3}$	mW-h	milliwatt hour	$10^3$	kW-h	kilowatt hour
$10^{-6}$	$\mu$ W-h	microwatt hour	$10^6$	MW-h	megawatt hour
			$10^9$	GW-h	gigawatt hour
			$10^{12}$	TW-h	terawatt hour
			$10^{15}$	PW-h	petawatt hour

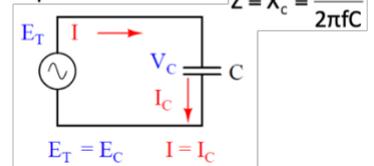
AC Resistor Circuits



AC Inductor Circuits



AC Capacitive Circuits



$$V_{rms} = \frac{V_{Peak}}{\sqrt{2}} = 0.707 V_{Peak}$$

$$I_{AC} = I_{RMS} = 0.707 I_{Peak}$$

$$\text{Average } P_{DC} = \text{Average } P_{AC}$$

$$P_{Avg} = I_{rms}^2 R \quad \text{watts}_{avg}$$

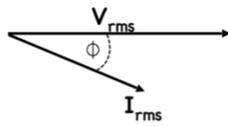
$$P_{Avg} = \frac{V_{RMS}^2}{R} \quad \text{watts}_{Avg}$$

$$P_{Avg} = V_{rms} I_{rms} \quad \text{watts}_{avg}$$

$$V_{rms} = \frac{P_{Avg}}{I_{rms}} \quad \text{volts}_{RMS}$$

$$I_{rms} = \frac{P_{Avg}}{V_{rms}} \quad \text{amps}_{RMS}$$

### Energia electrica



$$P_{avg} = \frac{V_m I_m}{2} \cos(\phi)$$

$$P_{avg} = \frac{V_m}{\sqrt{2}} \times \frac{I_m}{\sqrt{2}} \cos(\phi)$$

but  $V_{rms} = \frac{V_m}{\sqrt{2}}$  And

then  $P_{avg} = V_{rms} \times I_{rms} \cos(\phi)$

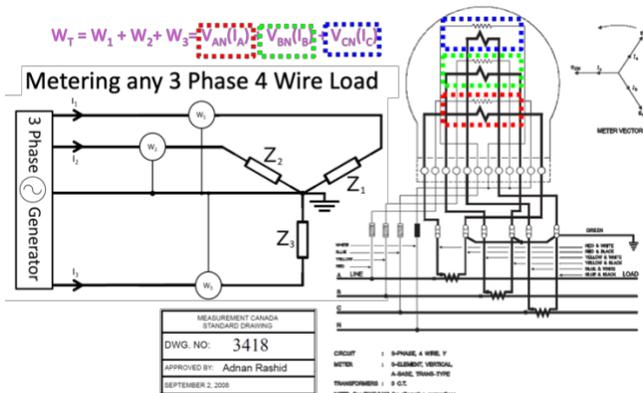
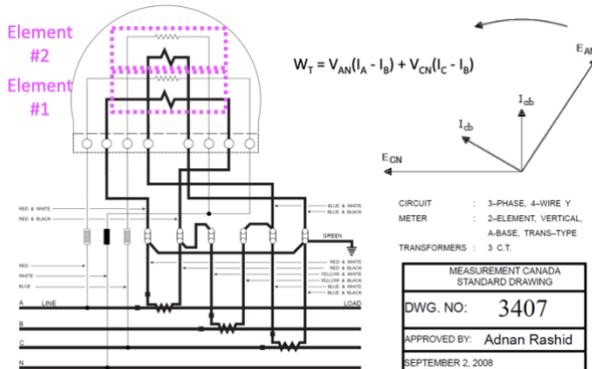
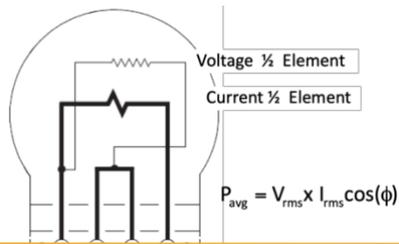
$$P_{avg} = \frac{V_m I_m}{2} \cos(\phi)$$

$$P_{avg} = V_{rms} \times I_{rms} \cos(\phi)$$

$$Q_{avg} = V_{rms} \times I_{rms} \sin(\phi) \text{ VARs}$$

Apparent Power =  $V_{rms} \times I_{rms} \text{ VA}$

### Contadores de vatios hora



### Especificaciones del sitio WEB de Industry Canada para medidores de electricidad

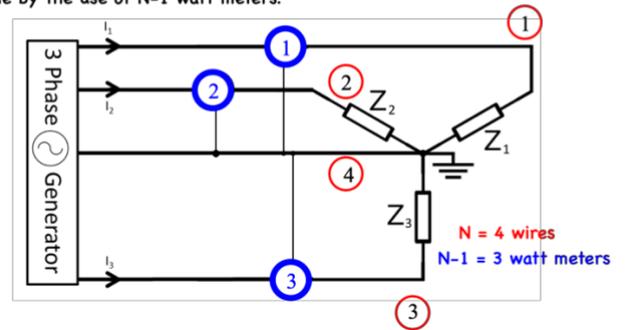


Industry Canada's WEB Site has the Specifications for the Installation and Use of Electricity Meters along with Measurement Canada Standard Drawings for Electricity Metering Installations including Colour Coded Connections

<http://www.ic.gc.ca/eic/site/mc-mc.nsf/eng/lm04068.html#AppendixII>

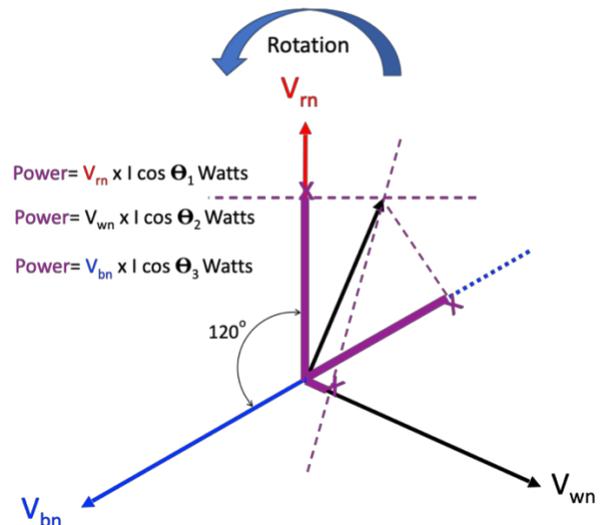
### Teorema de Blondel

If energy is supplied to any system of conductors through N wires, the total power in the system is given by the algebraic sum of the readings of N watt meters, so arranged that each of the N wires contains one current coil, the corresponding voltage coil being connected between that wire and some common point. If this common point is on one of the N wires, the measurement may be made by the use of N-1 watt meters.



### Verificación del vatímetro cruzado

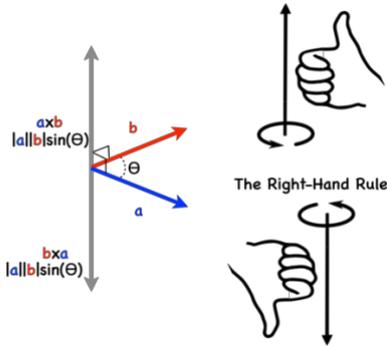
$V_m, V_{wn}, V_{bn}$   
Are reference phasors which are equal in magnitude and 120° apart



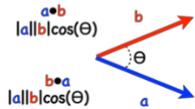
# 13) Máquinas Rotativas

Máquinas de corriente continua

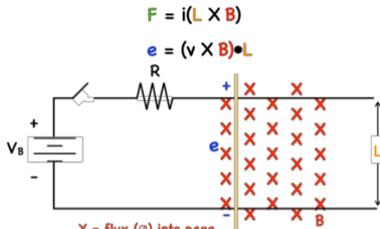
## The Cross Product of Two Vectors



## The Dot Product of Two Vectors

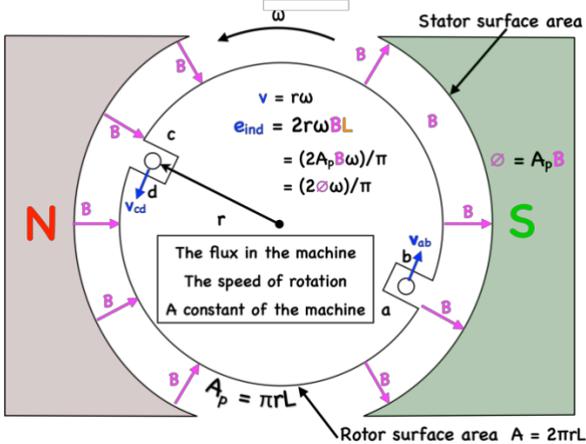


## The Linear DC Machine

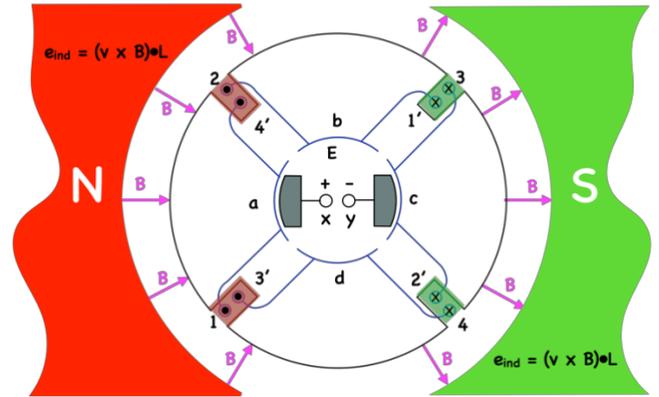


- X = flux ( $\phi$ ) into page
- B = flux density (X/Area)
- L = conductor length (direction defined the same as the current)
- v = velocity of motion
- e = induced voltage (EMF)
- F = force

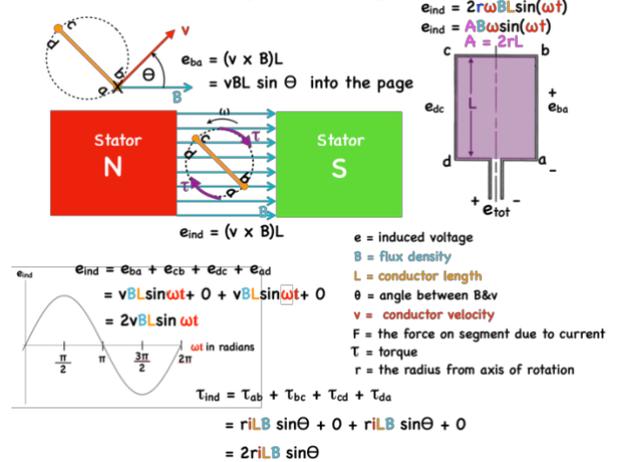
## Rotating DC Machines



## Commutation in a Simple Four-Loop DC Machine

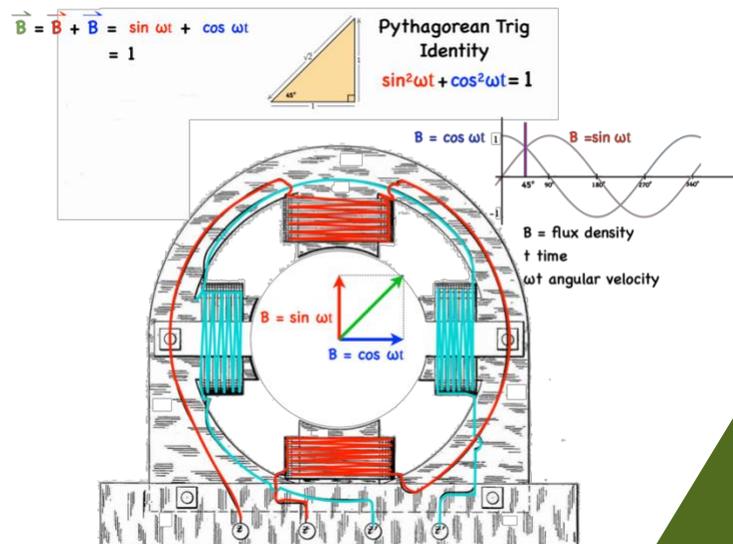


## Induced Voltage in Rotating Loop

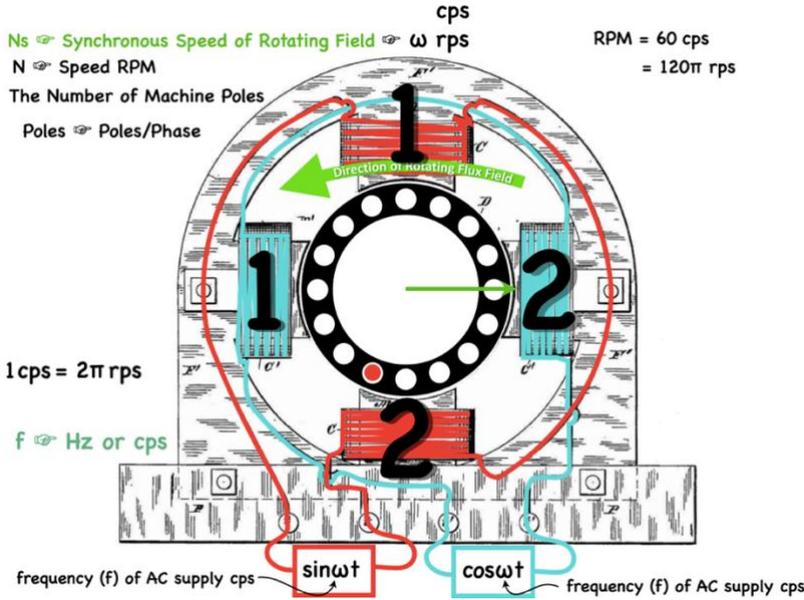


## El motor de inducción

### A Rotating Magnetic Field



Rotores de motores de inducción



$$\% \text{ slip } s = \frac{N_s - N}{N_s} \times 100\% \quad N' = N_s - N \text{ (relative speed)}$$

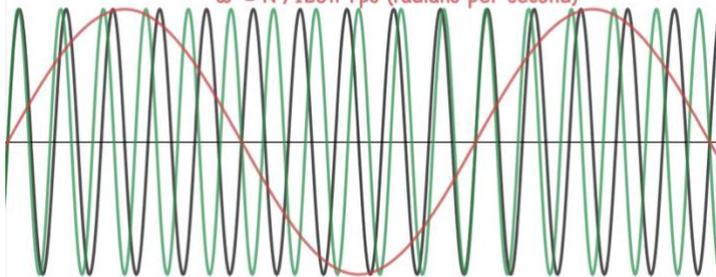
$$e_{ind} = \phi_{max} \omega \sin(\omega t)$$

$e_{ind}$  = induced voltage  
 $B$  = flux density  
 $\omega$  = angular velocity (radians/second)

Rotating Magnetic Field =  $N_s$  RPM =  $60\omega$  cps =  $120\pi\omega$  rps

Rotor =  $N$  RPM

$N' = N_s - N$  RPM Current Frequency =  $\omega'$  rps  
 $\omega' = N'/120\pi$  rps (radians per second)



$$\omega' = \frac{(N_s - N)}{120\pi} = s\omega \quad s = \frac{N_s - N}{N_s}$$

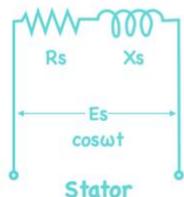
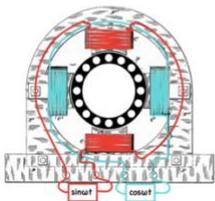
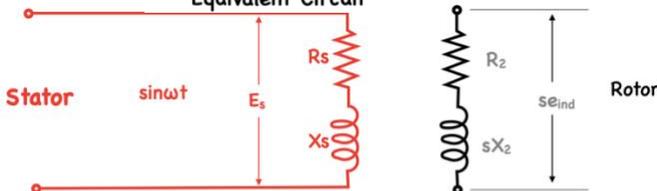
$\omega'$  = frequency in rad/sec  
 $\frac{N_s}{120\pi} = \omega$

$$e_{ind} = \phi_{max} \omega \sin(\omega t) \quad s = 1$$

$$e_{ind} = \phi_{max} s \omega \sin(s\omega t) \quad s < 1$$

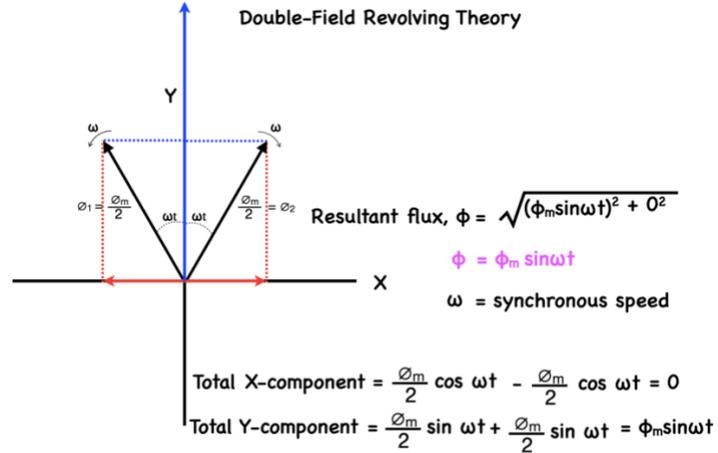
Two Pole Induction Motor

Equivalent Circuit

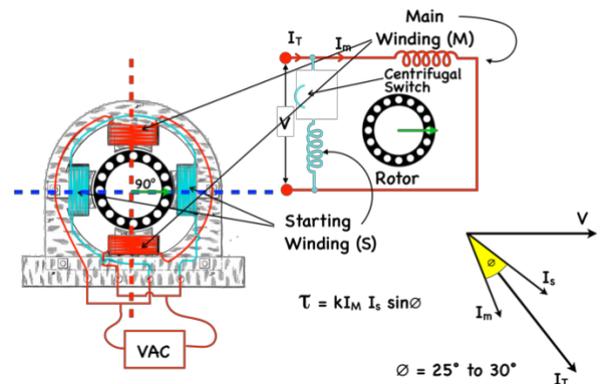


Motores de inducción monofásicos

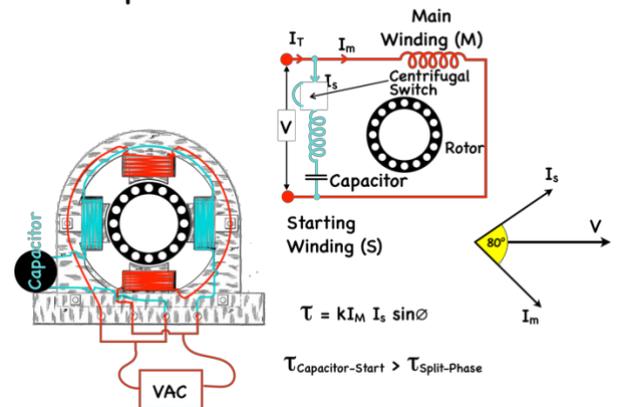
Double-Field Revolving Theory



Split-Phase Induction Motor



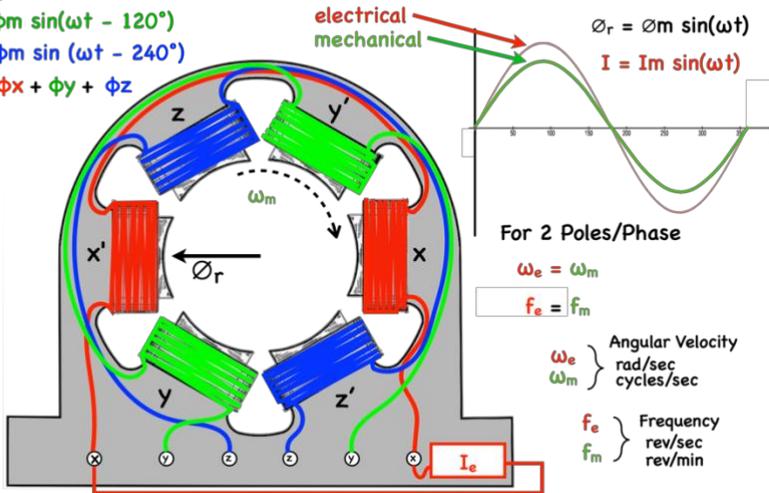
Capacitor-Start Induction Motor



### Motores de inducción trifásicos

Electrical Frequency and the Speed of Magnetic Field Rotation

$$\begin{aligned} \phi_x &= \phi_m \sin \omega t \\ \phi_y &= \phi_m \sin(\omega t - 120^\circ) \\ \phi_z &= \phi_m \sin(\omega t - 240^\circ) \\ \phi_r &= \phi_x + \phi_y + \phi_z \end{aligned}$$



### Rotor Torque

The torque  $T$  developed by the rotor is directly proportional to:

- rotor current  $I_2$
- rotor e.m.f.  $E_2$
- power factor of the rotor circuit  $\cos \phi_2$

$$\therefore T \propto E_2 I_2 \cos \phi_2$$

$$\text{or } T = K E_2 I_2 \cos \phi_2$$

Since  $I_2 = \frac{E_2}{\sqrt{(R_2)^2 + (X_2)^2}}$  and  $\cos \phi_2 = \frac{R_2}{\sqrt{(R_2)^2 + (X_2)^2}}$  at standstill

$$\text{Then } T = K E_2 \times \frac{E_2}{\sqrt{(R_2)^2 + (X_2)^2}} \times \frac{R_2}{\sqrt{(R_2)^2 + (X_2)^2}} = \frac{K(E_2)^2 R_2}{(R_2)^2 + (X_2)^2}$$

Rotating  
Stator  
Field  
Speed =  $N_s$

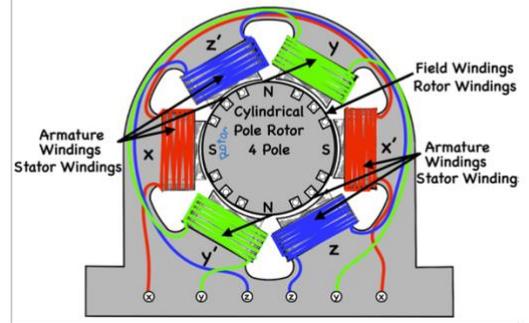
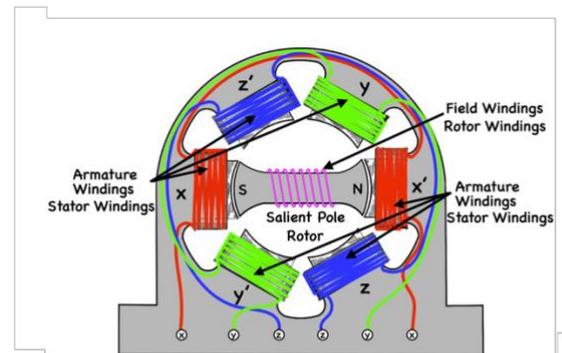
$N_s - N$  slip speed

$$\text{slip } s = \frac{N_s - N}{N_s}$$

$$\% \text{ slip } s = \frac{N_s - N}{N_s} \times 100\%$$

Rotor  
Speed =  $N$

A stationary rotor ( $N = 0$ )  
slip,  $s = 1$  or 100 %



### Rotor Current

At standstill

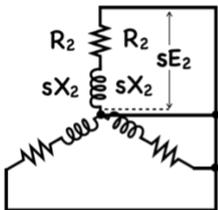
$$\text{Rotor current/phase } I_2 = \frac{E_2}{Z_2} = \frac{E_2}{\sqrt{(R_2)^2 + (X_2)^2}}$$

$$\text{Rotor P. F. } \cos \phi_2 = \frac{R_2}{Z_2} = \frac{R_2}{\sqrt{(R_2)^2 + (X_2)^2}}$$

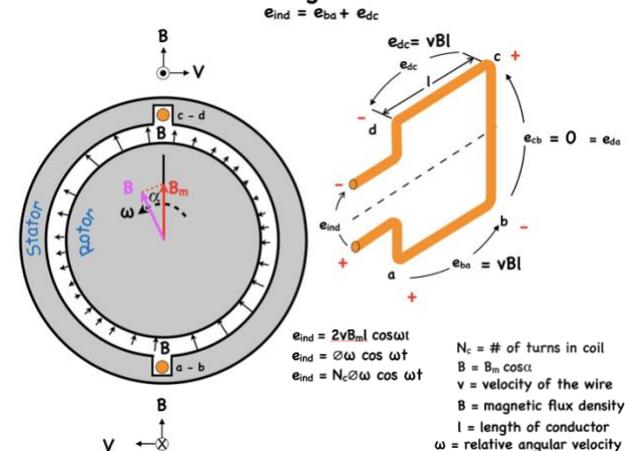
When running at slip  $s$

$$\text{Rotor current/phase } I'_2 = \frac{sE_2}{Z'_2} = \frac{sE_2}{\sqrt{(R_2)^2 + (sX_2)^2}}$$

$$\text{Rotor P. F. } \cos \phi'_2 = \frac{R_2}{Z'_2} = \frac{R_2}{\sqrt{(R_2)^2 + (sX_2)^2}}$$

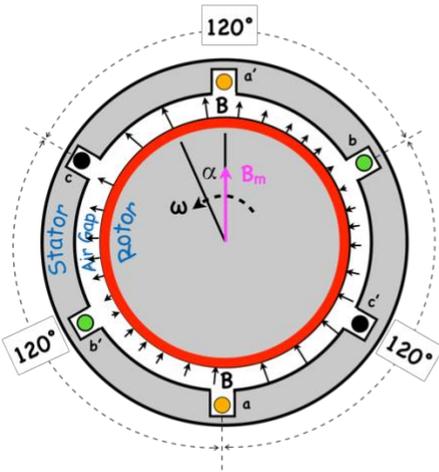


### Three-Phase Induced Voltages



### Three-Phase Induced Voltages (Cont'd)

### El circuito equivalente de un Generador síncrono



$$e_{aa'}(t) = Nc\phi\omega \cos \omega t$$

$$e_{bb'}(t) = Nc\phi\omega \cos (\omega t - 120^\circ)$$

$$e_{cc'}(t) = Nc\phi\omega \cos (\omega t - 240^\circ)$$

$$E_{max} = Nc\phi\omega$$

Since  $\omega = 2\pi f$        $f \rightarrow$  CPS

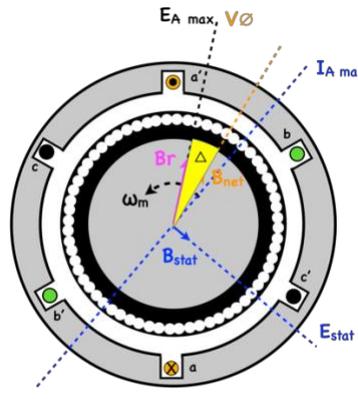
$$E_{max} = 2Nc\phi\pi f$$

**Magnitude**

$$|E_A| = \frac{2\pi}{\sqrt{2}} Nc\phi f$$

$$|E_A| = \sqrt{2} \pi Nc\phi f$$

$f \rightarrow$  cps of magnetic field



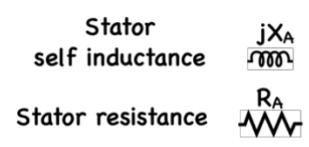
**Armature (stator) Reaction**

$$E_{stat} = -jX_I A$$

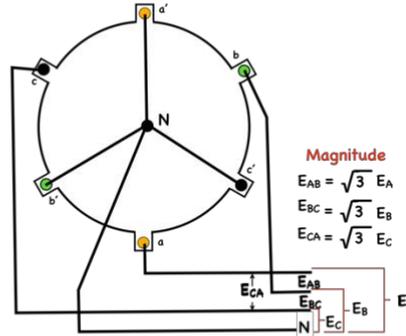
$$V_\phi = E_A - jX_I A$$

$$V_\phi = E_A + E_{stat}$$

$$B_{net} = B_r + B_{stat}$$



#### Y-Connected



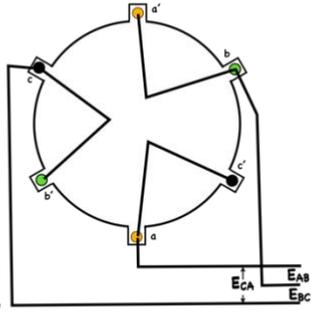
**Magnitude**

$$E_{AB} = \sqrt{3} E_A$$

$$E_{BC} = \sqrt{3} E_B$$

$$E_{CA} = \sqrt{3} E_C$$

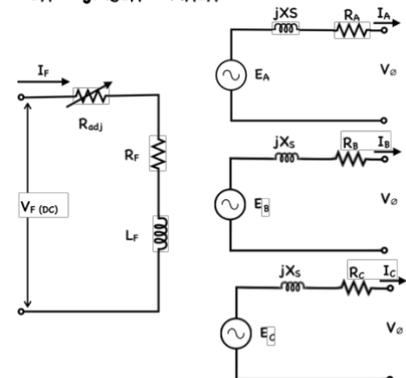
#### Delta(Δ)-Connected



$$V_\phi = E_A - jX_A I_A - jX_A I_A - R_A I_A$$

$$X_S = X + X_A$$

$$V_\phi = E_A - jX_S I_A - R_A I_A$$



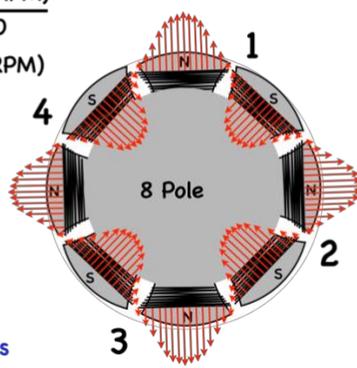
Rotor Speed =  $f$  cps

Induced Voltage Frequency of an  $P$  Pole Rotor =  $\frac{P}{2} \times f$  cps

$$f_e \text{ (cps)} = \frac{P}{2} f_r \text{ (cps)}$$

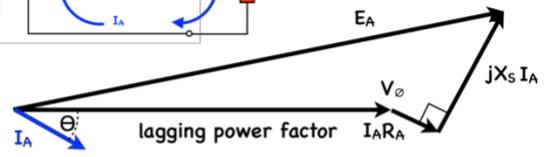
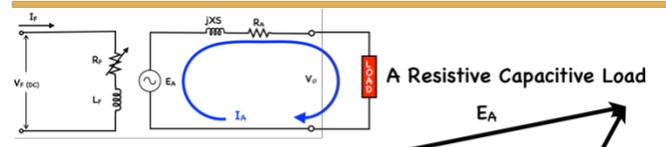
$$f_e \text{ (cps)} = \frac{P}{2} \frac{f_r \text{ (RPM)}}{60}$$

$$f_e \text{ (cps)} = \frac{P}{120} f_r \text{ (RPM)}$$

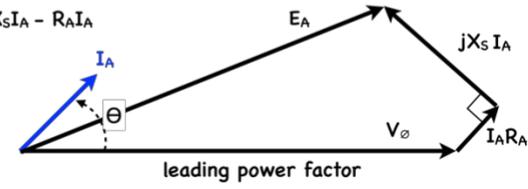


As the rotor completes one cycle the induced stator voltage coil will go through 1/2 the number of cycles as there are pole on the rotor.

$P$  = number of poles  
 $f_e$  = electrical frequency, in Hz (cps)  
 $f_r$  = mechanical speed of the rotor



$$V_\phi = E_A - jX_S I_A - R_A I_A$$



The Phasor Diagram of a Synchronous Generator

**Droop** ☞ Drop in frequency of the generator as load increases

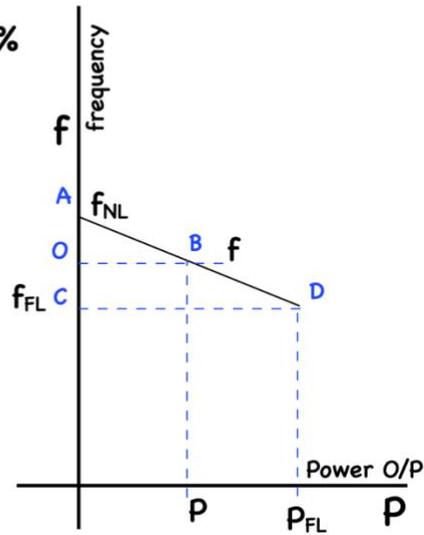
$$\text{droop} = \frac{f_{NL} - f_{FL}}{f_{FL}} \times 100\%$$

$$\triangle AOB \cong \triangle ACD$$

$$OB = \frac{AO}{AC} \times CD$$

$$P = \frac{f_{NL} - f}{f_{NL} - f_{FL}} \times P_{FL}$$

$$f = f_{NL} + \frac{f_{FL} - f_{NL}}{P_{FL}} P$$



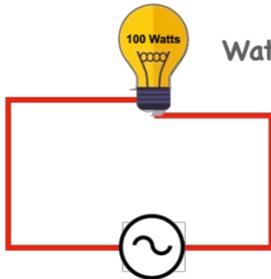
# 14) Cableado eléctrico de bajo voltaje

All electrical circuits have:

1) Voltage, 2 ) Current and 3) Resistance 4) Watts

$$\text{Current} = \frac{\text{Voltage}}{\text{Resistance}}$$

$$I = \frac{V}{R}$$



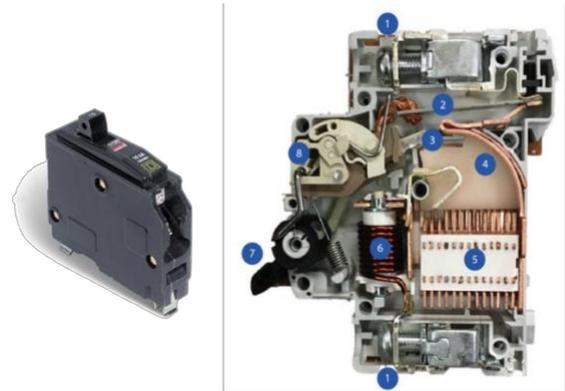
Watts = Current x Voltage

$$W = I \times V$$

$$W = I^2 \times R$$

$$W = \frac{V^2}{R}$$

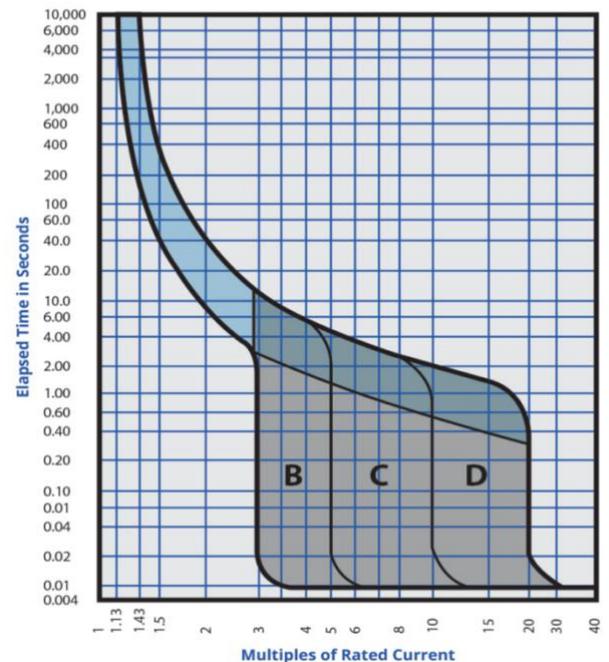
## Rompedores de circuito



- ① Terminal for line/load power.
- ② Bi-metallic strip. Bends with heat (current).
- ③ Contacts. Current flows through when closed.
- ④ Arc Chamber.
- ⑤ Arc divider/extinguisher.
- ⑥ Coil/Solenoid. Response to high overcurrents
- ⑦ Actuator lever. Manually trips or resets.
- ⑧ Actuator mechanism. Forces contacts together or apart.

American Wire Gauge (AWG)	
AWG	Current (amps)
2	95
3	85
4	70
6	55
8	40
10	30
12	20
14	15
16	13
18	10

## Different Types of Breaker Trip Curves



THHN – Thermoplastic High Heat-resistant Nylon-coated wire  
 THWN – same as THHN, "W" water- resistance  
 Romex – Thermoplastic-Sheathed Cable (TPS) NM-D, or B.

### Wire Size

### Breaker Rating

14-2 Copper Wire



15 Amp

12-2 Copper Wire



20 Amp

12-3 Copper Wire



20 Amp

10-2 Copper Wire

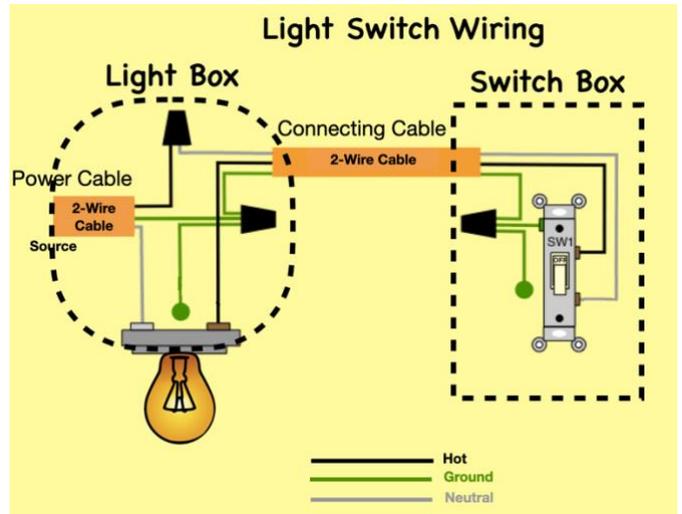
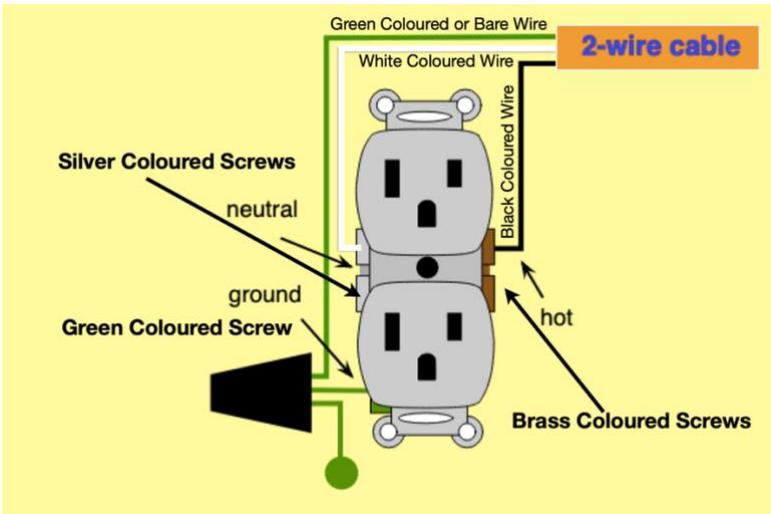


30 Amp

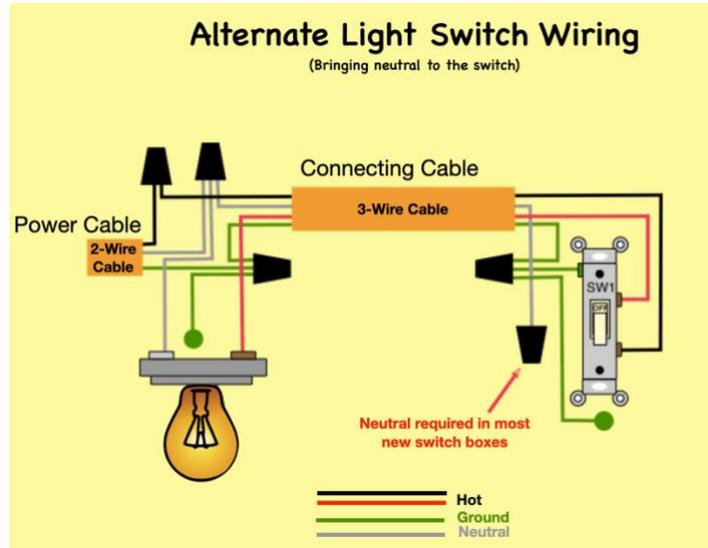
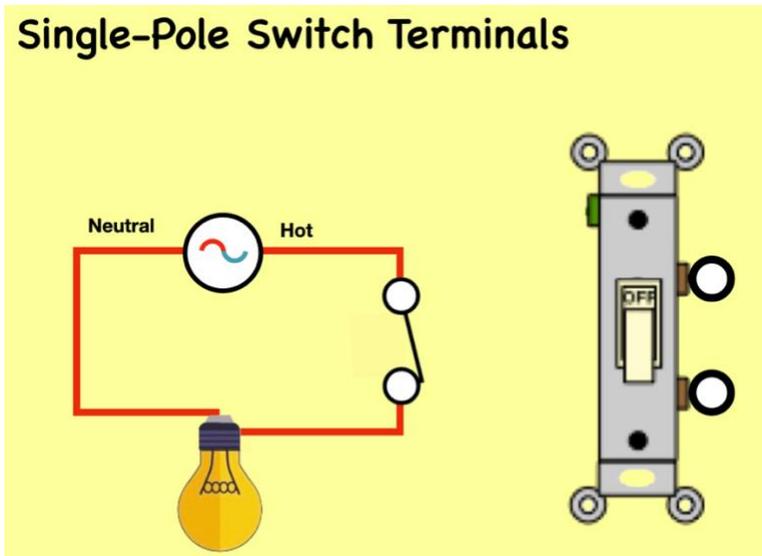
10-3 Copper Wire



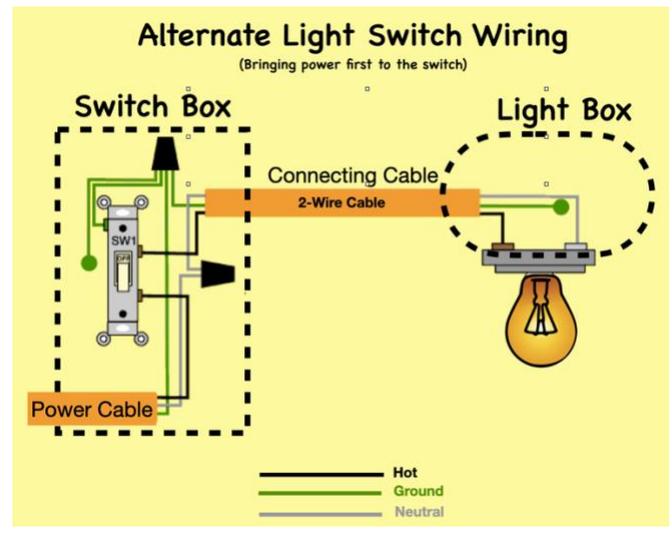
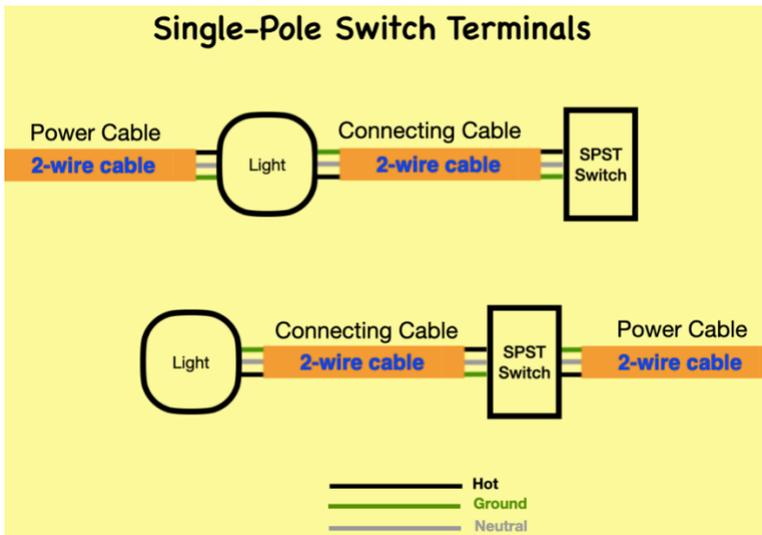
30 Amp



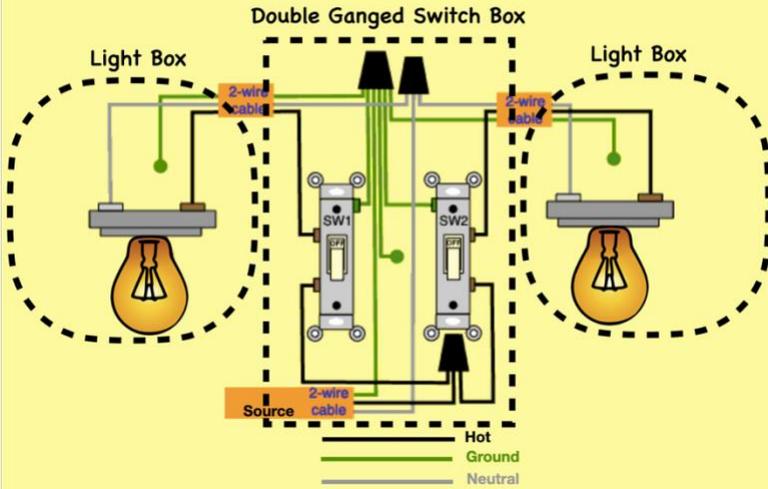
### Single-Pole Switch Terminals



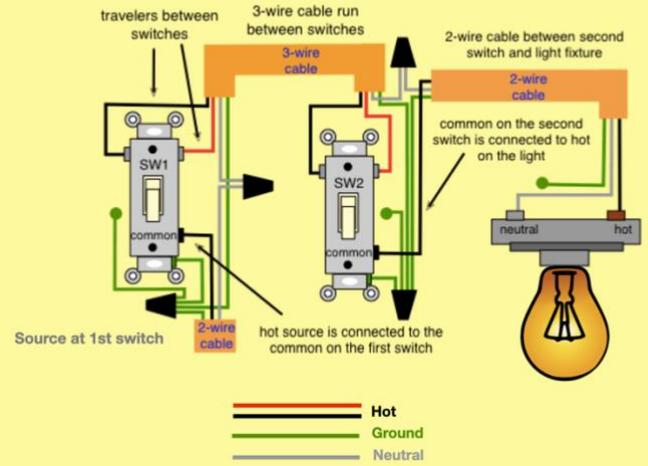
### Single-Pole Switch Terminals



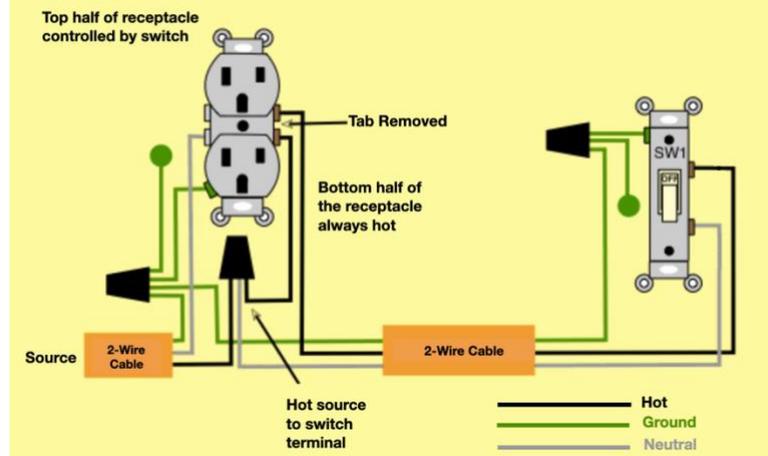
### Alternate Light Switch Wiring



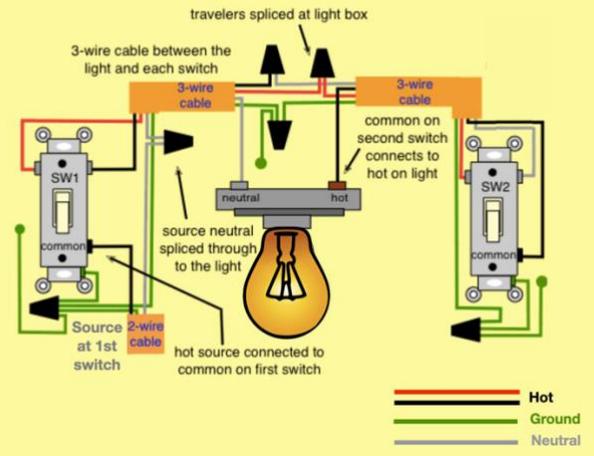
### 3 Way Switch with Light at the End



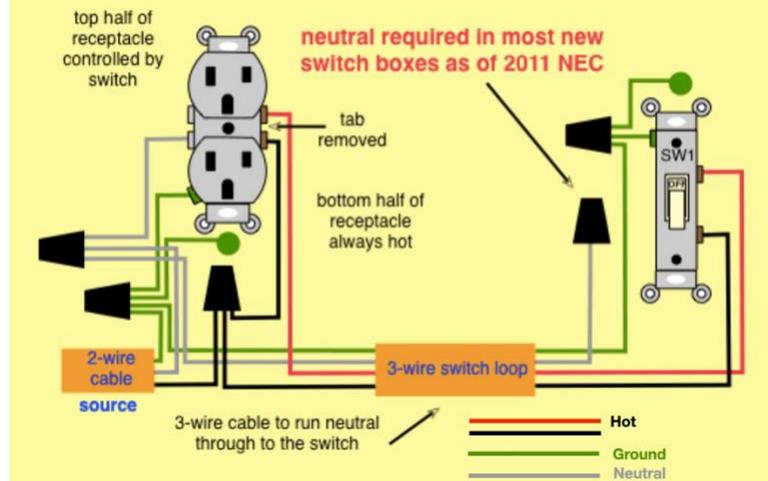
### Wiring a Switch to a Wall Outlet



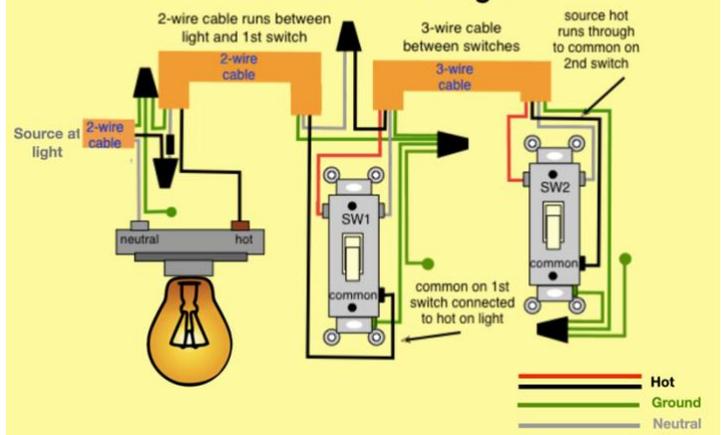
### 3 Way Switch Wiring with Light Middle



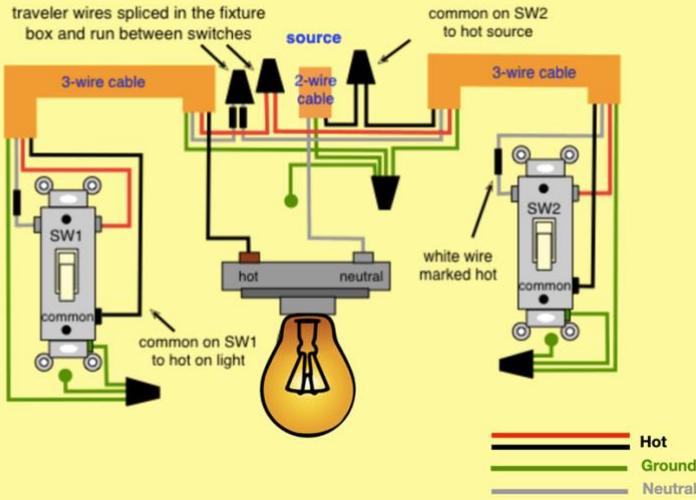
### Wiring a Switch to a Wall Outlet



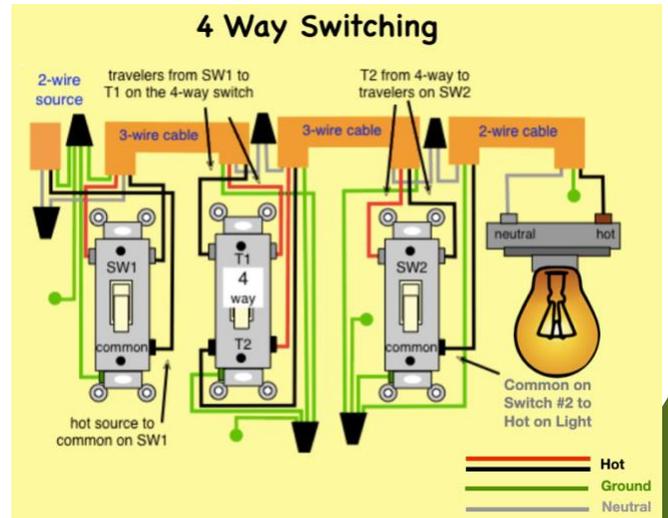
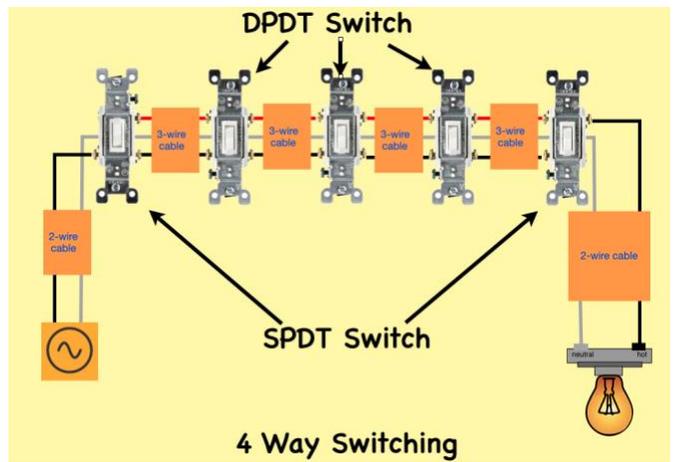
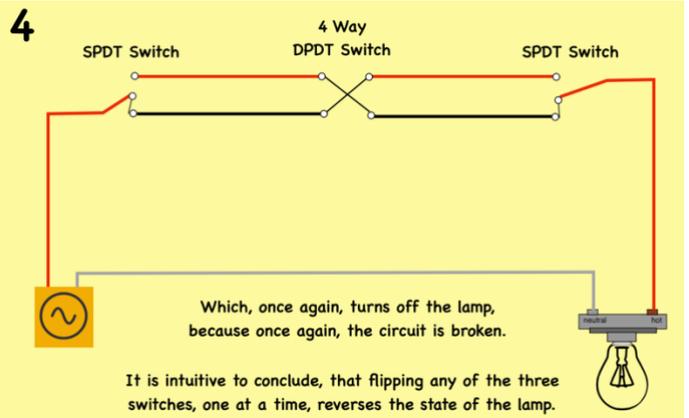
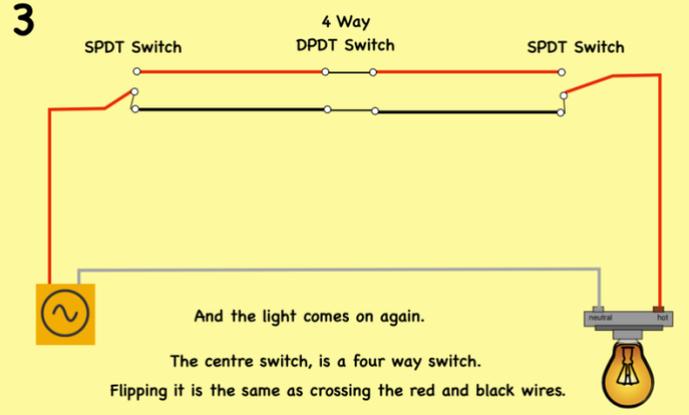
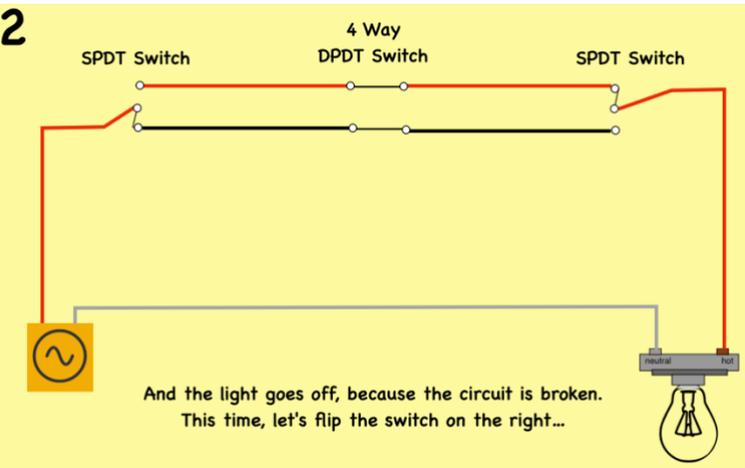
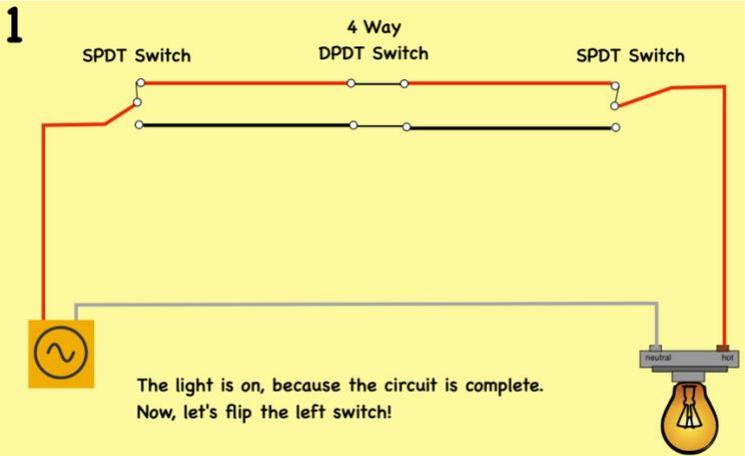
### 3 Way Switch Wiring with Source to the Light

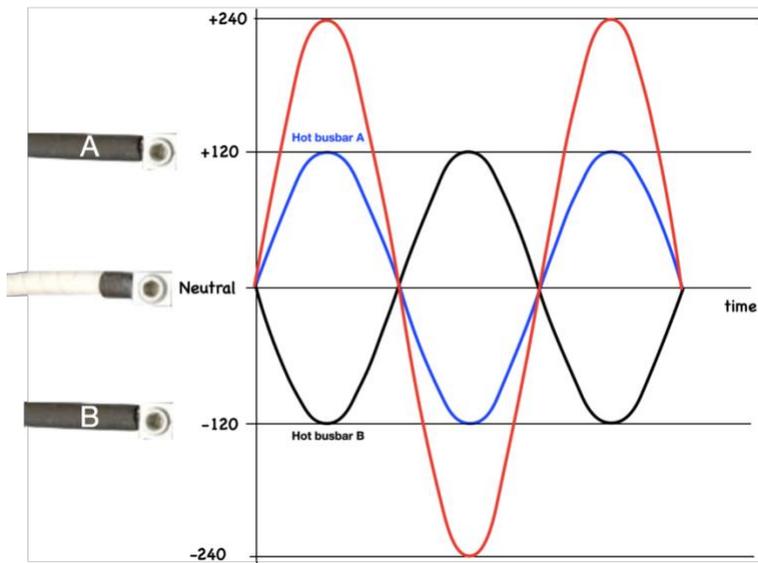
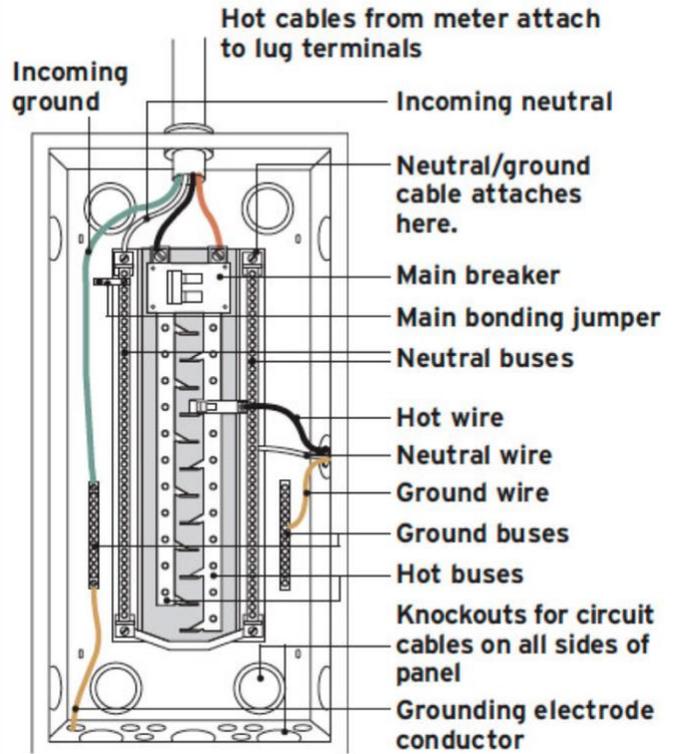
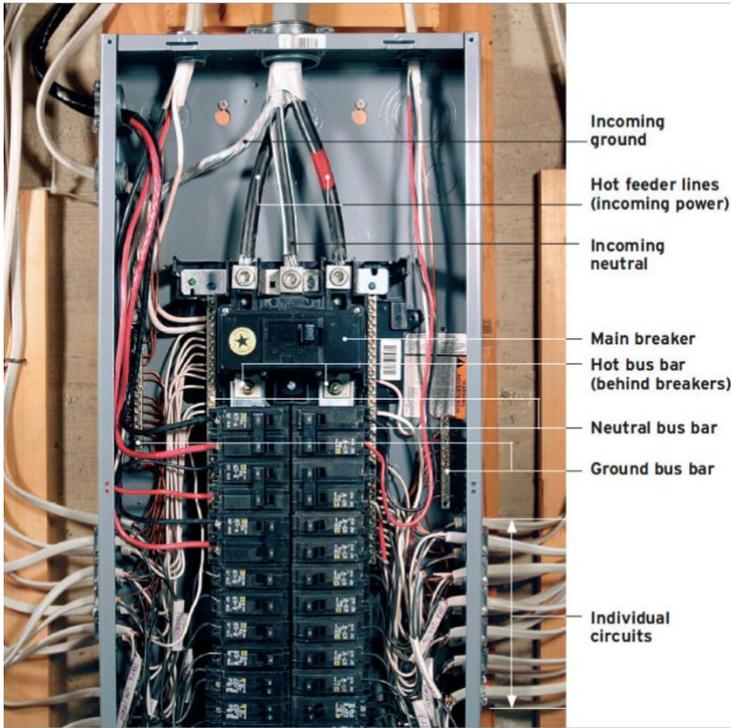


### 3 Way Switch Wiring with Source to the light in the Middle



Las siguientes cuatro diapositivas demuestran esquemáticamente cómo se conecta y funciona un interruptor de cuatro vías.

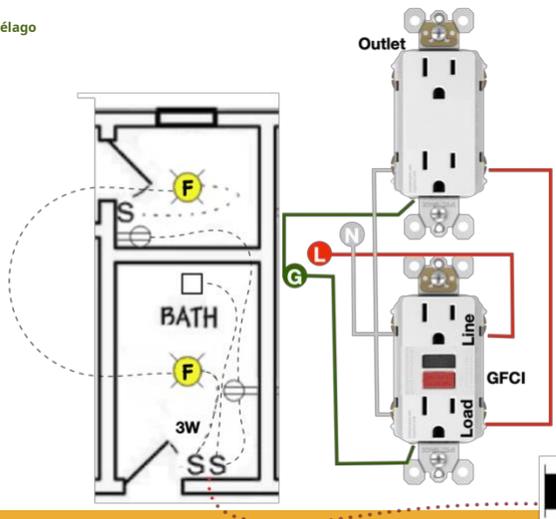


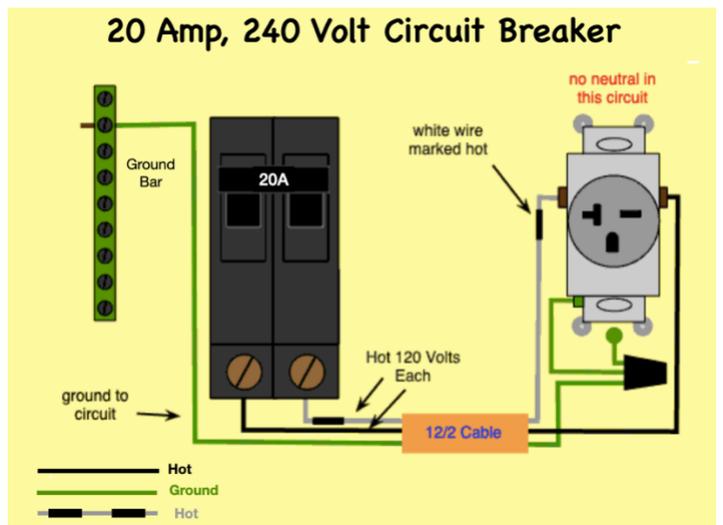
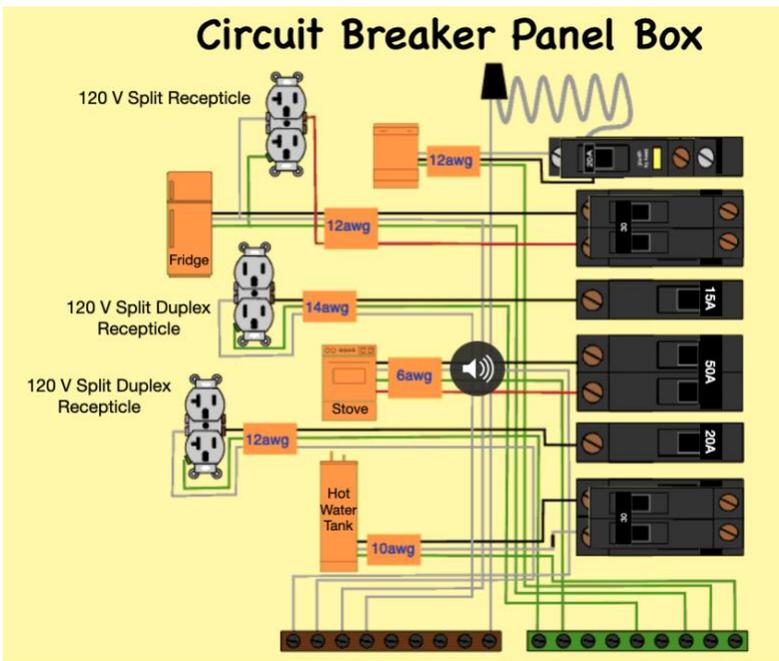
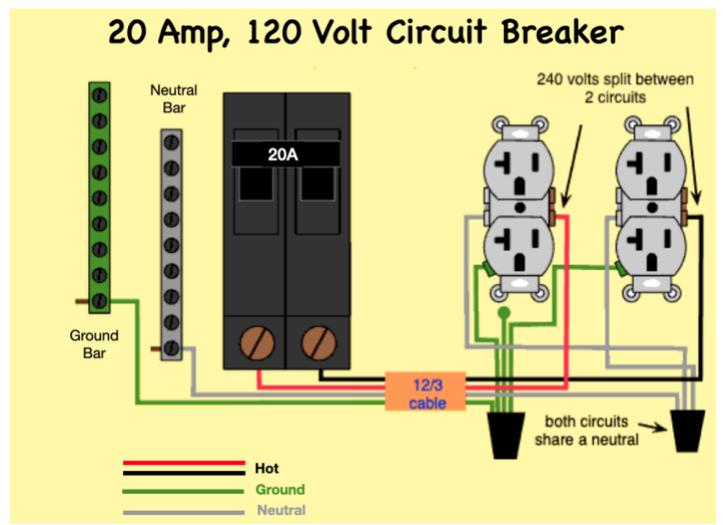
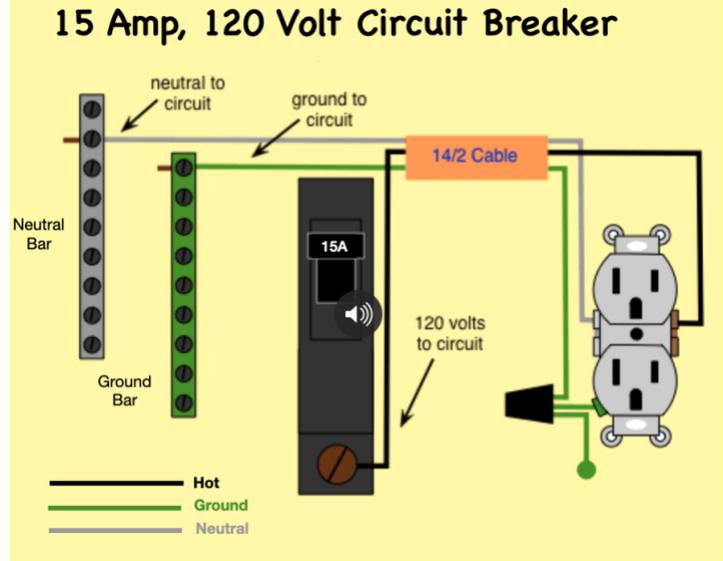
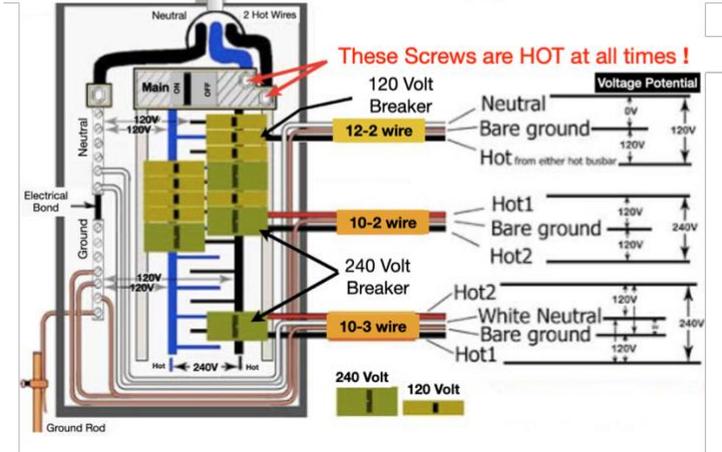
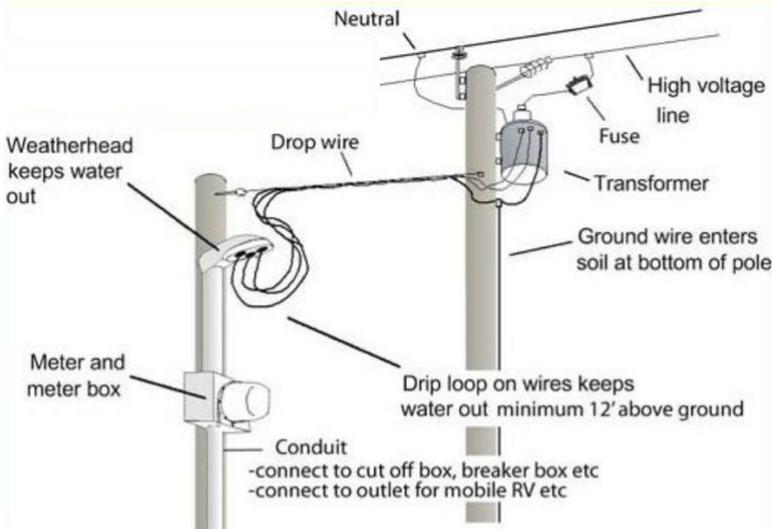


Símbolos estándar del diagrama de cableado doméstico

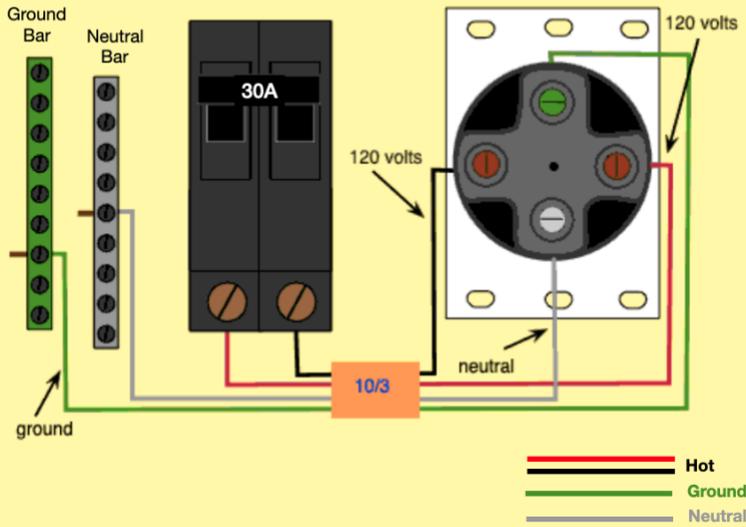
	Electrical switchbox		Single Pole Switch
	Three-Way Switch		SinglePlex Receptacle
	Duplex Receptacle		Duplex Receptacle WP= Waterproof
	GFCI Duplex Receptacle		Isolated Ground Receptacle
	Switched Receptacle		FourPlex Four Gang Receptacle
	240-Volt Receptacle		Ceiling Mounted Light Fixture PC= Pullchain
	Wall-Mounted Light Fixture		Recessed Light Fixture
	Weatherproof Light Fixture		Fluorescent Light Fixture
	Ceiling Fan		Combination Light & Fan
	Power Vent Fan		Electric Motor Number=HP
	Smoke Detector		Circuit Breaker
	Telephone Jack		Doorbell Transformer
	Doorbell Pushbutton		Ground

Murciélago

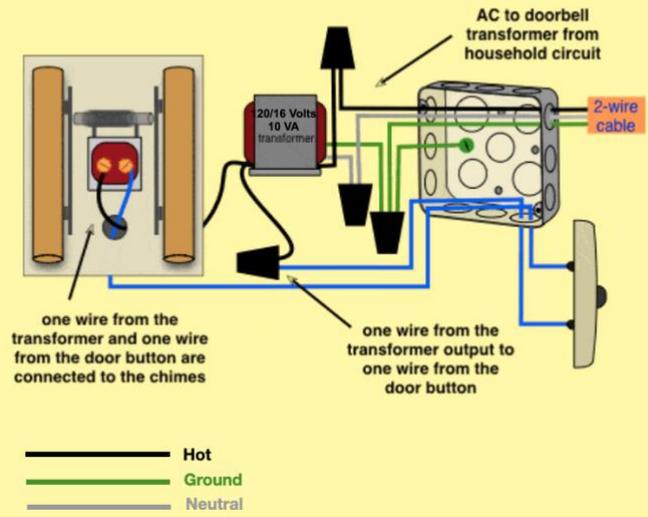




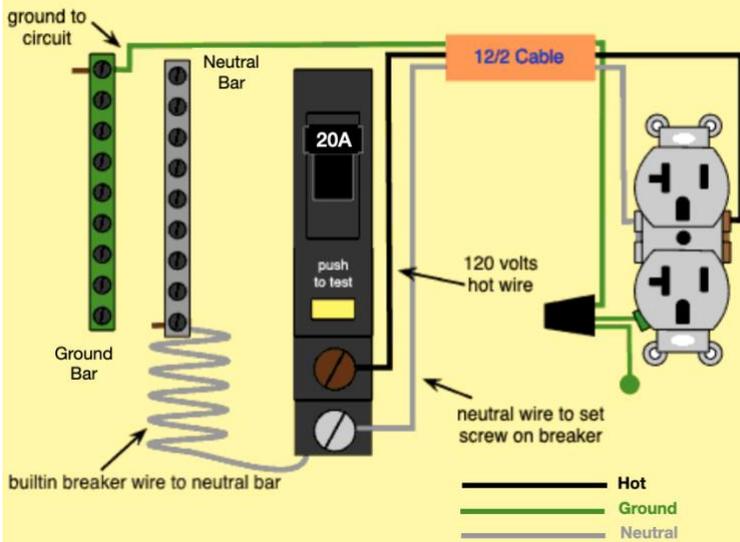
### 30 Amp, 240 Volt Circuit Breaker



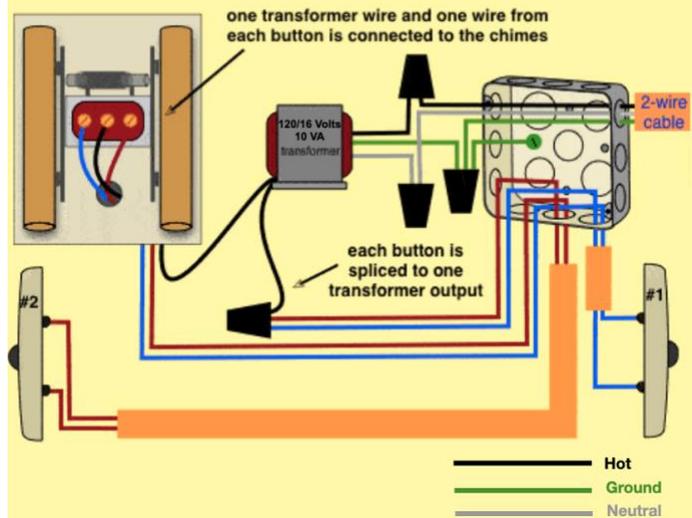
### Doorbell Wiring



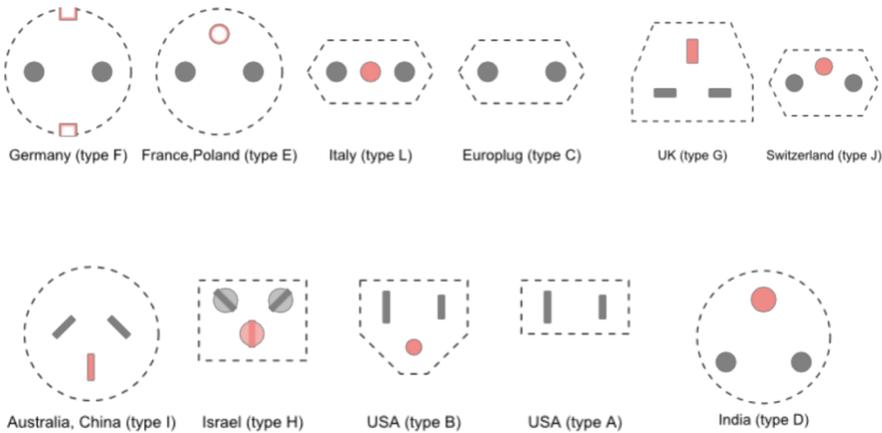
### 20 Amp, GFI Circuit Breaker



### Doorbell Wiring



### Tipos de puntos de venta en todo el mundo



### Check the Label on the Wire Nuts Packaging

Model	AWG wire sizes fit for	Dimensions (Millimet)	Color	Material
SP1	MIN 2X#22 MAX 2X#16	0.59x0.34 inch	Grey	Screw terminals: copper Insulated screw tube: nylon
SP2	MIN 2X#22 MAX 3X#16	0.69x0.4 inch	Blue	
SP3	MIN 1X#18+ 1X#20 MAX 4X#16 MAX 1X#20	0.87x0.49 inch	Orange	
SP4	MIN 2X#18 MAX 4X#16 MAX 1X#18	0.96x0.54 inch	Yellow	
SP5	MIN 2X#14 MAX 4X#10 MIAx 2X#12	1.05x0.63 inch	Red	